

```
!pip install yfinance --upgrade --no-cache-dir

import yfinance as yf
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns

sns.set(style='whitegrid')

acoes = ['CSMG3.SA', 'KLBN11.SA', 'PETR4.SA', 'VALE3.SA', 'TAE11.SA', 'BBAS3.SA']

ydata = yf.download(acoes, '2018-01-01', '2023-12-31', '1d');
dados = ydata["Adj Close"]

[*****100%*****] 6 of 6 completed

dados = dados *100 / dados.iloc[0]
display(dados)
```

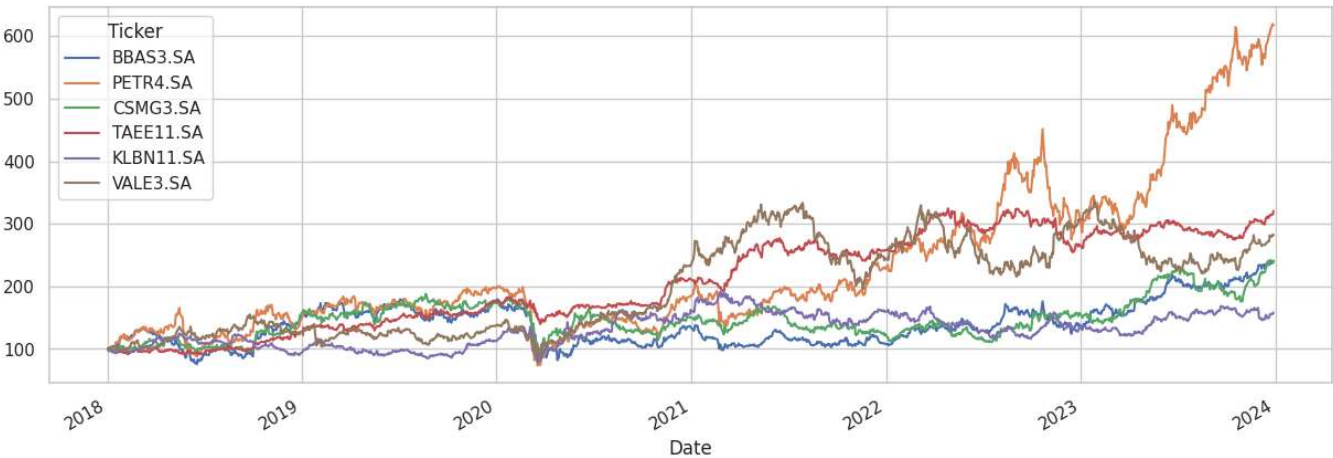


Ticker	BBAS3.SA	CSMG3.SA	KLBN11.SA	PETR4.SA	TAE11.SA	VALE3.SA
Date						
2018-01-02	100.000000	100.000000	100.000000	100.000000	100.000000	100.000000
2018-01-03	101.275424	97.628277	98.736247	100.906351	100.139765	99.400775
2018-01-04	102.247215	96.123144	98.901095	101.087604	98.555430	99.808248
2018-01-05	102.247215	96.898488	97.967017	101.691857	99.021428	101.366232
2018-01-08	102.490169	97.491436	99.725279	102.900307	98.555430	103.619363
...
2023-12-21	235.461052	240.959337	153.854229	603.164896	311.920020	281.420937
2023-12-22	236.111589	242.038597	156.027106	608.966190	314.174863	279.300310
2023-12-26	238.280153	239.917524	155.813387	618.745453	314.842972	280.287519
2023-12-27	237.933198	238.149933	156.454572	619.242683	315.344037	282.993127
2023-12-28	240.231849	241.331565	158.306960	617.253699	320.521864	282.261850

1487 rows × 6 columns

```
nova_ordem = [ 'BBAS3.SA', 'PETR4.SA', 'CSMG3.SA', 'TAE11.SA', 'KLBN11.SA', 'VALE3.SA' ]
dados = dados[nova_ordem]
```

```
dados.plot(figsize = (15,5));
```



```
dados_chg = dados.pct_change()
dados_chg = dados_chg.fillna(0)
```

```
ret_acc = (dados.iloc[-1] / dados.iloc[0]) - 1
print("Retorno acumulado:\n", ret_acc)
```

```
Retorno acumulado:
Ticker
BBAS3.SA      1.402318
PETR4.SA      5.172537
CSMG3.SA      1.413316
TAE11.SA      2.205219
KLBN11.SA     0.583070
VALE3.SA      1.822618
dtype: float64
```

```
ret_aa = ((dados.iloc[-1]/dados.iloc[0])** (1/5)) - 1
print("Retorno anualizado:\n", ret_aa)
```

```
Retorno anualizado:
Ticker
BBAS3.SA      0.191588
PETR4.SA      0.439106
CSMG3.SA      0.192677
TAE11.SA      0.262326
KLBN11.SA     0.096226
VALE3.SA      0.230638
dtype: float64
```

