Username: CS441 2025-09-03 Name: Discrete Structures for CS rec_1

Problem 1. Which of these sentences are propositions? What are the truth values of those that are propositions?

- a) 2 + 3 = 5
- b) Wash your hands
- c) Swimming is fun
- d) $2x \ge x$
- e) 4.3 is an integer

Username: CS441 2025-09-03 Name: Discrete Structures for CS rec_1

Problem 2. Let p and q be the propositions "Swimming at the shore is allowed" and "Sharks have been spotted near the shore," respectively. Express each of these compound propositions as an English sentence.

- a) $\neg q \wedge \neg p$
- b) $\neg q \rightarrow p$
- c) $p \leftrightarrow \neg q$

- a)
- b)
- c)

Username:	CS441	2025-09-03
Name:	Discrete Structures for CS	rec 1

Problem 3. For each of the following sentences, determine whether an inclusive or, or an exclusive or, is intended. Explain your answer.

- a) Coffee or tea comes with dinner
- b) A password must have at least three digits or be at least eight characters long.
- c) The prerequisite for the course is a course in number theory or a course in cryptography.
- d) You can pay using U.S. dollars or euros.)

Username: CS4412025-09-03 Name: Discrete Structures for CS ${\rm rec}_1$

Problem 4. Construct a truth table for each of these compound propositions.

- a) $(p \lor \neg q) \to q$
- b) $(p \to q) \leftrightarrow (\neg p \lor q)$ c) $(p \land q) \to (p \lor q)$

Username:	CS441	2025-09-03
Name:	Discrete Structures for CS	rec 1

 ${\bf Problem~5.~State~the~converse,~contrapositive,~and~inverse~of~each~of~the~following~conditional~statements.}$

- a) I will wear a sweater only if it is below freezing.
- b) I come to class whenever there is a quiz.
- c) If I have a connecting flight, it is necessary for me to fly business class.

Username: CS441 2025-09-03 Name: Discrete Structures for CS rec_1

Problem 6. Determine whether each of the following conditional statements is true or false. Explain your answers.

- a) If 1 + 1 = 2 then 2 + 2 = 5.
- b) If 1+1=3 then 2+2=4.
- c) If 1 + 1 = 2then 2 + 2 = 4.
- d) If monkeys can fly then 1 + 1 = 3.

Username:	CS441	2025-09-03
Name:	Discrete Structures for CS	rec_1

Problem 7. Determine whether each of the following biconditional statements is true or false. Explain your answers.

- a) 1 + 1 = 2 if and only if 2 + 2 = 5.
- b) 1 + 1 = 3 if and only if 2 + 2 = 4.
- c) 1+1=2 if and only if 2+2=4.
- d) Monkeys can fly if and only if 1 + 1 = 3.