

```
In [1]: import numpy as np
from matplotlib import pyplot as plt
from scipy import signal as sgn
```

Make two equal noise signals with $\tau = 10$ samples apart

```
In [59]: N = 1000
x = 0.5 - np.random.rand(N)

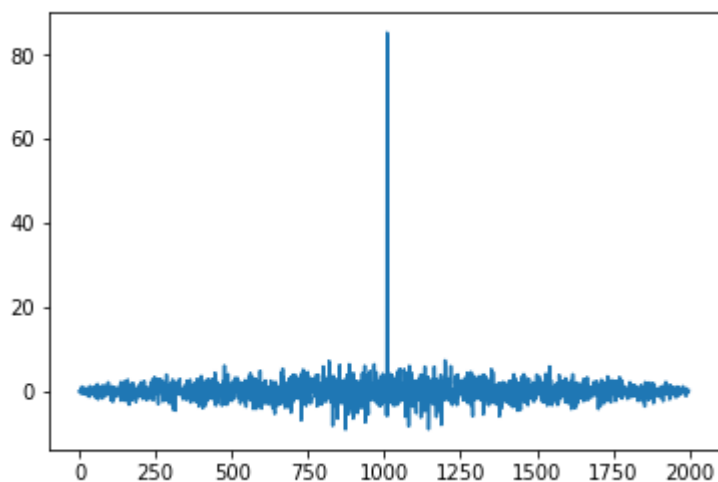
tau = 10

y = np.roll(x, -tau)
```

Correlate and plot the correlation:

```
In [3]: corr = sgn.correlate(x,y)

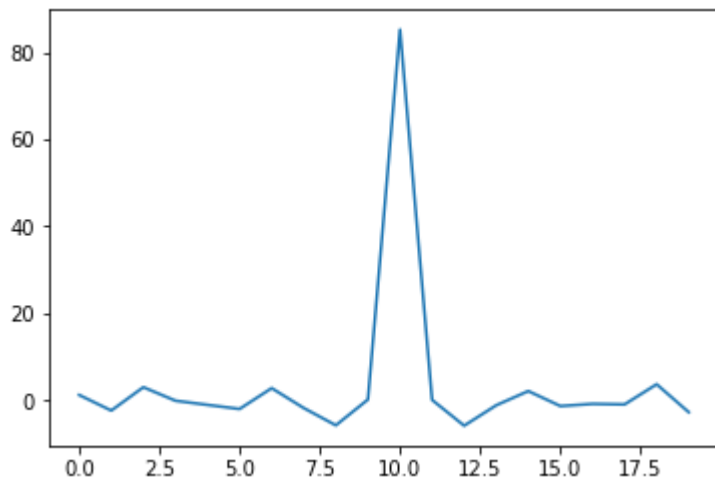
plt.plot(corr)
plt.show()
```



Lets zoom in on the first 20 samples

```
In [4]: zoom = corr[len(corr)//2:len(corr)//2 + 20]
```

```
plt.plot(zoom)  
plt.show()
```



Lets find the maximum of the absolute value of the correlation

```
In [5]: def findDelay(corr):  
  
    abs_corr = np.abs(corr)  
  
    max_value = np.amax(abs_corr)  
  
    index = np.where(corr == max_value)  
  
    delay = (index[0] - len(corr)//2)[0]  
  
    return delay  
  
print("The delay is, in samples: ", findDelay(corr))
```

The delay is, in samples: 10

To get effective delay in seconds, we have $nT = t$, and $T = 1/F_s$. If we for example 44800Hz sampling frequency we get

```
In [6]: T = 1 / 44800  
n = findDelay(corr)  
t = n*T  
print("Delay in seconds", t)
```