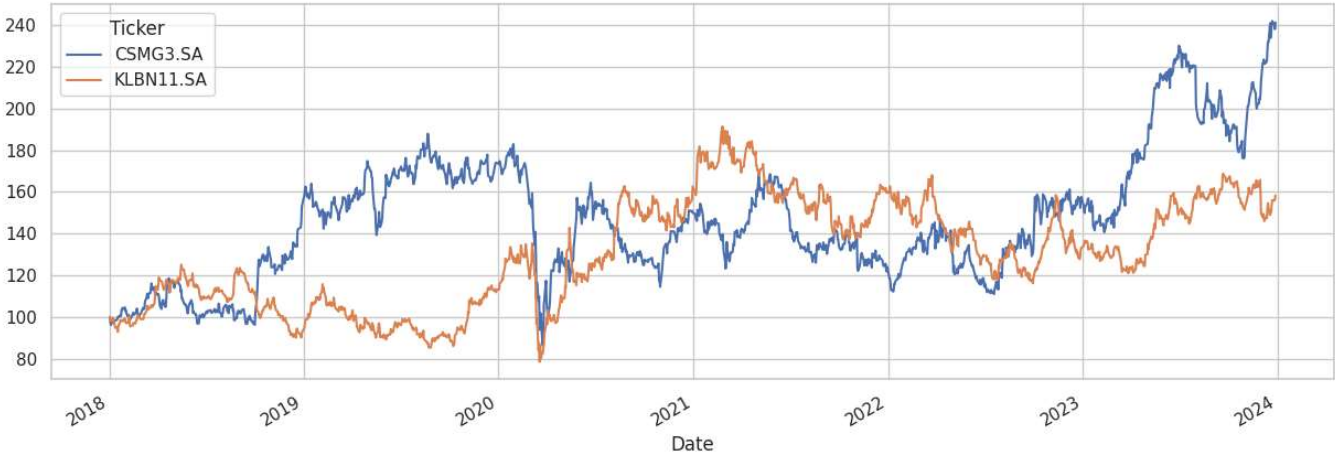
```
vol_aa = dados_chg.std() * np.sqrt(252)
print("Vol anualizada:\n", vol_aa)
```

```
Vol anualizada:
Ticker
BBAS3.SA      0.390788
PETR4.SA      0.463584
CSMG3.SA      0.365302
TAE11.SA      0.205062
KLBN11.SA     0.303409
VALE3.SA      0.390549
dtype: float64
```

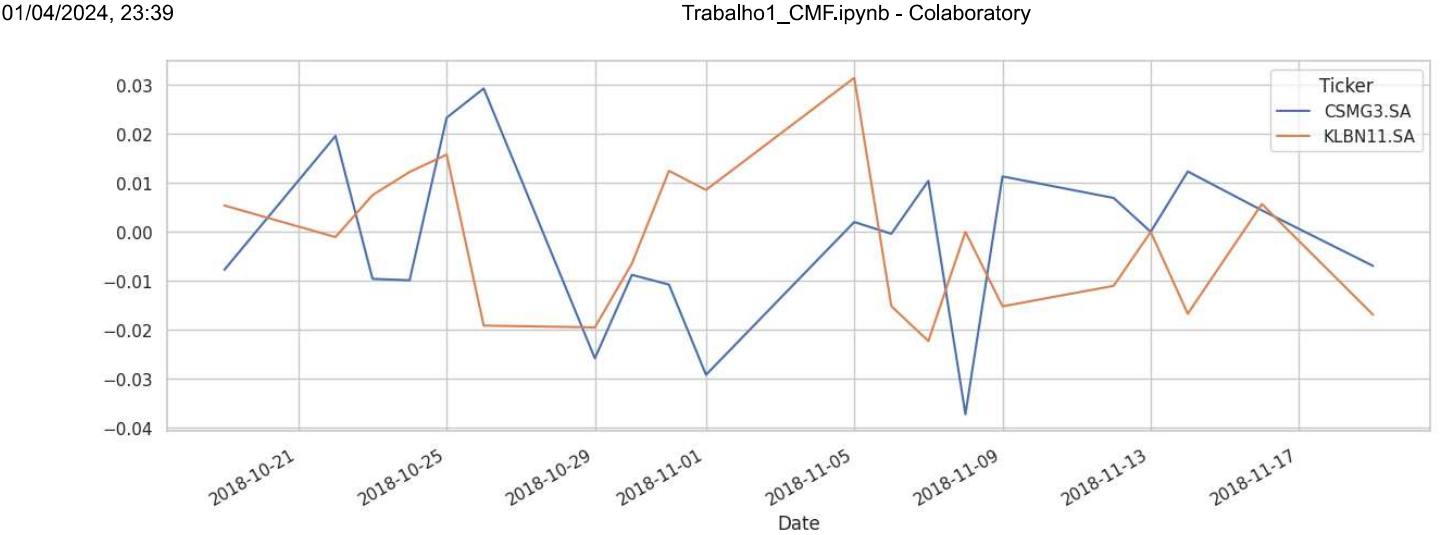
```
#Calculo da correlação dos dados
dados_chg.corr()
```

