

EE 5450 Project 01: Simultaneous Monocular Calibration and Pose Estimation

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February 21, 2018

1 Introduction

Determination of the pose of rigid objects within images is a common problem within many practical application of computer vision, robotics, computer graphics, etc. The following set of experiments are focused on the application of the simultaneous monocular calibration and pose estimation algorithm to a series of images of rigid objects with known dimensions and correspondence points. From this known data, the algorithm is capable of calibrating a single monocular camera with a fixed focal length. The calibration enables simultaneous discovery of the pose of the viewed object, and from this generate a three dimensional representation of that same object.

2 Methods and Results

The foundation of this project is based on the known dimensions of a given rigid object, a box for example, which is manually assigned a number of points on the object corresponding to its corners (i.e. the coordinates in the object frame represent the dimensions of the object). A model of the initial box and its correspondence points can be seen in Figure 1, additionally, the measured dimensions of the object are shown in Table 1. Given this data we are able to proceed with the implementation of the monocular pose algorithm.

Using the object coordinates in their homogeneous form (i.e. $X_o^i = [x_o^i \ y_o^i \ z_o^i \ 1]^T$), we begin with calculating an approximation of the projection matrix, Π_{est} . The projection matrix is such that $\Pi = [KR \ KT] \in \mathbb{R}^{3 \times 4}$, where K is the camera calibration matrix, R is a rotation matrix, and T is the translation vector. Given that we know the location of the correspondence points, χ^{pj} , and their matching locations in the object frame, X_o^j , assuming that a sufficient number of points are provided, we are then able to find an approximation to Π . This approximation can be expressed as a least squares minimization of Equation 1, where e_3 is the standard basis vector $[001]^T$, Π^S is the vectorized or “stacked” version of Π , and \otimes represents the Kronecker product. The least squares estimate of the vectorized projection matrix can be found as the minimum input direction of N , which is the final right singular vector yielded from the singular value decomposition (SVD) of N .

$$N^j \Pi^{pj} = [(X_o^{jT} \otimes I_3) - (X_o^{jT} \otimes \chi^{pj} e_3^T)] \Pi^S = 0 \quad (1)$$

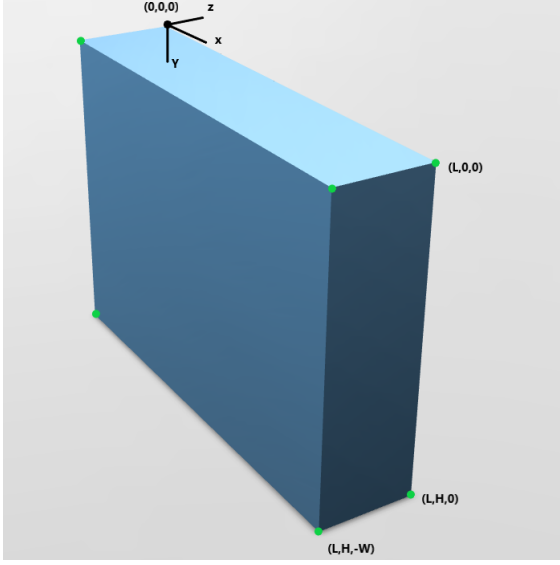


Figure 1: Rigid object model.

Parameter	Value (cm)
<i>Length</i>	45.6
<i>Height</i>	32.5
<i>Width</i>	10.1

Table 1: Object Dimensions

From this we are able to de-vectorize the result of the SVD and obtain Π_{est} . Using this we extract all of the necessary components to describe the calibration and pose of the camera. From order reversing the standard QR decomposition we are able to obtain the scaling factor α , the calibration matrix, and the rotation matrices corresponding to the given set of pixel coordinates. Using this information we can lastly find the translation vector associated with the system from the following equation, where $T' = KT$, and is the rightmost column of Π_{est} :

$$T = \frac{K^{-1}T'}{\alpha} \quad (2) \quad \chi^{pj} = \frac{\Pi_{est}X_0^j}{\lambda^j} \quad (3)$$

