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Assignment 9

Algorithms & Data Structures

Problem 9.1

a) Here, $m = 5$

$$h_1(k) = k \bmod 5$$

$$h_2(k) = 7k \bmod 8$$

\Rightarrow Hashing $k = 3$

Applying h_1 on $k = 3$

From h_1 , we have $\text{index} = 3 \bmod 5 = 3$

Index 3 is available, so current index = 3.

index 0	1	2	3	4
			3	

 No collision

Hashing $k = 10$

Applying h_1 on $k = 10$

From h_1 , we have $\text{index} = 0$

Index 0 is available, so, we don't need to look for h_2 .

10		3		
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 No collision

Hashing $k = 2$

Applying h_1 on $k = 2$

From h_1 , we have $\text{index} = 2$

Index 2 is available, so index = 2.

No collision.

10		2	3
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10	2	3	3
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Hashing $h = 4$

Applying h_1 on $h = 4$,

index = 4

Index 4 is available,

no collision occurred.

Final
Array sequence:

10		2	3	4
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b) Hashtable.cpp

Problem 9.2

a) This can be proved with the help of a counter example.

Let's say our start-finish intervals in this manner: $[(2, 4), (3, 5), (4, 11)]$. If we take the activity with the shortest duration, we pick $(3, 5)$. Then, we can't choose any

other activity as they overlap with it. So, our resulting activity is only the 2nd activity $(3, 5)$.

This is not a globally optimal solution as for this problem, we could have done activity 1 and 3 $[(2, 4), (4, 11)]$, which is a globally optimal solution. Since, we know that this greedy choice doesn't always give the globally optimal solution, the statement is proved.

b) // Note: using[] contains selected activities in reverse order (at last)

=> 1. for $i \leftarrow 1$ to n

2. $A[i][1] \leftarrow i$

3. $A[i][2] \leftarrow$ starting time

4. $A[i][3] \leftarrow$ ending time

5. $\{$

6. Sort A according to finish time

7. latest_start $\leftarrow A[i][2]$

8. last_activity $\leftarrow A[i][1]$

9. for $i \leftarrow 1$ to n

10. $\{$ if $A[i][2] > \text{latest_start}$

11. $\{$ latest_start $\leftarrow A[i][2]$

12. last_activity $\leftarrow A[i][1]$

13. last_finish $\leftarrow A[i][3]$

14. $\{ \{$ // get activity with latest starting time

15. $j \leftarrow n; k \leftarrow 2$ last_activity

16. using $[1] \leftarrow \text{latest_start}$ // first selected activity

17. $s_j \leftarrow \text{latest_start}$

18. for $i \leftarrow n$ to 1 // start looking from back

19. $\{$ if $(A[i][1] \neq \text{last_activity})$ // avoid repeating

20. $\{$ $f_i \leftarrow A[i][3]$

21. if $(f_i \leq s_j)$ // if previous final time is less

22. $\{$ using $[k] \leftarrow A[i][1]$ // activity selected

23. $j \leftarrow i, k \leftarrow k + 1$ // change index

24. $s_j \leftarrow A[j][2]$ // update start check

25. $\{ \{$

26. $\{$

Demo: (A) Activity no / start time / End Time

Activity no	start time	End Time
1	2	3
2		
3		
4		

Array using Index Activity no

1			
2			
3			
4			

using Quick Sort // sort
// using algorithm
// lesser than $O(n \log n)$