Delay in seconds 0.000223214285714

```

In [231]: def t (n21,n31,n32):
            y = sqrt3*(n21 + n31)
            x = (n21 - n31 - 2*n32)
            return atan2(y,x)

nmax = 2
def findmaxangles(nmax):
    nplt = np.zeros(10000)
    i = 0
    for n1 in range(-nmax,nmax + 1):
        for n2 in range(-nmax,nmax + 1):
            for n3 in range(-nmax,nmax + 1):

                nplt[i] = t(n1,n2,n3)
                i = i+ 1
    nplt = np.unique(nplt)
    print(len(nplt)," different angles with ", nmax, " maximum delay")
    print("Which gives ", 360/len(nplt), " degree angular resolution")
findmaxangles(2)
findmaxangles(4)
findmaxangles(6)

```

```

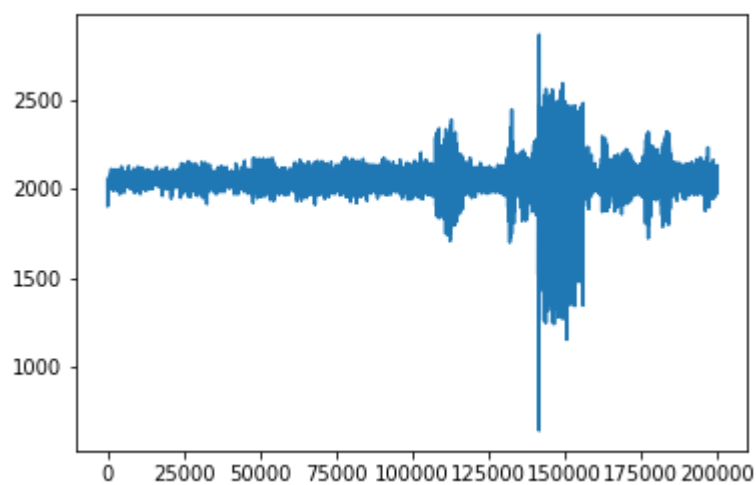
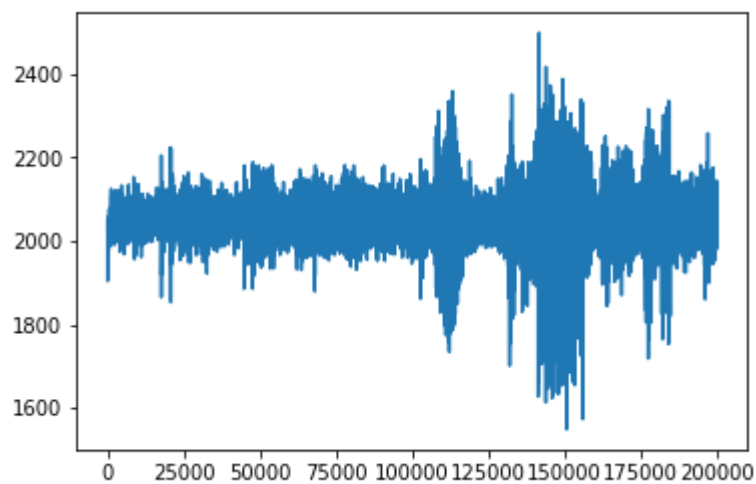
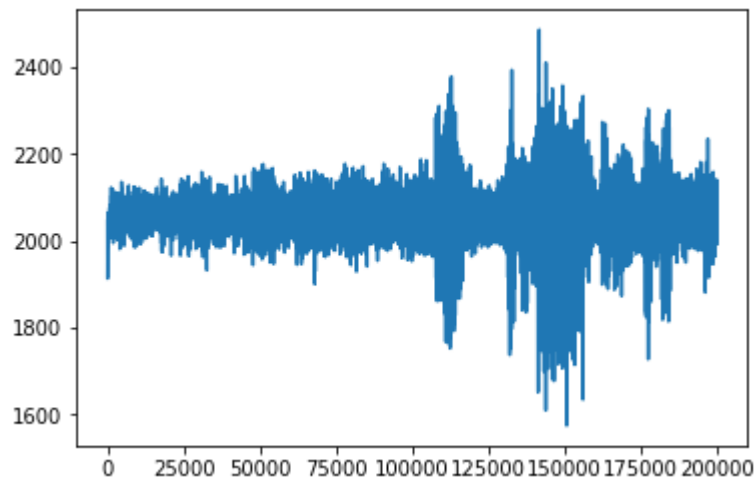
36 different angles with 2 maximum delay
Which gives 10.0 degree angular resolution
136 different angles with 4 maximum delay
Which gives 2.6470588235294117 degree angular resolution
284 different angles with 6 maximum delay
Which gives 1.267605633802817 degree angular resolution