Ticker	BBAS3.SA	PETR4.SA	CSMG3.SA	TAE11.SA	KLBN11.SA	VALE3.SA
Ticker						
BBAS3.SA	1.000000	0.640989	0.484127	0.439334	0.176719	0.354287
PETR4.SA	0.640989	1.000000	0.362899	0.337913	0.239288	0.421012
CSMG3.SA	0.484127	0.362899	1.000000	0.438240	0.170870	0.213889
TAE11.SA	0.439334	0.337913	0.438240	1.000000	0.195351	0.192620
KLBN11.SA	0.176719	0.239288	0.170870	0.195351	1.000000	0.297905
VALE3.SA	0.354287	0.421012	0.213889	0.192620	0.297905	1.000000

```
dados[['CSMG3.SA', 'KLBN11.SA']].plot(figsize = (15,5));
```



```
dados_chg[['CSMG3.SA', 'KLBN11.SA']].iloc[200:220].plot(figsize = (15,5));
```



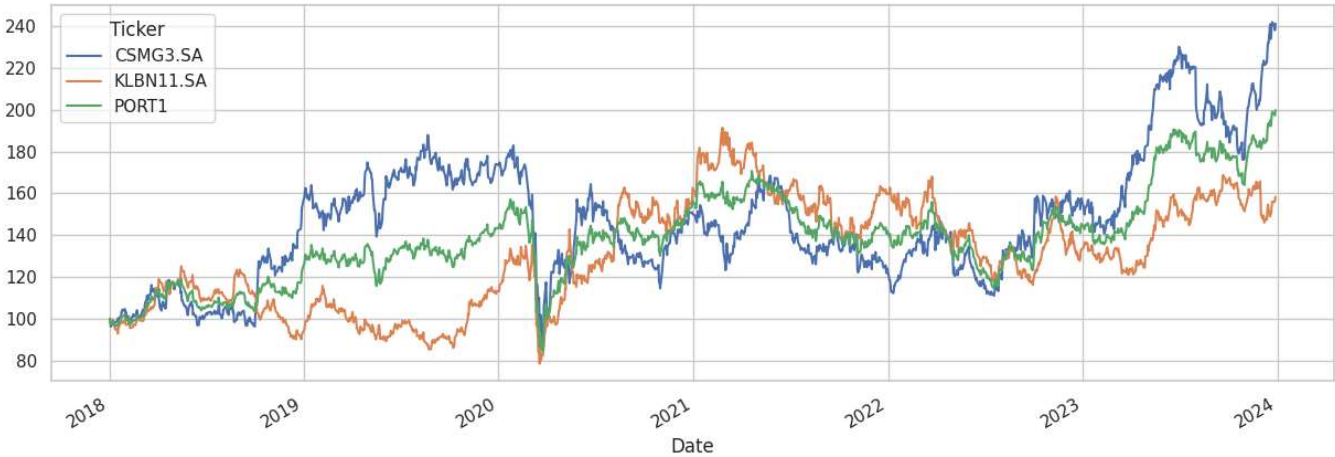
```
port_pesos = [0, 0, 0.5, 0, 0.5, 0]
dados['PORT1'] = dados.dot(port_pesos)
```

```
display(dados)
```

Ticker	BBAS3.SA	PETR4.SA	CSMG3.SA	TAEF11.SA	KLBN11.SA	VALE3.SA	PORT1
Date							
2018-01-02	100.000000	100.000000	100.000000	100.000000	100.000000	100.000000	100.000000
2018-01-03	101.275424	100.906351	97.628277	100.139765	98.736247	99.400775	98.182262
2018-01-04	102.247215	101.087604	96.123144	98.555430	98.901095	99.808248	97.512120
2018-01-05	102.247215	101.691857	96.898488	99.021428	97.967017	101.366232	97.432753
2018-01-08	102.490169	102.900307	97.491436	98.555430	99.725279	103.619363	98.608357
...
2023-12-21	235.461052	603.164896	240.959337	311.920020	153.854229	281.420937	197.406783
2023-12-22	236.111589	608.966190	242.038597	314.174863	156.027106	279.300310	199.032852
2023-12-26	238.280153	618.745453	239.917524	314.842972	155.813387	280.287519	197.865456
2023-12-27	237.933198	619.242683	238.149933	315.344037	156.454572	282.993127	197.302252
2023-12-28	240.231849	617.253699	241.331565	320.521864	158.306960	282.261850	199.819262

