

# Rank Fusion

## Information Retrieval Project

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**Abstract—** Recently researches have focused on the idea that performance and the effectiveness of individual IR models can be improved by combining the outputs of some individual models into a single result set. Data fusion is the combination of the results of independent searches on a document collection into one single output result set. In fact, ranking quality can be achieved by adopting different strategies and so different retrieval models. In this regard, we have implemented some rank fusion base strategies to perform retrieval experiments by generating runs and by comparing their individual results with results obtained by ten runs of different systems through Terrier. Afterwards, we have implemented an advanced rank fusion strategy called ProbFuse to perform another results comparison and to look for eventual improvements compared to the popular fusion algorithms. We have reported also a ProbFuse variant after the IIX section namely ProbFuse Variant, whose explanations can be found in the VII section namely Implementation Issues.

### I. INTRODUCTION

It has been shown in the past that rank fusion can greatly improve retrieval effectiveness over that of the individual results. This improvement can be achieved by evaluating the results obtained by implementation of different rank fusion algorithms and by the developing and comparing new rank fusion techniques. In this work ten runs have been generated through Terrier by choosing different IR models to catch all the important features from the given files collection. Then, we have implemented the following classical rank fusion algorithms: CombSUM, CombMAX, CombMNZ, CombANZ and CombMIN. Through these ones we have assessed the generated runs and compared them

with those ones previously obtained through Terrier. Finally, we have realized the ProbFuse algorithm described in the reference paper: an interesting method that could led us to the achievement of better IR results. ProbFuse's idea consists in ranking documents based on their probability of relevance to the given topic in a certain k segment. This probability depends on which input system returned the document in its results and the position in which it is returned in the result set. The inputs to the fusion process are produced by different IR models that use the same topics on the document collection. At the beginning of this implementation we had realized a similar but different algorithm by considering the different lengths of the various runs, then we have corrected our initial hypothesis and followed the ProbFuse paper indications. We have reported also this one in the last section.

### II. COLLECTION FILE UNPACKING

At the beginning it has been difficult decompress the collection files. It has been discovered that Terrier's 4.2 version was bugged and so we had to use the 4.1 version to unpacked all the files. The zip file to be decompressed needed one decompression program but it contained other zipped files that needed another decompression program, they were compressed by using Unix. Some file were named with their names followed by an integer number and their extension names, such as if they were divided in small groups. They needed to be renamed, so it has been written a bash file to specify how to rename and decompress them automatically.

### III. INDEXING

It has been used Terrier to index Trec collection. At the beginning, it was unknown what was the correct format and the exact markup structure to adopt for the given collection for Terrier, so it has

been complicated to understand how to set up the properties file and create the indexing with the appropriate lexical analysis, stop-word removal, stemmer and the other settings. The stop-list and the stemmer used for indexing are those ones of Terrier used for English language, the stemmer is PorterStemmer.

#### IV. CHOICE OF IR MODELS FOR RUN GENERATION

The following models have been chosen though Terrier to generate ten runs to evaluate subsequently:

- 1) TFIDF
- 2) BM25
- 3) DFRBM25 (DFR)
- 4) LGD (DFR)
- 5) PL2 (DFR)
- 6) InexpC2 (DFR)
- 7) InL2 (DFR)
- 8) DLH13 (DFR)
- 9) IFB2 (DFR)
- 10) BB2 (DFR)

These are very different models based in sundry approaches, some of them have something in common, other use different functions if we compare them to some others, so they are different each other generally. In this way, the rank fusion should achieve better results, because if it takes values from all the individual models, it can capture collection qualities and strength elements given by these and so the fusion should report better results.

#### V. NORMALIZATION

The normalization used in this work has been the Standard Normalization which calculates normalized scores by using the maximum and the minimum scores given in the result set. The minimum score is subtracted to the unnormalized score of each run element and then this result is divided for the difference between the maximum score and the minimum score. After the score normalization, the followed combination functions for the scores combination have been implemented: CombMAX, CombSUM, CombMNZ, CombMIN, CombANZ. They allow to carry out the rank fusion.