```

```
In [7]: from raspi_import import raspi_import

sample_period, data4 = raspi_import("./out/adcdData_mic1.bin")

plt.plot(data4[1:,0])
plt.show()
plt.plot(data4[1:,1])
plt.show()
plt.plot(data4[1:,2])
plt.show()
```



Fjerne DC-komponent: Normaliserer signalet og fjerner DC-komponent

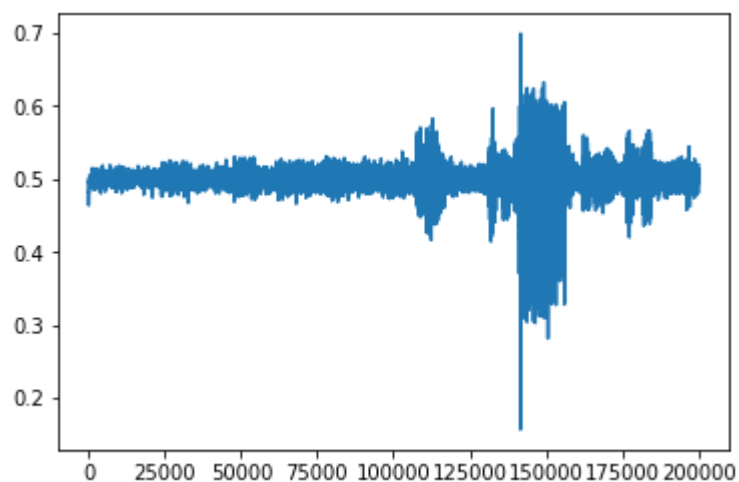
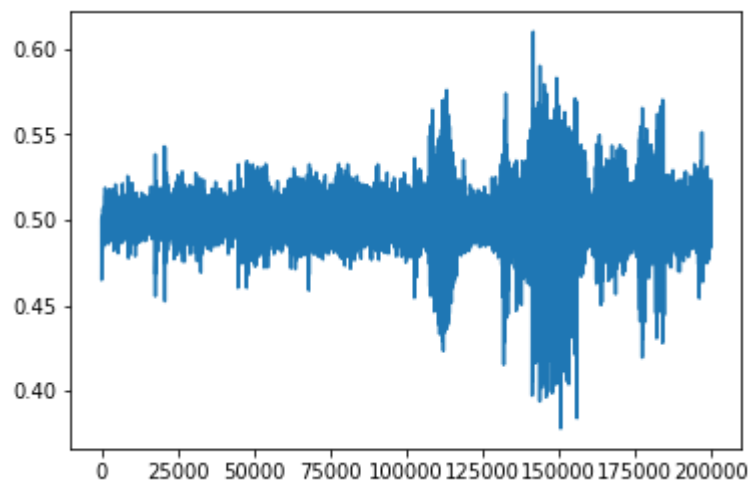
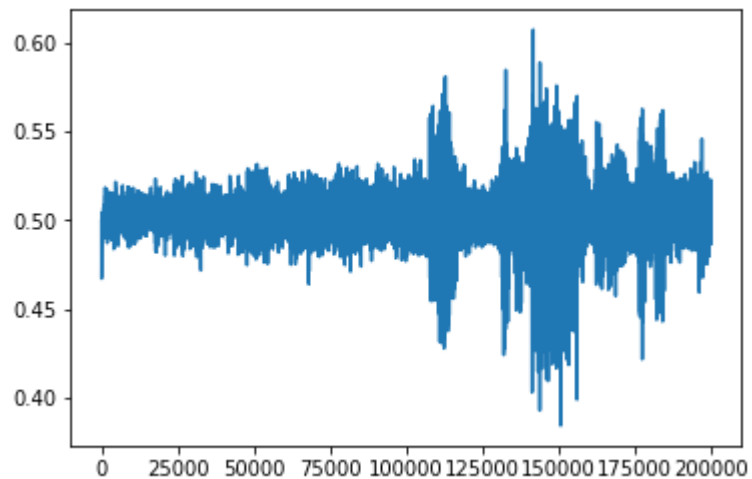
```
In [8]: def prepros (data, maximum = 4096):  
        d = data / maximum  
        d - 0.5  
        return d  
  
res = 4096
```

```
In [9]: x1 = prepros(data4[1:,0], res)
x2 = prepros(data4[1:,1], res)
x3 = prepros(data4[1:,2], res)

plt.plot(x1)
plt.show()
plt.plot(x2)
plt.show()
plt.plot(x3)
plt.show()

def resample(data, factor):
    return sgn.resample(data, len(data)*factor)

factor = 2
```



