

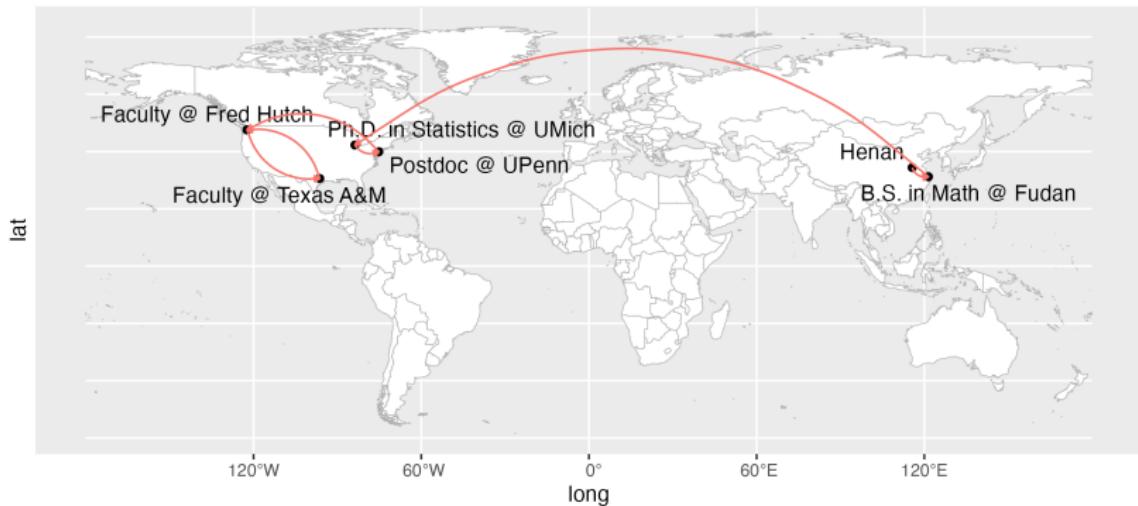
Statistical Modeling for Enhanced Microbiome Biomarker Discovery

24 April 2024

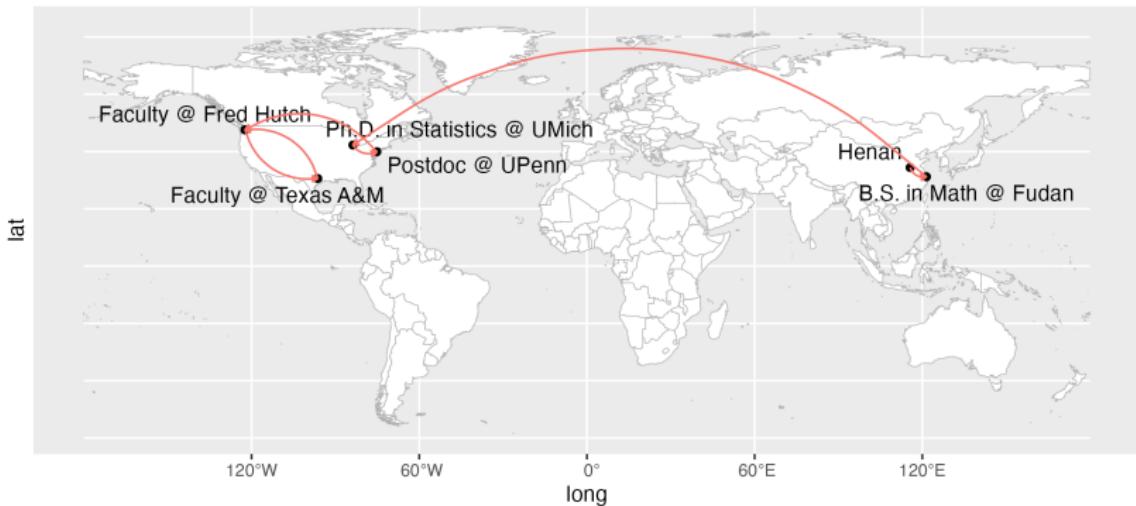
Jing Ma

Associate Professor of Biostatistics
Division of Public Health Sciences

My Journey



My Journey



You can read more about my story [here](#).

My Journey

- My thesis: graphical models, high-dimensional data analysis
- My postdoctoral training: graphical models for microbiome data, high-dimensional data analysis
- Now: statistics in microbiome, neuroscience, and aging

My Job

Fred Hutch is an independent, nonprofit organization, that also serves as UW Medicine's cancer program.