1487 rows × 7 columns

```
dados[['CSMG3.SA', 'KLBN11.SA', 'PORT1']].plot(figsize = (15,5));
```



```
dados_chg = dados.pct_change()
dados_chg = dados_chg.fillna(0)
```

```
ret_acc = (dados.iloc[dados.count()[0]-1] / dados.iloc[0])-1
print("Retorno acumulado:\n", ret_acc)
ret_aa = ((dados.iloc[-1]/dados.iloc[0])** (1/5))-1
print("Ret aa:\n", ret_aa)
```

```
Retorno acumulado:
Ticker
BBAS3.SA      1.402318
PETR4.SA      5.172537
CSMG3.SA      1.413316
TAE11.SA      2.205219
KLB11.SA      0.583070
VALE3.SA      1.822618
PORT1         0.998193
dtype: float64
Ret aa:
Ticker
BBAS3.SA      0.191588
PETR4.SA      0.439106
CSMG3.SA      0.192677
TAE11.SA      0.262326
KLB11.SA      0.096226
VALE3.SA      0.230638
PORT1         0.148491
dtype: float64
```

```
vol_aa = dados_chg.std()*np.sqrt(252)
print("Vol aa:\n", vol_aa)
```

```
Vol aa:
Ticker
BBAS3.SA      0.390788
PETR4.SA      0.463584
CSMG3.SA      0.365302
TAE11.SA      0.205062
KLB11.SA      0.303409
VALE3.SA      0.390549
PORT1         0.260533
dtype: float64
```

```
#Calcular drawdown
ddown = pd.DataFrame()
```

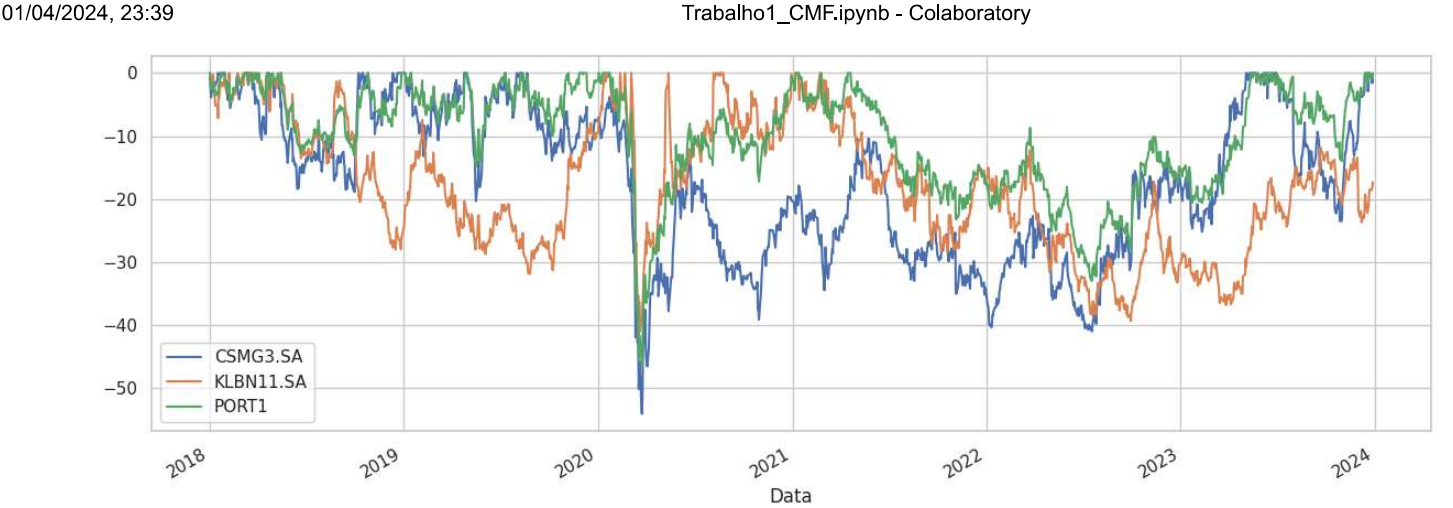
```
for ativo in dados.columns:
    list = []
    for ind in range(dados.count()[0]):
        list.append((dados[ativo].iloc[ind]/dados[ativo].iloc[:ind+1].max()-1)*100)
    ddown[ativo]=list
```

```
ddown['Data']=dados.index.values
ddown.set_index(keys = 'Data', inplace = True)
```

```
#display(ddown)
print(ddown.min())
```

```
BBAS3.SA      -58.286996
PETR4.SA      -63.356055
CSMG3.SA      -54.029209
TAE11.SA      -23.694037
KLB11.SA      -42.009959
VALE3.SA      -43.724133
PORT1         -46.258119
dtype: float64
```

```
ddown[['CSMG3.SA', 'KLB11.SA', 'PORT1']].plot(figsize = (15,5));
```



```
dados=dados.drop(['PORT1'], axis=1)
dados_chg=dados_chg.drop(['PORT1'], axis=1)
```

