Comparing von Bertalanffy Growth Functions

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Preliminaries

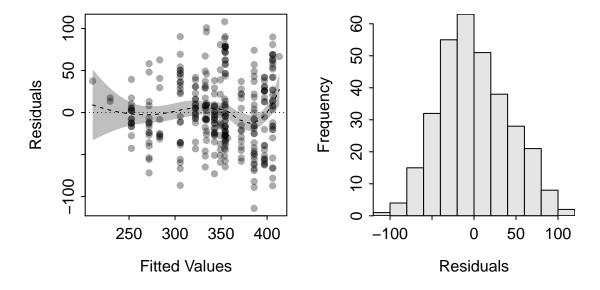
```
> library(FSA)
> library(FSAdata)  # for Croaker2 data
> library(dplyr)  # for mutate()
```

Loading the Data and Some Preparations

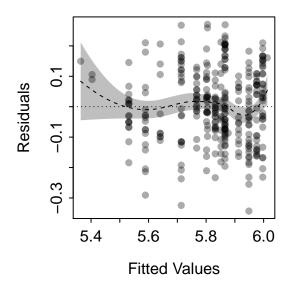
```
> data(Croaker2)
> str(Croaker2)
'data.frame': 318 obs. of 3 variables:
$ age: int 1 1 1 2 2 2 2 2 2 2 2 ...
$ t1 : int 243 247 248 330 320 285 280 265 260 248 ...
$ sex: Factor w/ 2 levels "F", "M": 1 1 2 1 1 1 1 1 1 1 ...
> Croaker2 <- mutate(Croaker2, logTL=log(t1))</pre>
```

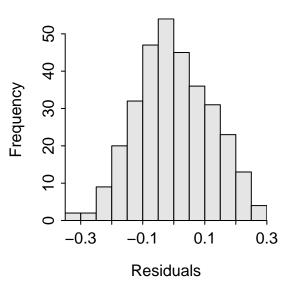
Fitting Most Complex Model and Checking Assumptions

```
> ( sv0m <- vbStarts(tl~age,data=Croaker2,meth0="yngAge") )</pre>
$Linf
[1] 434.697
$K
[1] 0.1837369
$t0
[1] -3.541856
> ( svLKt <- Map(rep,svOm,c(2,2,2)) )</pre>
[1] 434.697 434.697
$K
[1] 0.1837369 0.1837369
$t0
[1] -3.541856 -3.541856
> vbLKt <- tl~Linf[sex]*(1-exp(-K[sex]*(age-t0[sex])))</pre>
> fitLKt <- nls(vbLKt,data=Croaker2,start=svLKt)</pre>
> residPlot(fitLKt,col=rgb(0,0,0,1/3))
```



- > vbLKt <- logTL~log(Linf[sex]*(1-exp(-K[sex]*(age-t0[sex]))))
- > fitLKt <- nls(vbLKt,data=Croaker2,start=svLKt)</pre>
- > residPlot(fitLKt,col=rgb(0,0,0,1/3))





Are There Any Differences?

```
> vbOm <- logTL~log(Linf*(1-exp(-K*(age-t0))))</pre>
> fit0m <- nls(vb0m,data=Croaker2,start=sv0m)</pre>
> extraSS(fitOm,com=fitLKt,sim.name="{Omega}",com.name="{Linf,K,t0}")
Model 1: {Omega}
Model A: {Linf,K,t0}
    DfO
           RSSO DfA
                       RSSA Df
                                                  Pr(>F)
                                     SS
1vA 315 5.23971 312 4.44264 3 0.79707 18.659 3.705e-11
> lrt(fit0m,com=fitLKt,sim.name="{Omega}",com.name="{Linf,K,t0}")
Model 1: {Omega}
Model A: {Linf,K,t0}
    DfO logLikO DfA logLikA Df logLik Chisq Pr(>Chisq)
1vA 315 201.597 312 227.835 3 -26.238 52.476 2.372e-11
```

Is the Most Complex Model Warranted?

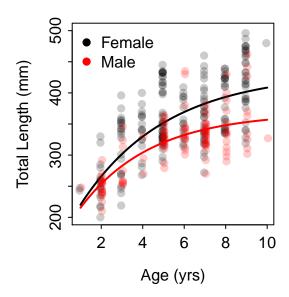
```
> vbLK <- logTL~log(Linf[sex]*(1-exp(-K[sex]*(age-t0))))</pre>
> ( svLK <- Map(rep,svOm,c(2,2,1)) )</pre>
$Linf
[1] 434.697 434.697
$K
[1] 0.1837369 0.1837369
$t0
[1] -3.541856
> fitLK <- nls(vbLK,data=Croaker2,start=svLK)</pre>
> vbLt <- logTL~log(Linf[sex]*(1-exp(-K*(age-t0[sex]))))</pre>
> svLt <- Map(rep,sv0m,c(2,1,2))
> fitLt <- nls(vbLt,data=Croaker2,start=svLt)</pre>
> vbKt <- logTL~log(Linf*(1-exp(-K[sex]*(age-t0[sex]))))
> svKt <- Map(rep,svOm,c(1,2,2))
> fitKt <- nls(vbKt,data=Croaker2,start=svKt)</pre>
> extraSS(fitLK,fitLt,fitKt,com=fitLKt,com.name="{Linf,K,t0}",
          sim.names=c("{Linf,K}","{Linf,t0}","{K,t0}"))
Model 1: {Linf,K}
Model 2: {Linf,t0}
Model 3: {K,t0}
Model A: {Linf,K,t0}
            RSSO DfA
    DfO
                          RSSA Df
                                         SS
                                                 F Pr(>F)
1vA 313 4.442641 312 4.442639 1 0.000002 0.0001 0.9916
2vA 313 4.444957 312 4.442639 1 0.002318 0.1628 0.6869
3vA 313 4.476736 312 4.442639 1 0.034097 2.3946 0.1228
```