Research Institutes

- Independent research
- Collaborative research
- Mentoring students

Universities

- Independent research
- Collaborative research
- Mentoring students
- Teaching

What We Do

We develop statistical methods to study the human microbiome.

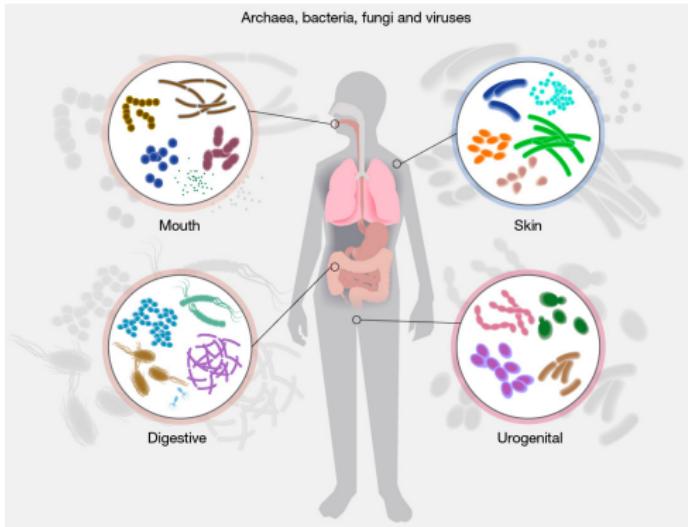
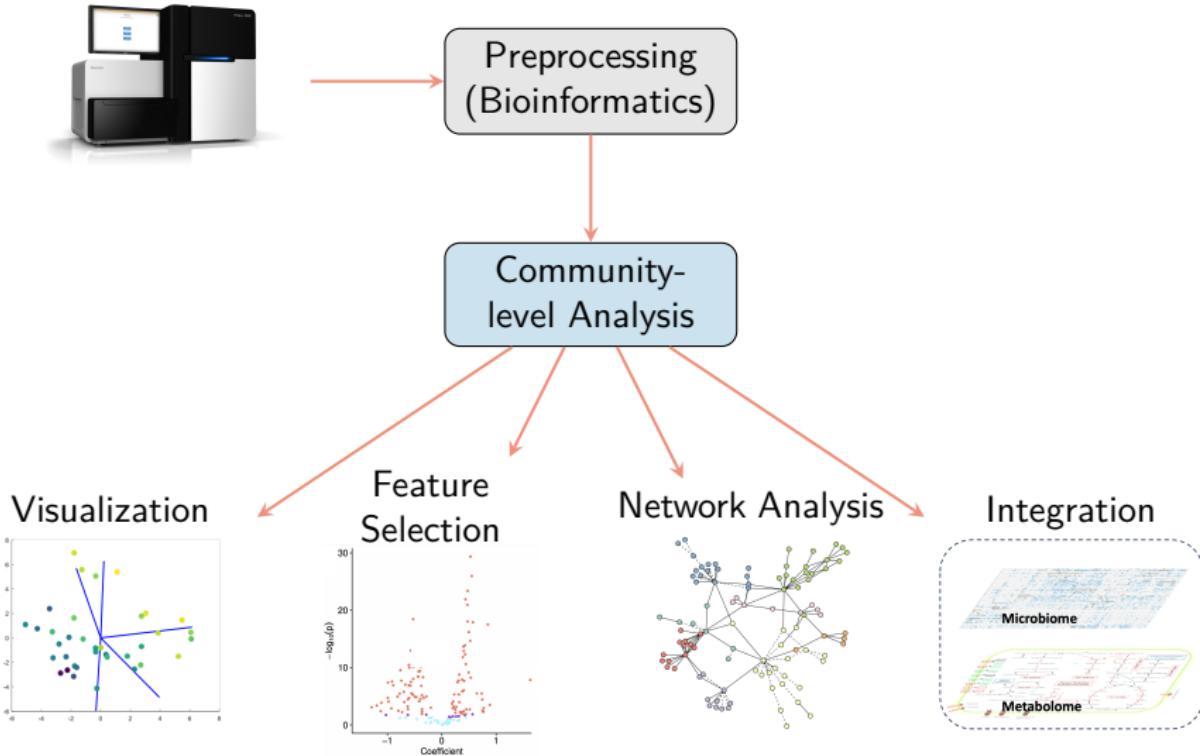