#### VI. PROBE FUSE ALGORITHM

ProbFuse algorithm needs to build a set of probabilities for each input model. The analysis of the performance of each individual model on training

queries allow to calculate these probabilities. To calculate these probabilities we need runs given by the individual models and to divide each topic of each run in  $k$  segments. For each segment we count relevant and not relevant documents and we calculate the probability considering each relevant document  $d$  returned by query considering each topic. So, for each segment we want to calculate the probability that a relevant document returned in this segment is relevant according to the given query. Each probability is obtained by the relationship between the number of documents in segment  $k$  that are judged to be relevant to query  $q$  and the number of documents in  $k$  segment that are judged to be relevant added to those ones that are judged to be non relevant to the query.

$$P(d_k | m) = \frac{R_k}{R_k + NR_k}$$

Then, on the various runs it is calculated the sum of the probabilities previously calculated with weight  $\frac{1}{k}$ ,  $k$  indicates the number of segment where it appears. The final score is the result of the followig sum:

$$s_d = \sum_{m \in M} \frac{P(d_k | m)}{k}$$

Thus, the resulting elements will form the fused run by using the probabilities calculated. We have considered before twenty segments and subsequently fifty segments, because these ones have produced more satisfying results in ProbFuse paper and we wanted to test with these ones. Subsequently we have tried ProbFuse with other  $k$  values, in particular: seventy, ninety and hundred and ten segments, because by increasing the number of segments we obtained results improvements. In fact, in assessment phase we have discovered that we can obtain better results by using one hundred and ten segments. We have also implemented another similar approach to ProbFuse. We'll discuss about it in the last section called "ProbFuse variant".

#### VII. IMPLEMENTATION ISSUES

At first, it occurred a lot of time to execute main, the reading phase was very slow; the slowness was due to the structure used for Standard Rank Fusion functions. This problem has been solved by changing the structure from List to HashMap. In these functions the research by score of run

elements needed to iterate all run elements list, so complexity was  $O(n)$ . Instead, by introducing HashMap structure the access for example to the element with maximum score value can occur directly. In this way the complexity is reduced to  $O(1)$  and main program can be executed in few minutes. During the printing phase on file there was another problem: during this operation, after the execution of for cycle that iterates inside the run, it was created a single string. It took run's rows and created a single string that was passed to an object which wrote a single string on file, but the string object was immutable and so every time it was created a new object copied by precedent string that added the new row. This caused copy of every run rows. This has been solved by using an object able to write on file through enqueueing elements inside a buffer, so that an element can be enqueued after the previous, the copy is avoided and the problem disappears. Furthermore, when we have started to implement ProbFuse algorithm we thought we had to consider run's subparts composed by  $k$  documents instead to divide each run in  $k$  segments, because the various runs have different number of documents for each topic, so there are different lengths to consider for the given collection. We thought that the difference of lengths could be a problem in the calculation of the probabilities required by ProbFuse algorithm, but finally we have followed the correct instructions of ProbFuse paper for its implementation and we have reported also this our ProbFuse variant.

### VIII. RUN ASSESSMENT

We have used Matters library to assess all the different strategies adopted in this work and so to calculate all the necessary assessment measures and generate some plots. The principal measures performed for the various comparisons have been: the calculation of precision in different cut-off levels, RPrec, Average Precision and Mean Average Precision (MAP). Precision has been calculated by considering ten and thirty cut-off levels because for many research tasks is important to consider results ranking in a certain range, and so to mark runs that have relevant documents in high positions. At this purpose, we have considered ten and thirty cut-off levels according to the tasks' needs. We have calculated also precision with cut-off level equal to the recall base (the number of the relevant documents

in the pool for a certain topic), that currently is one of the most important measures used for IRs assessment. Instead, Average Precision is another important measure presently used that gives more power to relevant documents which correspond to high rank. Finally it has been calculated Mean Average Precision through Average Precision values calculated previously. By comparing measures between runs evaluated by Terrier and those returned by standard rank fusion implemented algorithms, it has been noticed that on average the measures values of the different strategies are very similar. The comparison between MAP measures, we have reported, can confirm this.