Can the Model be Reduced to Only One Parameter that Differs?

```
> vbL < logTL\simlog(Linf[sex]*(1-exp(-K*(age-t0))))
> (svL \leftarrow Map(rep, svOm, c(2,1,1)))
$Linf
[1] 434.697 434.697
$K
[1] 0.1837369
$t0
[1] -3.541856
> fitL <- nls(vbL,data=Croaker2,start=svL)</pre>
> vbK <- logTL~log(Linf*(1-exp(-K[sex]*(age-t0))))</pre>
> svK \leftarrow Map(rep,svOm,c(1,2,1))
> fitK <- nls(vbK,data=Croaker2,start=svK)</pre>
> extraSS(fitL,fitK,com=fitLK,com.name="{Linf,K}",sim.names=c("{Linf}","{K}"))
Model 1: {Linf}
Model 2: {K}
Model A: {Linf,K}
    DfO
             RSSO DfA
                           RSSA Df
                                          SS
                                                    F
                                                        Pr(>F)
1vA 314 4.484252 313 4.442641 1 0.041612 2.9317 0.087847
2vA 314 4.621667 313 4.442641 1 0.179027 12.6131 0.000442
```

Summarize Final Model

```
> summary(fitL,correlation=TRUE)
Formula: logTL \sim log(Linf[sex] * (1 - exp(-K * (age - t0))))
Parameters:
       Estimate Std. Error t value Pr(>|t|)
Linf1 425.37154 17.13519 24.824 < 2e-16
Linf2 384.21646 15.65097 24.549 < 2e-16
      0.24825 0.05315 4.671 4.45e-06
       -2.12303 0.66226 -3.206 0.00149
t0
Residual standard error: 0.1195 on 314 degrees of freedom
Correlation of Parameter Estimates:
      Linf1 Linf2 K
Linf2 0.94
     -0.95 -0.93
      -0.87 -0.85 0.97
Number of iterations to convergence: 4
Achieved convergence tolerance: 1.84e-06
> round(cbind(coef(fitL),confint(fitL)),3)
Waiting for profiling to be done...
                 2.5%
                      97.5%
Linf1 425.372 400.090 481.671
Linf2 384.216 360.721 435.082
K
       0.248 0.144 0.357
      -2.123 -3.986 -1.108
t0
> vb <- vbFuns("typical")</pre>
> # Females
> crF <- filterD(Croaker2,sex=="F")</pre>
> svF <- list(Linf=425,K=0.25,t0=-2)
> fitF <- nls(logTL~log(vb(age,Linf,K,t0)),data=crF,start=svF)</pre>
> # Males
> crM <- filterD(Croaker2,sex=="M")</pre>
> svM <- list(Linf=385,K=0.25,t0=-2)
> fitM <- nls(logTL~log(vb(age,Linf,K,t0)),data=crM,start=svM)</pre>
> clr1 <- c(rgb(0,0,0,1/5),rgb(1,0,0,1/5))
> clr2 <- c("black","red")</pre>
> offset <- 0.04
> # Females
> plot(tl~I(age-offset),data=crF,pch=19,col=clr1[1],ylim=c(200,500),
       xlab="Age (yrs)",ylab="Total Length (mm)")
> curve(vb(x-offset,coef(fitF)),from=1,to=10,col=clr2[1],lwd=2,add=TRUE)
> # Males
> points(tl~I(age+offset),data=crM,pch=19,col=clr1[2])
> curve(vb(x+offset,coef(fitM)),from=1,to=10,col=clr2[2],lwd=2,add=TRUE)
> legend("topleft",c("Female","Male"),pch=19,col=clr2,bty="n")
```



Using Information Criterion

Fit the Only Other Model not Fit Above

```
> vbt <- logTL~log(Linf*(1-exp(-K*(age-t0[sex]))))
> svt <- Map(rep,sv0m,c(1,1,2))
> fitt <- nls(vbt,data=Croaker2,start=svt)</pre>
```

AICc Table

```
> library(AICcmodavg)
> ms <- list(fitOm,fitL,fitK,fitLK,fitLt,fitKt,fitLKt)
> mnames <- c("{Omega}","{Linf}","{K}","{t0}","{Linf,K}","{Linf,t0}","{K,t0}","{Linf,K,t0}")
> aictab(ms,mnames)
```

Model selection based on AICc :

	K	AICc	Delta_AICc	AICcWt	Cum.Wt	LL
{Linf,K}	6	-443.40	0.00	0.31	0.31	227.84
{Linf,t0}	6	-443.23	0.17	0.29	0.60	227.75
{Linf}	5	-442.51	0.89	0.20	0.80	226.35
{Linf,K,t0}	7	-441.31	2.09	0.11	0.91	227.84
{K,t0}	6	-440.97	2.43	0.09	1.00	226.62
{K}	5	-432.91	10.49	0.00	1.00	221.55
{t0}	5	-422.44	20.96	0.00	1.00	216.31
{Omega}	4	-395.07	48.33	0.00	1.00	201.60