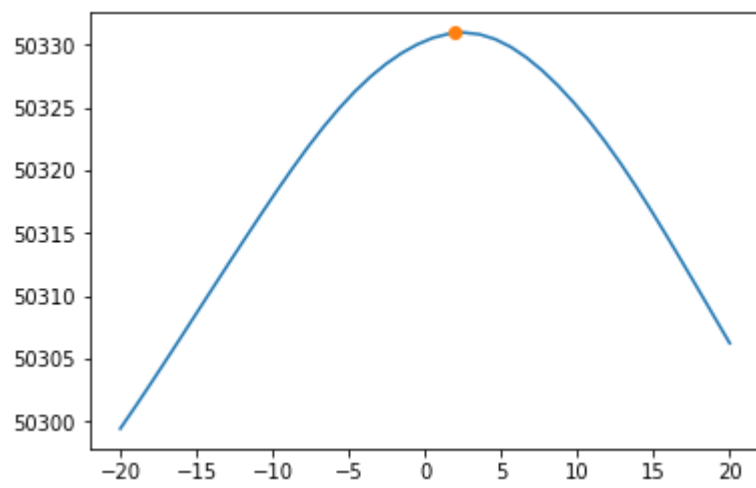
```
In [208]: def windowedcorr(x,y, maxlag):
            rxy = np.zeros(2*maxlag)
            for l in range(0, 2*maxlag):
                rxy[l] = np.sum(np.roll(x, maxlag - l)*y)

            return rxy
lag = 20
wcorr= windowedcorr(x1,x3, lag)
#plt.plot(np.linspace(-L, L, lag*2), wcorr)
plt.plot(np.linspace(-lag,lag,lag*2) ,wcorr)
plt.plot(findDelay(wcorr),wcorr[lag + findDelay(wcorr)], marker="o")
plt.show()

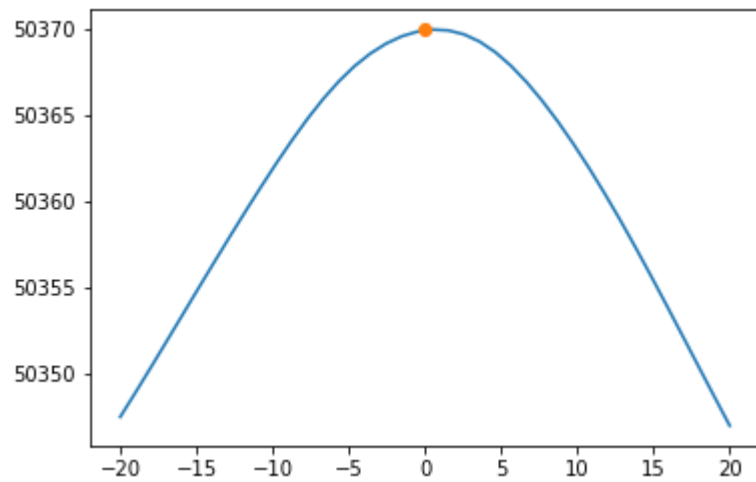
print(findDelay(wcorr))
wcorr= windowedcorr(x2,x1, lag)
#plt.plot(np.linspace(-L, L, lag*2), wcorr)
plt.plot(np.linspace(-lag,lag,lag*2) ,wcorr)
plt.plot(findDelay(wcorr),wcorr[lag + findDelay(wcorr)], marker="o")
plt.show()

print(findDelay(wcorr))
wcorr= windowedcorr(x3,x2, lag)
#plt.plot(np.linspace(-L, L, lag*2), wcorr)
plt.plot(np.linspace(-lag,lag,lag*2) ,wcorr)
plt.plot(findDelay(wcorr),wcorr[lag + findDelay(wcorr)], marker="o")
plt.show()

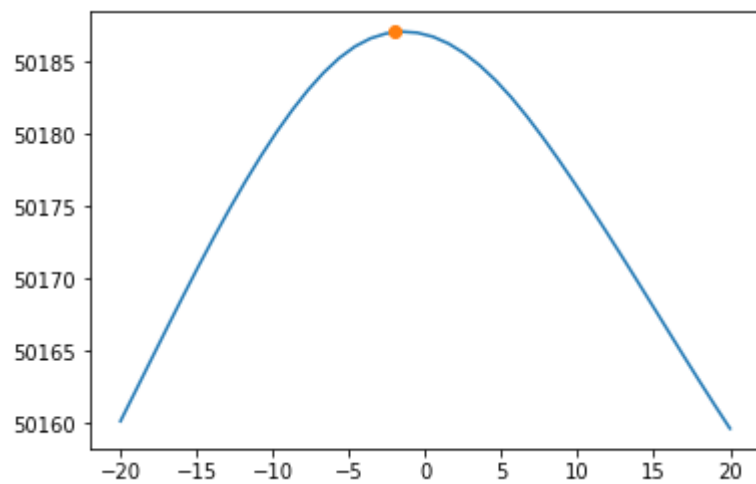
print(findDelay(wcorr))
```