dados

Ticker	BBAS3.SA	PETR4.SA	CSMG3.SA	TAE11.SA	KLBN11.SA	VALE3.SA
Date						
2018-01-02	100.000000	100.000000	100.000000	100.000000	100.000000	100.000000
2018-01-03	101.275424	100.906351	97.628277	100.139765	98.736247	99.400775
2018-01-04	102.247215	101.087604	96.123144	98.555430	98.901095	99.808248
2018-01-05	102.247215	101.691857	96.898488	99.021428	97.967017	101.366232
2018-01-08	102.490169	102.900307	97.491436	98.555430	99.725279	103.619363
...
2023-12-21	235.461052	603.164896	240.959337	311.920020	153.854229	281.420937
2023-12-22	236.111589	608.966190	242.038597	314.174863	156.027106	279.300310
2023-12-26	238.280153	618.745453	239.917524	314.842972	155.813387	280.287519
2023-12-27	237.933198	619.242683	238.149933	315.344037	156.454572	282.993127
2023-12-28	240.231849	617.253699	241.331565	320.521864	158.306960	282.261850

1487 rows × 6 columns

```
def calc_ret_vol(ativos, ativos_chg, port_pesos):
    port = ativos.dot(port_pesos)
    port_chg =port.pct_change()
    port_chg = port_chg.fillna(0)
    ret = ((port.iloc[-1]/port.iloc[0]))**(1/5))-1
    vol = port_chg.std()*np.sqrt(252)
    return ret, vol
```

port_pesos

[0, 0, 0.5, 0, 0.5, 0]