TABLE I  
MAP VALUES

ComMNZ	ComMAX	ComSUM	CombANZ	CombMIN
0.1871	0.1831	0.1874	0.1833	0.1301

BB2	BM25	DFR_BM25	TF-IDF	DLH	IFB2
0.1882	0.1828	0.1835	0.1821	0.1830	0.1881

InL2	In_expC2	LGD	PL2
0.1854	0.1826	0.1882	0.1683

Higher values can be obtained through rank fusion standard methods for some topics, but there are also some lower values for other topics compared to runs generated by Terrier. This difference is very small so it can be considered negligible. We have reported Average Precision plot considering the three best standard rank fusion strategies compared with the best three runs evaluated by Terrier derived from three IR models previously choosen.

By calculating the assessment measures of rank fusion obtained with ProbFuse we have obtained the best results by considering one hundred and ten segments.

The increasing of the number of segments is proportional to the improvement of assessment measures results. This can be noticed by looking the following MAP measures for different ProbFuse  $k$  segments reported.

TABLE II  
PROBFUSE MAP VALUES

k=110	k=90	k=70	k=50	k=20
0.1585	0.1475	0.1260	0.1106	0.0696

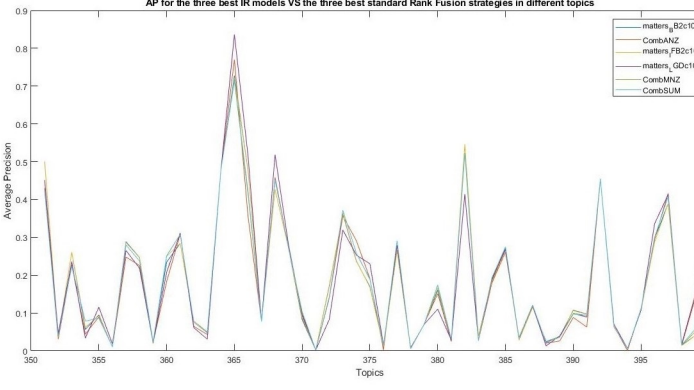


Fig. 1. Average Precision for the three best standard Rank Fusion strategies VS the best three IR models in different topics

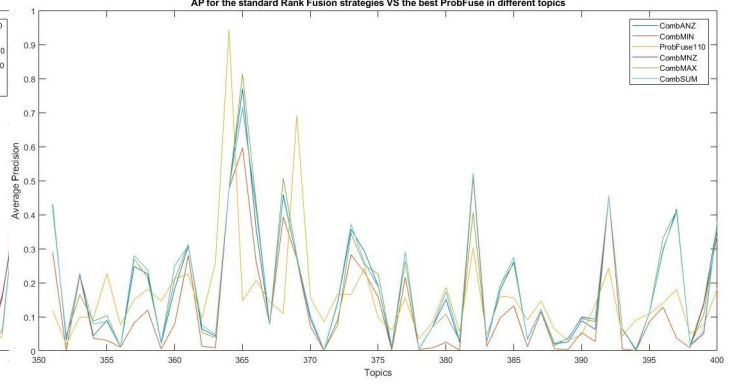


Fig. 3. Average Precision for Standard Rank Fusion strategies VS the best ProbFuse in different topics

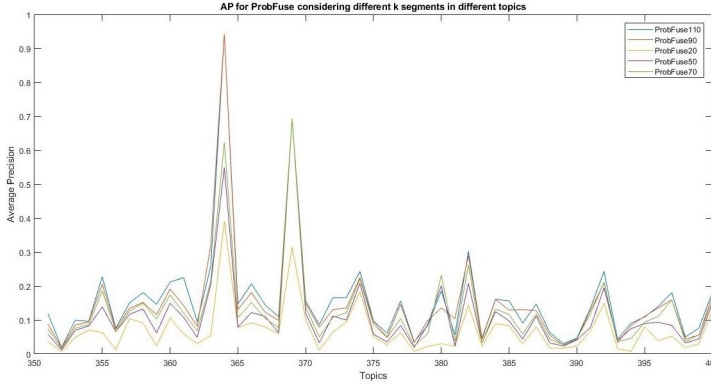


Fig. 2. Average Precision for ProbFuse considering different k segments in different topics

Furthermore, we have noticed that all the assessment values obtained through the different measures aren't very similar with those ones of the standard rank fusion strategies.

In the better ProbFuse obtained (considering one hundred and ten segments) we have observed better results for topics from 354 to 356, from 362 to 365, from 368 to 371 and for 380.