2



0



-2

```
In [194]: maxlag = 10
n21 = findDelay(windowedcorr(x2,x1, maxlag))
n31 = findDelay(windowedcorr(x3,x1, maxlag))
n32 = findDelay(windowedcorr(x3,x2, maxlag))

print("Delays in samples: n21: ",n21," n31: ", n31, " n32: ", n32 )
```

Delays in samples: n21: 0 n31: -2 n32: -2

In [152]: **from math import atan2**

```
sqrt3 = 1.73205081
```

```
def est_theta (n21,n31,n32):
```

```
    p = 0
```

```
    y = sqrt3*(n21 + n31)
```

```
    x = (n21 - n31 - 2*n32)
```

```
    return atan2(y,x)
```

```
theta = est_theta(n21,n31,n32)
```

```
print(theta)
```

```
print((theta*180) / (np.pi))
```

```
-0.5235987762060795
```

```
-30.00000003482327
```

In [188]: **def** estimate_angle (data, res=4096):

```
    x1 = prepros(data[1:,0], res)
```

```
    x2 = prepros(data[1:,2], res)
```

```
    x3 = prepros(data[1:,1], res)
```

```
    c21 = windowedcorr(x2,x1, maxlag)
```

```
    c31 = windowedcorr(x3,x1, maxlag)
```

```
    c32 = windowedcorr(x3,x2, maxlag)
```

```
    #plt.plot(c21)
```

```
    #plt.plot(c31)
```

```
    #plt.plot(c32)
```

```
    #plt.show()
```

```
    n21 = findDelay(c21)
```

```
    #print(n21)
```

```
    n31 = findDelay(c31)
```

```
    #print(n31)
```

```
    n32 = findDelay(c32)
```

```
    #print(n32)
```

```
    theta = est_theta(n21,n31,n32)
```

```
    #print(theta)
```

```
    #print((theta*180) / (np.pi))
```

```
    if(theta < 0):
```