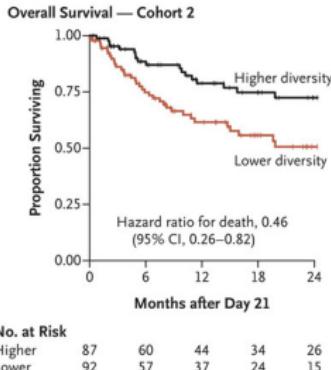
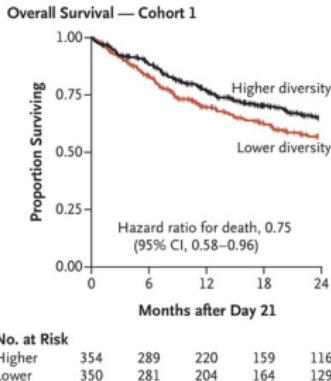
Figure 1: Composition of the human microbiome varies by body sites. They play important roles in human health and have been associated with many diseases. Most of the microbes are bacteria and live in human gut.

What We Do



Microbiome and Cancer Treatment

- Allogeneic Hematopoietic-Cell Transplantation (allo-HCT) is a curative therapy for hematologic cancers, but complications such as graft-versus-host disease (GVHD) remain a major cause of illness and death.
- Lower diversity predicts poor overall survival¹.



- Interventions to restore integrity to the intestinal microbiota?

¹Peled et al., NEJM. 20'

Scientific Question



Which bacterial species are associated with poor outcome (e.g., GVHD status)?

Microbiome Data

	Sample1	Sample2	Sample3
ASV1	17	0	335
ASV2	231	1180	45
ASV3	30	0	0
...
Age	25	48	65
Disease	yes	no	yes

Table 1: A typical microbiome contingency table

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Univariate Feature Selection

Perform univariate test of each species with respect to an outcome

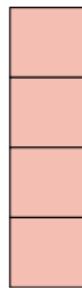
Outcome

Bacteria

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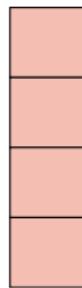
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Light Red					
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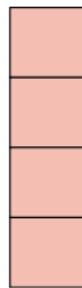


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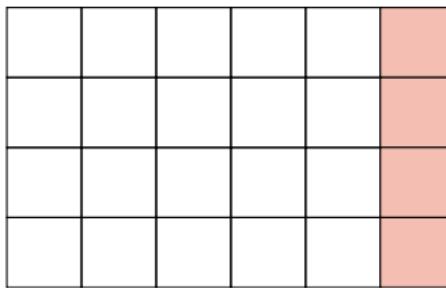
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Output:

- p -value for testing each bacterial species (after correcting for multiple comparisons)

²Paulson et al. Nat Meth. 13'

³Martin et al. AoAS. 20'

⁴Ling et al. Microbiome. 21'

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Output:

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Options

- different normalization methods
- different noise models for bacterial abundances (e.g., zero-inflated log normal², beta-binomial³, zero-inflated quantile regression⁴, etc.)

²Paulson et al. Nat Meth. 13'

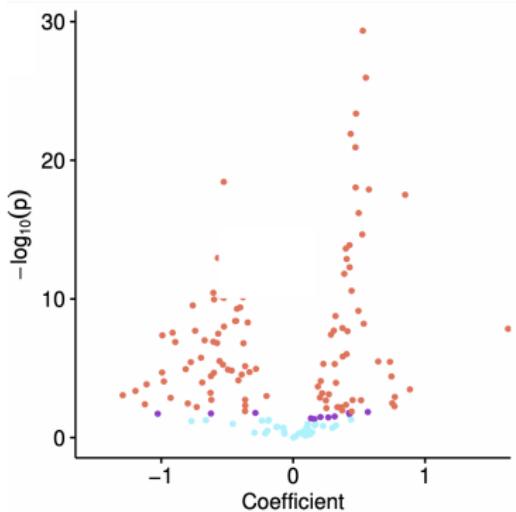
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Application to Yatsunenko 12'

Which bacteria are associated with age?