This can be seen by observing the plot in the Fig.3.

We have also reported small examples where ProbFuse results are better than those obtained through standard strategies for different assessment measures in the following tables.

## IIX. CONCLUSION

We have implemented standard rank fusion strategies and ProbFuse algorithm, a data fusion algorithm that relies on the probability of relevance to calculate a ranking score for documents in a

TABLE III  
COMPARISON FOR AVERAGE PRECISION VALUES

T	ComMNZ	ComMAX	ComSUM	ProbFuse
355	0.086124	0.10336	0.086233	0.227280
363	0.047316	0.039032	0.047187	0.258369
380	0.17362	0.10718	0.17408	0.185909

TABLE IV  
COMPARISON FOR RPREC VALUES

T	ComMNZ	ComMAX	ComSUM	ProbFuse
363	0.125	0.0625	0.125	0.25
387	0.1176	0.1412	0.1176	0.1529
394	0.058824	0	0.058824	0.1176

TABLE V  
COMPARISON FOR PRECISION VALUES AT TEN CUT-OFF LEVEL

T	ComMNZ	ComMAX	ComSUM	ProbFuse
363	0.2	0.1	0.2	0.3
369	0.3	0.3	0.3	0.9
374	0.4	0.4	0.4	0.7

TABLE VI  
COMPARISON FOR PRECISION VALUES AT THIRTY CUT-OFF LEVEL

T	ComMNZ	ComMAX	ComSUM	ProbFuse
359	0.033333	0.033333	0.033333	0.2000
370	0.1	0.13333	0.1	0.3333
379	0.033333	0.033333	0.033333	0.1333

fused result set. These probabilities are calculated based on the position of relevant documents in result sets returned in response to the collection's queries. For this collection, full relevance judgments were available, so all the document were just been judged. By assessing the fused result set given by the different strategies adopted, we have discovered

that standard rank fusion strategies are able to achieve results very similar to those obtained through fused result set derived from runs given by different individual models evaluated by Terrier. For some topics, the use of standard strategies has led to achieve results even better than these last. Instead, by comparing fused result set obtained through ProbFuse algorithm and those of standard strategies we have obtained better results for some topics that have been cited previously, for many others topics we have obtained similar results and for about ten topics the results achieved were worse than those derived from standard rank fusion strategies.

### IX. PROBFUSE VARIATION

In this other ProbFuse implementation we have considered run's subparts of each individual model containing  $k$  documents instead to divide runs in  $k$  segments. We have considered different sizes for these subparts, in particular we have tested them considering fifteen, twenty, thirty and fifty documents. In the assessment phase we have obtained the best results with subparts of fifteen documents. In general, results obtained by considering all the assessment measures have been lower than original ProbFuse algorithm as can be seen by Fig.4, but for a few specific topics the output results have been even better than those obtained through standard rank fusion algorithms implemented.

TABLE VII  
PROBFUSE VARIANT MAP VALUES

k=15	k=20	k=30	k=50
0.1083	0.0951	0.0842	0.0689

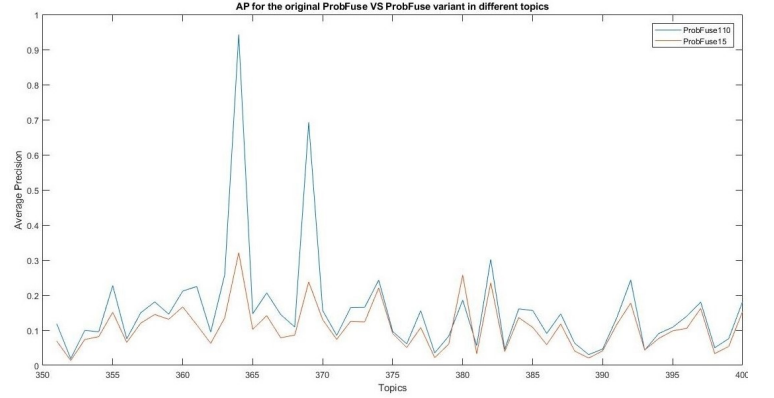


Fig. 4. Average Precision for this ProbFuse variant VS the original ProbFuse (with  $k=110$  segments) in different topics