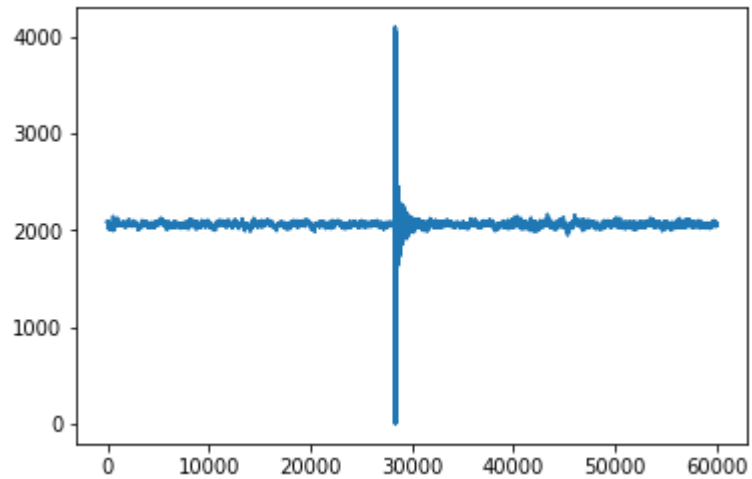
```
        theta = theta + 2*np.pi
```

```
    return theta
```

```
sample_period, data = raspi_import("./out/adcData_mic_180.bin")
```

```
theta = estimate_angle(data)
```

```
In [163]: sample_period, temp_data = raspi_import("./out/adcdData_mic_315.bin")  
plt.plot(temp_data[1:,0])  
plt.show()  
plt.show()
```



```
In [154]: estimate_angle(temp_data)
```

```
-3  
-6  
-3  
-1.0471975518043783  
-60.000000034823266
```

```
Out[154]: -1.0471975518043783
```

```

In [191]: sample_period, d0 = raspi_import("./out/adcData_mic_0.bin")
sample_period, d45 = raspi_import("./out/adcData_mic_45.bin")
sample_period, d90 = raspi_import("./out/adcData_mic_90.bin")
sample_period, d120 = raspi_import("./out/adcData_mic_120.bin")
sample_period, d145 = raspi_import("./out/adcData_mic_145.bin")
sample_period, d180 = raspi_import("./out/adcData_mic_180.bin")
sample_period, d235 = raspi_import("./out/adcData_mic_235.bin")
sample_period, d245 = raspi_import("./out/adcData_mic_245.bin")
sample_period, d270 = raspi_import("./out/adcData_mic_270.bin")
sample_period, d315 = raspi_import("./out/adcData_mic_315.bin")

arr = np.array([(d0,0),(d45,45),(d90,90),(d120,120),(d145,145),(d180,180),(d235,235),(d245,245),(d270,270),(d315,315)])
result = [(0,0,0)]*(len(arr) + 1)
result[0] = ("Estimated angle", "Actual angle", "Deviation")
for i in range(len(arr)):
    est = round((estimate_angle(arr[i][0])*180) / (np.pi),2)
    actual = arr[i][1]
    result[i + 1] = (est,actual,round(actual - est,2) )

from IPython.display import HTML, display

display(HTML(
    '<table><tr>{</tr></table>'.format(
        '</tr><tr>'.join(
            '<td>{</td>'.format('</td><td>'.join(str(_) for _ in row)) for row in res
ult)
        )
    ))

```

Estimated angle	Actual angle	Deviation
6.59	0	-6.59
40.89	45	4.11
90.0	90	0.0
120.0	120	0.0
150.0	145	-5.0
186.59	180	-6.59
229.11	235	5.89
240.0	245	5.0
273.67	270	-3.67
300.0	315	15.0