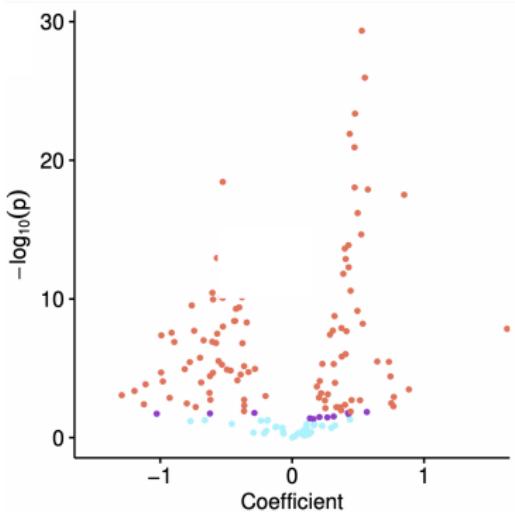
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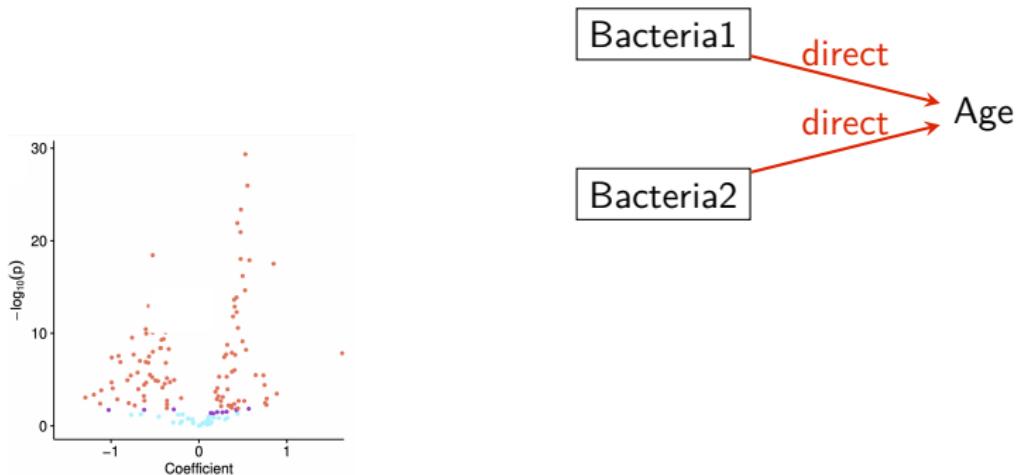
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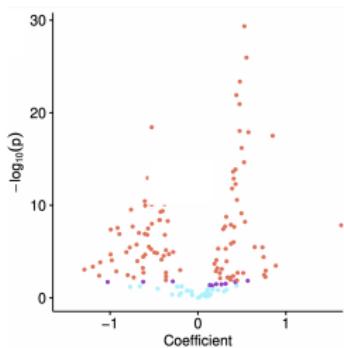
Which bacteria should I target?

Two Possible Explanations

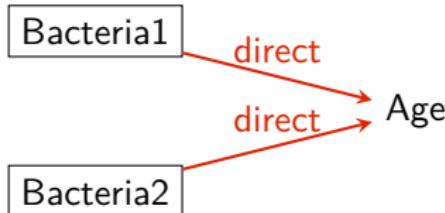
- ① Many bacteria are *directly* associated with age



Two Possible Explanations



- ① Many bacteria are *directly* associated with age



- ② Bacteria are correlated and only a few bacteria are *directly* associated with age



Conditional Associations



Figure 2: Conditional on Bacteria 2, Bacteria 1 is independent of Age.

Multiple linear regression

$$y_i = X_{i,1}\beta_1 + \dots + X_{i,p}\beta_p + \text{error}_i,$$

- Coefficients β_j : conditional association between bacteria j and y
- When $p \ll n$, inference for β is straightforward by large sample theory.

Curse of Dimensionality

$$y \approx X \cdot \beta$$

A diagram illustrating the curse of dimensionality. On the left, there is a vertical vector y represented by four empty boxes stacked vertically. In the center, there is a matrix X represented by a 4x6 grid of empty boxes. On the right, there is a vertical vector β represented by six empty boxes stacked vertically, with each box containing a question mark '?'.

If the number of unknown parameters exceeds the sample size, we have **identifiability issue!**

Curse of Dimensionality

$$y \approx X \cdot \beta$$

The diagram illustrates a linear regression problem. On the left, there is a vertical vector y represented by four empty boxes. In the center, there is a matrix X represented by a 4x6 grid of empty boxes. On the right, there is a vertical vector β represented by seven empty boxes, labeled from top to bottom as 0, ?, ?, 0, 0, 0, and 0.