dados

Ticker	BBAS3.SA	PETR4.SA	CSMG3.SA	TAE11.SA	KLBN11.SA	VALE3.SA
Date						
2018-01-02	100.000000	100.000000	100.000000	100.000000	100.000000	100.000000
2018-01-03	101.275424	100.906351	97.628277	100.139765	98.736247	99.400775
2018-01-04	102.247215	101.087604	96.123144	98.555430	98.901095	99.808248
2018-01-05	102.247215	101.691857	96.898488	99.021428	97.967017	101.366232
2018-01-08	102.490169	102.900307	97.491436	98.555430	99.725279	103.619363
...
2023-12-21	235.461052	603.164896	240.959337	311.920020	153.854229	281.420937
2023-12-22	236.111589	608.966190	242.038597	314.174863	156.027106	279.300310
2023-12-26	238.280153	618.745453	239.917524	314.842972	155.813387	280.287519
2023-12-27	237.933198	619.242683	238.149933	315.344037	156.454572	282.993127
2023-12-28	240.231849	617.253699	241.331565	320.521864	158.306960	282.261850

```
1487 rows x 6 columns

#Portfolio com 2 ativos: KLBN11 e TAE11
points = []
min_vol_ret = [100, 0] #[vol, ret]
port_pesos = [0, 0, 0, 0, 0, 0]
for w in range(0, 101, 5):
    ret, vol = calc_ret_vol(dados, dados_chg, [0, 0, w/100, 0, (1-w/100), 0])
    print(f"Aloc:{round(w/100, 2):.2f} {round(1-(w/100),2):.2f} Ret:{round(ret, 3):.3f} Vol:{round(vol, 3):.3f}")
    points.append([ret, vol])
    if vol < min_vol_ret[0]:
        min_vol_ret[0] = vol
        min_vol_ret[1] = ret
        port_pesos[2] = w/100
        port_pesos[4] = 1-w/100

    Aloc:0.00 1.00 Ret:0.096 Vol:0.303
    Aloc:0.05 0.95 Ret:0.102 Vol:0.291
    Aloc:0.10 0.90 Ret:0.107 Vol:0.280
    Aloc:0.15 0.85 Ret:0.113 Vol:0.271
    Aloc:0.20 0.80 Ret:0.118 Vol:0.264
    Aloc:0.25 0.75 Ret:0.124 Vol:0.259
    Aloc:0.30 0.70 Ret:0.129 Vol:0.256
    Aloc:0.35 0.65 Ret:0.134 Vol:0.254
    Aloc:0.40 0.60 Ret:0.139 Vol:0.254
    Aloc:0.45 0.55 Ret:0.144 Vol:0.257
    Aloc:0.50 0.50 Ret:0.148 Vol:0.261
    Aloc:0.55 0.45 Ret:0.153 Vol:0.266
    Aloc:0.60 0.40 Ret:0.158 Vol:0.273
    Aloc:0.65 0.35 Ret:0.162 Vol:0.281
    Aloc:0.70 0.30 Ret:0.167 Vol:0.290
    Aloc:0.75 0.25 Ret:0.171 Vol:0.301
    Aloc:0.80 0.20 Ret:0.176 Vol:0.312
    Aloc:0.85 0.15 Ret:0.180 Vol:0.324
    Aloc:0.90 0.10 Ret:0.184 Vol:0.337
    Aloc:0.95 0.05 Ret:0.189 Vol:0.351
    Aloc:1.00 0.00 Ret:0.193 Vol:0.365

print(min_vol_ret)
print(port_pesos)

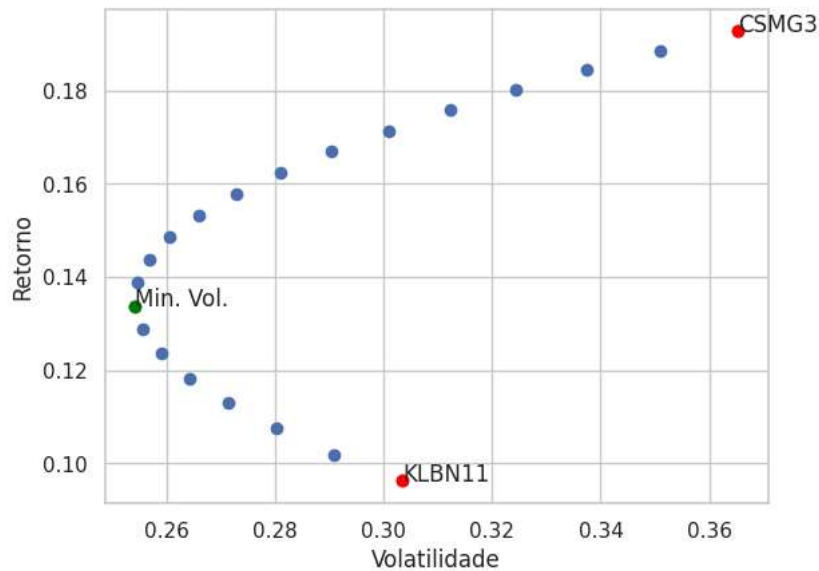
[0.25409394048001854, 0.13380393119163303]
[0, 0, 0.35, 0, 0.65, 0]
```

```
# a) GRAFICO DA FRONTEIRA EFICIENTE #
lp = np.array(points).T
plt.scatter(lp[[1][:]],lp[[0][:]]);
plt.ylabel("Retorno");
plt.xlabel("Volatilidade");

plt.scatter(vol_aa['CSMG3.SA'], ret_aa['CSMG3.SA'], color='red');
plt.text(vol_aa['CSMG3.SA'], ret_aa['CSMG3.SA'], 'CSMG3');

plt.scatter(vol_aa['KLBN11.SA'], ret_aa['KLBN11.SA'], color='red');
plt.text(vol_aa['KLBN11.SA'], ret_aa['KLBN11.SA'], 'KLBN11');

plt.scatter(min_vol_ret[0], min_vol_ret[1], color='green');
plt.text(min_vol_ret[0], min_vol_ret[1], 'Min. Vol.');
```



```
port_pesos
```

```
[0, 0, 0.35, 0, 0.65, 0]
```

```
dados['PORT1'] = dados.dot(port_pesos)
dados_chg = dados.pct_change()
dados_chg = dados_chg.fillna(0)
```

```
#          c) A RENTABILIDADE ANUIZADA DOS ATIVOS QUE COMPÕE O PORTIFÓLIO E O PORTIFOLIO_1      #
ret_aa = (((dados.iloc[-1]/dados.iloc[0])** (1/5))-1)*100
print("RENTABILIDADE ANUIZADA:\n", ret_aa.round(2))

print("\n")
```

```
#          d) A VOLATILIDADE ANUIZADA DOS ATIVOS QUE COMPÕE O PORTIFÓLIO E O PORTIFOLIO_1      #
vol_aa = (dados_chg.std()*np.sqrt(252))*100
print("VOLATILIDADE ANUIZADA:\n", vol_aa.round(2))
```

```
Ret aa:
Ticker
BBAS3.SA    0.191588
PETR4.SA    0.439106
CSMG3.SA    0.192677
TAE11.SA    0.262326
KLB11.SA    0.096226
VALE3.SA    0.230638
PORT1       0.133804
dtype: float64
Vol aa:
Ticker
BBAS3.SA    0.390788
PETR4.SA    0.463584
CSMG3.SA    0.365302
TAE11.SA    0.205062
KLB11.SA    0.303409
VALE3.SA    0.390549
PORT1       0.254094
dtype: float64
```

```
#Calcular drawdown
ddown = pd.DataFrame()
```

```
for ativo in dados.columns:
    list = []
    for ind in range(dados.count()[0]):
        list.append((dados[ativo].iloc[ind]/dados[ativo].iloc[ind+1].max()-1)*100)
    ddown[ativo]=list
```