Using the information obtained from the algorithm, we next show the ability to project estimated pixel coordinates in to the image plane. These estimated pixel coordinates are described by Equation 3. From this we are able to qualitatively visualize the success of the algorithm in matching provided correspondence points. From the estimated pixel coordinates in noiseless reconstructions of the object we calculate the average root mean square error (RMSE) of the position between the true coordinates and their respective estimates in the object frame in order to establish the overall fidelity of the algorithm across multiple images taken with varying rotations, translations, and calibrations. In this case PRMSE is expressed as:

$$content... \quad (4)$$

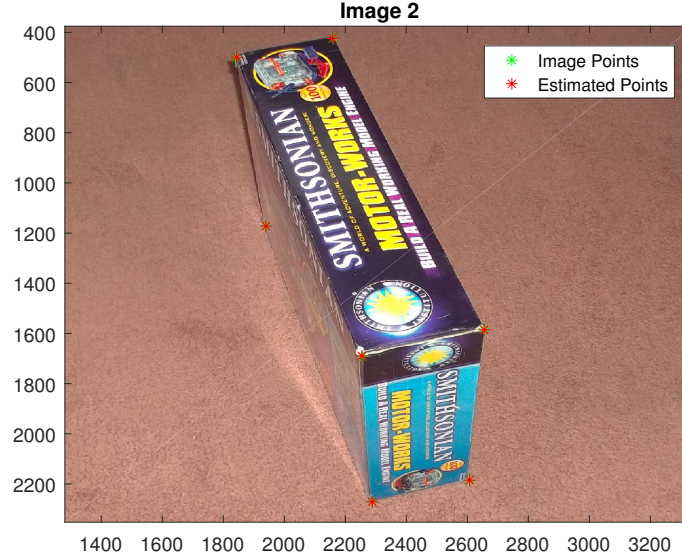


Figure 2: Estimated pixel coordinates

2.1 Corrupted Correspondence Points

Once the results of the algorithm are proven to work on its own data sets we observe the effect of the calibration and pose established by the algorithm on the pure data set (as opposed to the estimated) data to observe the distortions due to noise or error in correspondence.

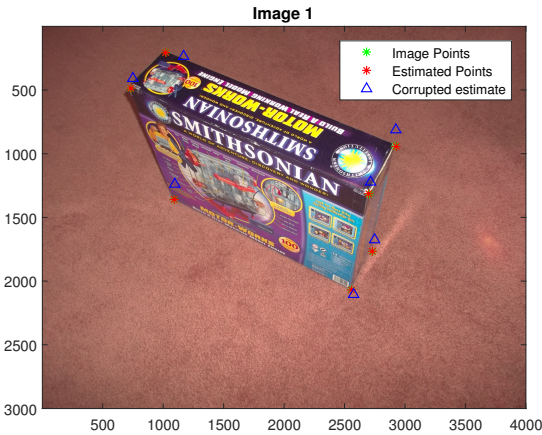


Figure 3: Estimated image coordinates

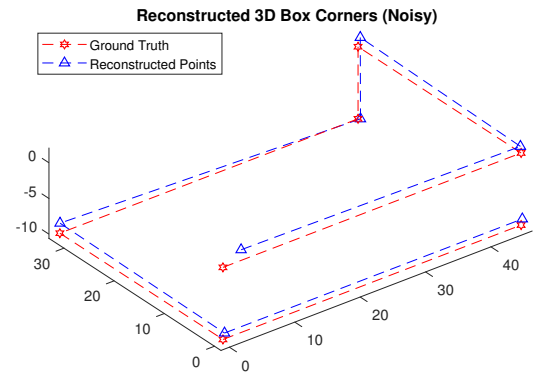


Figure 4: Reconstructed box relative to ground truth

2.2 Improper Dimensions

3 Conclusions

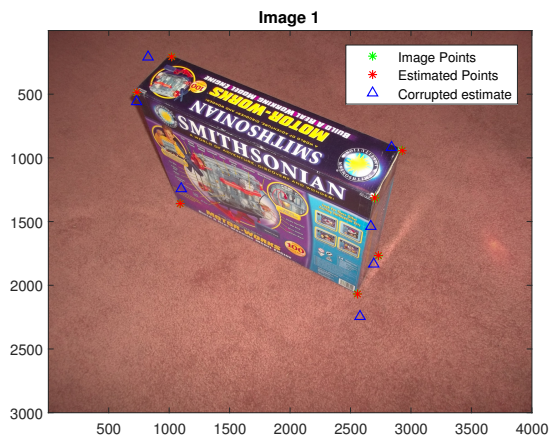


Figure 5: Estimated image coordinates (unique coordinate component noise)

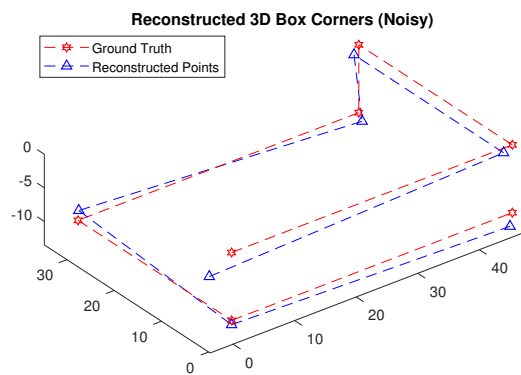


Figure 6: Reconstructed box relative to ground truth

A Code Listings

References