We can solve this problem if **an oracle** tells us that only a small number of coefficients are nonzero!

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We can solve this problem if **an oracle** tells us that only a small number of coefficients are nonzero!

In reality, we do not know which coefficients are nonzero, nor do we know if the coefficients are sparse!

Use Prior to Improve Power

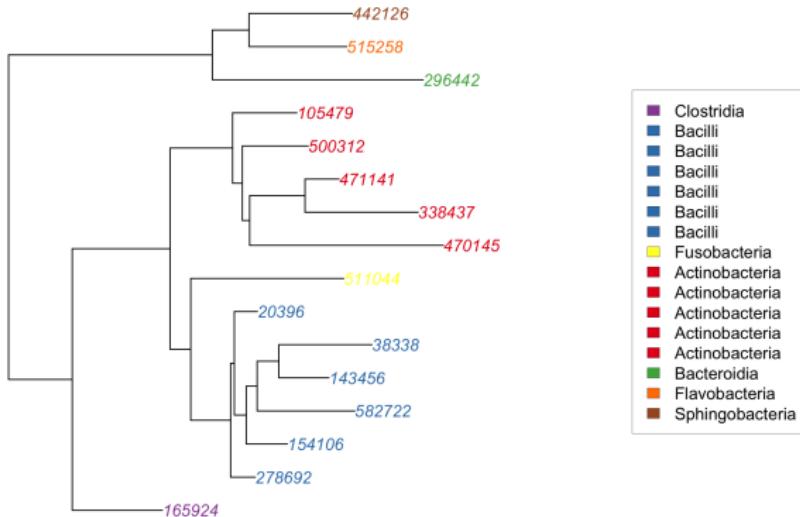
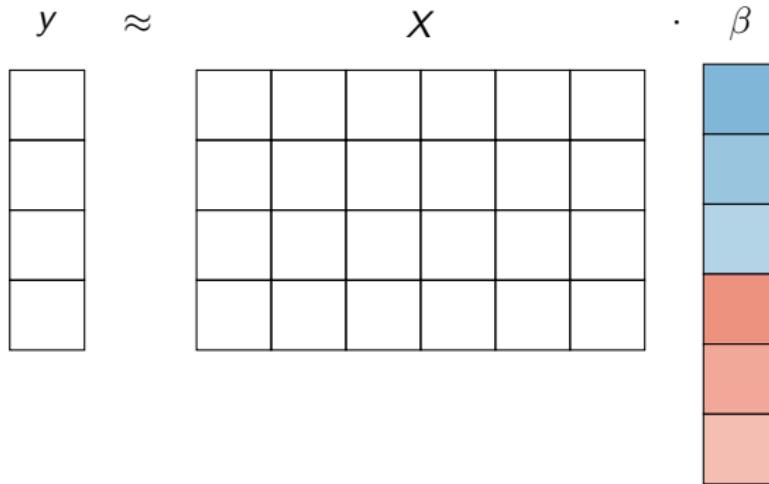


Figure 3: A simple phylogenetic tree

Bacteria closer on the tree are more similar in their DNA content and have similar effects on the outcome (**a reasonable assumption**).

Use Prior to Improve Power

$$y \approx X \cdot \beta$$


Assume coefficients are **smooth** with respect to the prior!

Are Observations Independent?



Most methods assume the observations are independent and identically distributed. **Is this assumption valid?**

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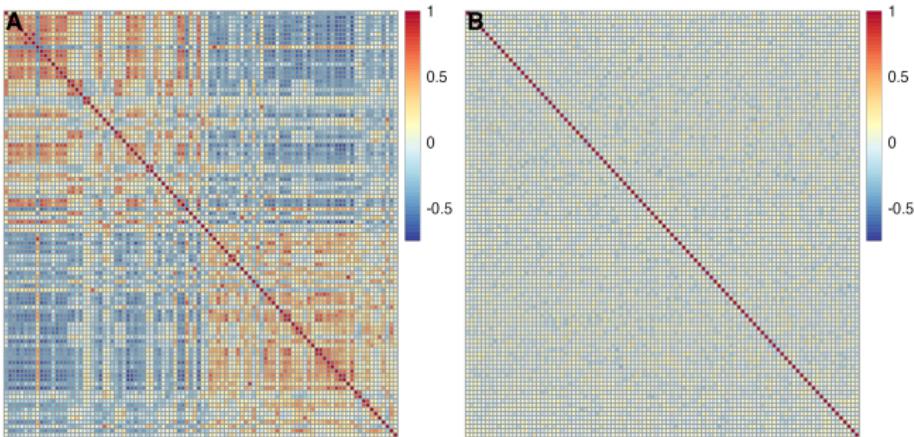