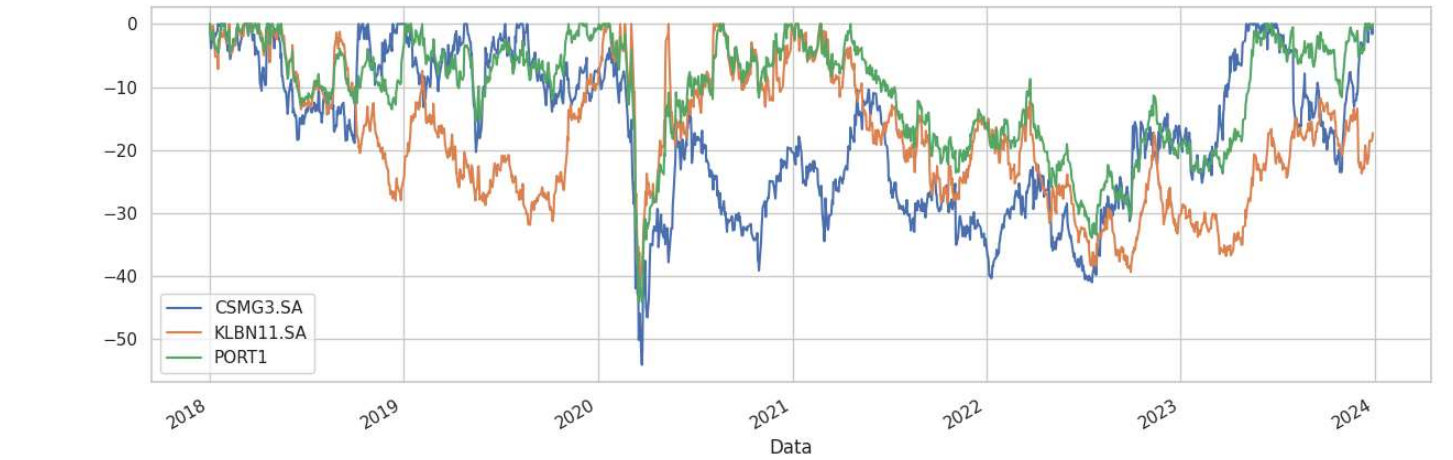
```
ddown['Data']=dados.index.values
ddown.set_index(keys = 'Data', inplace = True)
```

```
#display(ddown)
print(ddown.min())
```

```
BBAS3.SA    -58.286996
PETR4.SA    -63.356055
CSMG3.SA    -54.029209
```

```
TAE11.SA -23.694037
KLB11.SA -42.009959
VALE3.SA -43.724133
PORT1 -44.136837
dtype: float64
```

```
# b) CRIANDO O GRÁFICO DE DRAWDOWN #
ddown[['CSMG3.SA', 'KLB11.SA', 'PORT1']].plot(figsize = (15,5));
```



```
dados=dados.drop(['PORT1'], axis=1)
dados_chg=dados_chg.drop(['PORT1'], axis=1)
```

dados

Ticker	BBAS3.SA	PETR4.SA	CSMG3.SA	TAE11.SA	KLB11.SA	VALE3.SA
Date						
2018-01-02	100.000000	100.000000	100.000000	100.000000	100.000000	100.000000
2018-01-03	101.275424	100.906351	97.628277	100.139765	98.736247	99.400775
2018-01-04	102.247215	101.087604	96.123144	98.555430	98.901095	99.808248
2018-01-05	102.247215	101.691857	96.898488	99.021428	97.967017	101.366232
2018-01-08	102.490169	102.900307	97.491436	98.555430	99.725279	103.619363
...
2023-12-21	235.461052	603.164896	240.959337	311.920020	153.854229	281.420937
2023-12-22	236.111589	608.966190	242.038597	314.174863	156.027106	279.300310
2023-12-26	238.280153	618.745453	239.917524	314.842972	155.813387	280.287519
2023-12-27	237.933198	619.242683	238.149933	315.344037	156.454572	282.993127
2023-12-28	240.231849	617.253699	241.331565	320.521864	158.306960	282.261850

1487 rows × 6 columns

```
#Portfolio com 3 ativos: CSMG3, KLB11 e VALE3
points = []
min_vol_ret = [100, 0]
port_pesos = [0, 0, 0, 0, 0, 0]
for w1 in range(0, 101, 5):
    for w2 in range(0, 101-w1, 5):
        ret, vol = calc_ret_vol(dados, dados_chg, [0, 0, w1/100, 0, w2/100, (1-w1/100-w2/100)])
        #print("Aloc:", round(w1/100, 2), round(w2/100, 2), round(1-w1/100-w2/100, 2), "Ret:", round(ret, 3), "Vol:", round(vol, 3))
        print(f"Aloc:{round(w1/100, 2):.2f} {round(w2/100, 2):.2f} {round(1-w1/100-w2/100, 2):.2f} Ret:{round(ret, 3):.3f} Vol:{round(vol, 3):.3f}")
        points.append([ret, vol])
        if vol < min_vol_ret[0]:
            min_vol_ret[0] = vol
            min_vol_ret[1] = ret
            port_pesos[2] = w1/100
            port_pesos[4] = w2/100
            port_pesos[5] = 1-w1/100-w2/100

print(min_vol_ret)
print(port_pesos)
```



```
[0.2406876025071771, 0.1507672473324957]
[0, 0, 0.3, 0, 0.55, 0.14999999999999999]
```

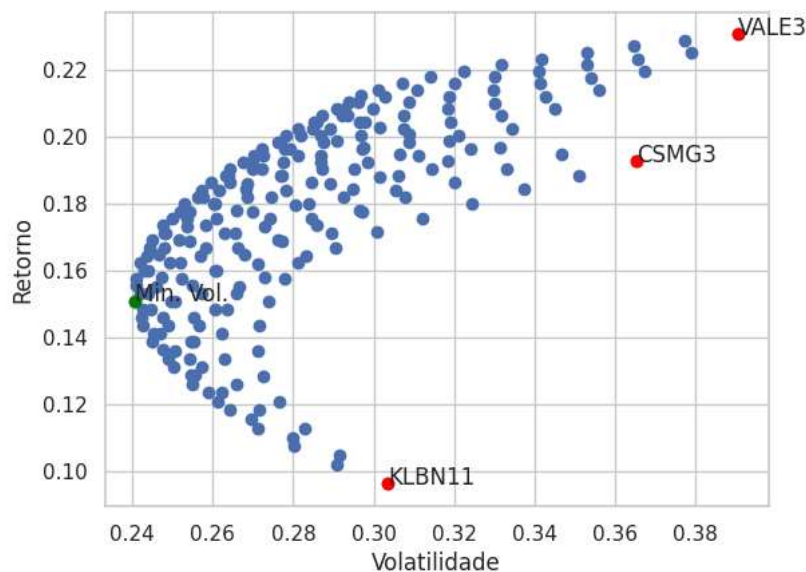
```
# a) GRAFICO DA FRONTEIRA EFICIENTE #
lp = np.array(points).T
plt.scatter(lp[[1][:]],lp[[0][:]]);
plt.ylabel("Retorno");
plt.xlabel("Volatilidade");

plt.scatter(vol_aa['CSMG3.SA'], ret_aa['CSMG3.SA'], color='red');
plt.text(vol_aa['CSMG3.SA'], ret_aa['CSMG3.SA'], 'CSMG3');

plt.scatter(vol_aa['KLB11.SA'], ret_aa['KLB11.SA'], color='red');
plt.text(vol_aa['KLB11.SA'], ret_aa['KLB11.SA'], 'KLB11');

plt.scatter(vol_aa['VALE3.SA'], ret_aa['VALE3.SA'], color='red');
plt.text(vol_aa['VALE3.SA'], ret_aa['VALE3.SA'], 'VALE3');

plt.scatter(min_vol_ret[0], min_vol_ret[1], color='green');
plt.text(min_vol_ret[0], min_vol_ret[1], 'Min. Vol.');
```



```
dados['PORT1'] = dados.dot(port_pesos)
dados_chg = (dados - dados.shift(1)) / dados.shift(1)
dados_chg = dados_chg.fillna(0)
```

```
# c) A RENTABILIDADE ANUIZADA DOS ATIVOS QUE COMPÕE O PORTIFÓLIO E O PORTIFOLIO_1 #
ret_aa = (((dados.iloc[-1]/dados.iloc[0])** (1/5))-1)*100
print("RENTABILIDADE ANUIZADA:\n", ret_aa.round(2))

print("\n")
```

```
# d) A VOLATILIDADE ANUIZADA DOS ATIVOS QUE COMPÕE O PORTIFÓLIO E O PORTIFOLIO_1 #
vol_aa = (dados_chg.std()*np.sqrt(252))*100
print("VOLATILIDADE ANUIZADA:\n", vol_aa.round(2))
```

RENTABILIDADE ANUIZADA:

Ticker	
BBAS3.SA	19.16
PETR4.SA	43.91
CSMG3.SA	19.27
TAE11.SA	26.23
KLB11.SA	9.62
VALE3.SA	23.06
PORT1	15.08

dtype: float64

VOLATILIDADE ANUIZADA:

Ticker	
BBAS3.SA	39.08
PETR4.SA	46.36
CSMG3.SA	36.53
TAE11.SA	20.51
KLB11.SA	30.34
VALE3.SA	39.05
PORT1	24.07

dtype: float64

```
#Calcular drawdown (valor de queda de um ativo em comparação ao valor máximo de cotação anterior)
ddown = pd.DataFrame()
```

```
for ativo in dados.columns:
    list = []
    for ind in range(dados.count()[0]):
        list.append((dados[ativo].iloc[ind]/dados[ativo].iloc[:ind+1].max()-1)*100)
    ddown[ativo]=list
```

```
ddown['Data']=dados.index.values
ddown.set_index(keys = 'Data', inplace = True)
```

```
#display(ddown)
print(ddown.min())
```

```
BBAS3.SA      -58.286996
PETR4.SA      -63.356055
CSMG3.SA      -54.029209
TAEF11.SA     -23.694037
KLBN11.SA     -42.009959
VALE3.SA      -43.724133
PORT1         -42.788396
dtype: float64
```

```
#                                     b) CRIANDO O GRÁFICO DE DRAWDOWN                                     #
ddown[['CSMG3.SA', 'KLBN11.SA', 'VALE3.SA', 'PORT1']].plot(figsize = (15,5));
```