Figure 4: Correlation among (A) Yatsunenko samples; (B) independent samples

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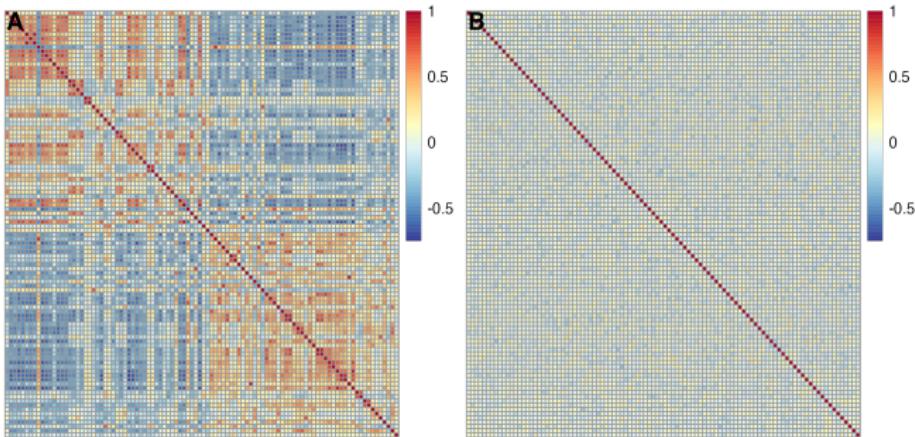


Figure 4: Correlation among (A) Yatsunenko samples; (B) independent samples

In Yatsunenko 12', subjects include individuals from the same household (twins, parent-offspring relationships).

Observations are Correlated



If a treatment works in a person's microbiome, it is more likely to work in the microbiome of their twin siblings.

It is unfair to count good outcomes in both individuals as 2 independent pieces of evidence for the treatment's effectiveness.

Doing so artificially increases the sample size, decreases the P values, and potentially results in effects being deemed significant when they should not be (a **type I error**).

If **an oracle** tells us the correlation among observations, we can use this knowledge to de-correlate the observations. This is called **generalized least squares**.

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In the absence of this oracle, we can derive a prior on sample correlation from **auxiliary data**.

Accounting for Correlated Observations

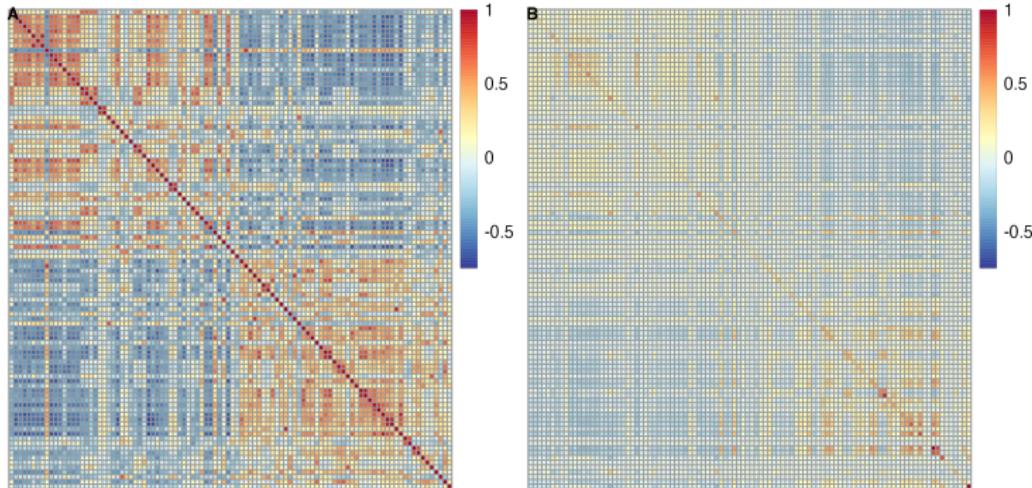


Figure 5: Sample correlation in Yatsunenko 12' from (A) 16S abundance and (B) metagenomic pathway abundance

Generalized Matrix Decomposition Regression

$$y_i = X_{i,1}\beta_1 + \dots + X_{i,p}\beta_p + \text{error}_i,$$



Yue Wang

subject to the constraints that

- the coefficients β are smooth with respect to a variable similarity network Q
- the **error** covariance is smooth with respect to a sample similarity network H

Prior Misspecification



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We propose robust GMDR:

- ① Test the association between given prior and observed correlations using the Kernel RV (KRV) coefficient. KRV rejects the null → prior is at least partially informative.

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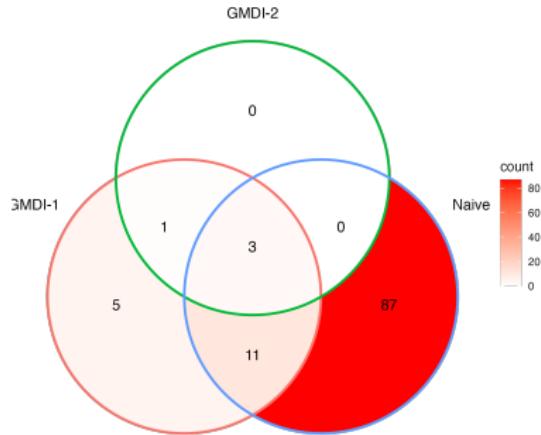
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- ① Test the association between given prior and observed correlations using the Kernel RV (KRV) coefficient. KRV rejects the null → prior is at least partially informative.
- ② For partially informative prior, use a likelihood criterion to weight the prior against an uninformative baseline.

Revisit Yatsunenko 12'

Which bacteria are associated with age?

- $n = 100$
- $p = 149$
- FDR = 0.1
- Results from **robust GMDI**.



GMDI-1: discrete shrinkage; GMDI-2: continuous shrinkage

Visualization

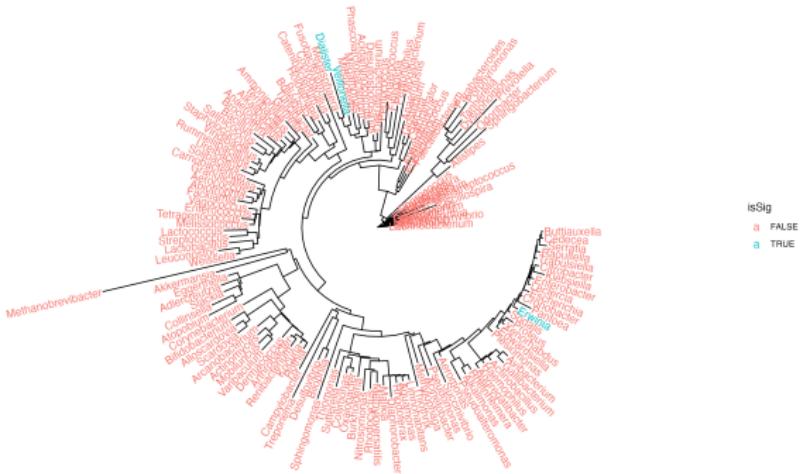


Figure 6: *Dialister* and *Veillonella* are phylogenetically close.

- *Dialister* has been shown to play a role in age-related diseases, such as obesity and diabetes⁵.
 - *Veillonella* is a signature of infant (4-month old) microbiome and breast feeding⁶.

⁵Xu et al., 20'; Gurung et al., 20'

⁶Backhed et al., 15'

Network biology

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- gut-brain association: how to define the association and perform valid inference?

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- disease association networks: how do disease co-occurrences vary with age? how to integrate data from epidemiological surveys with electronic medical records?

Microbiome

- gut-brain association: how to define the association and perform valid inference?
- microbiome and cancer: what features of the microbiome are correlated with cancer diagnosis and treatment?

Acknowledgement

Ma Lab



Yue Wang (CU), Ilias Moysidis (CERTH), Kristyn Pantoja (Novartis), Xinyi Xie,
Wenjie Guan

Collaborators



Tim Randolph, Ali Shojaie, David Jones, Kate Markey, Robert Kaplan

Funding



National Institute of
General Medical Sciences

FHCC TDS IRC Pilot