HYPOTHESIS TESTING • MTH107

Class R FAQ

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1-Sample Z-Test

H_0: $\mu = \mu_0$ (where μ_0 = specific value)

Statistic: $\bar{x}$ **Test Statistic:** $Z = \frac{\bar{x}-\mu_0}{\frac{\sigma}{\sqrt{n}}}$ **Conf. Region:** $\bar{x} + Z^* \frac{\sigma}{\sqrt{n}}$

Assumptions: 1) σ is known
2) $n \geq 30$, $n \geq 15$ and popn not strongly skewed, OR popn is normal

R: z.test()

1-Sample t-Test

H_0: $\mu = \mu_0$ (where μ_0 = specific value)

Statistic: $\bar{x}$ **Test Statistic.:** $t = \frac{\bar{x}-\mu_0}{\frac{s}{\sqrt{n}}}$ **Conf. Region:** $\bar{x} + t^* \frac{s}{\sqrt{n}}$ **df:** n-1

Assumptions: 1) σ is UNknown,
2) $n \geq 40$, $n \geq 15$ & histogram not strongly skewed, OR histogram is normal

R: t.test(), hist()

2-Sample t-Test

H_0: $\mu_1 = \mu_2$ **Statistic:** $\bar{x}_1 - \bar{x}_2$

Test Statistic: $t = \frac{(\bar{x}_1-\bar{x}_2)-0}{\sqrt{s_p^2\left(\frac{1}{n_1}+\frac{1}{n_2}\right)}}$ where $s_p^2 = \frac{(n_1-1)s_1^2+(n_2-1)s_2^2}{n_1+n_2-2}$

Conf. Region: $(\bar{x}_1 - \bar{x}_2) + t^* \sqrt{s_p^2\left(\frac{1}{n_1}+\frac{1}{n_2}\right)}$ **df:** $n_1 + n_2 - 2$

Assumptions:
1) Individuals in populations are independent
2) Variances are equal (use Levene's Test)
3) $n_1+n_2 \geq 40$, $n_1+n_2 \geq 15$ and both histograms are not strongly skewed, OR both histograms are normal

R: t.test(), levenesTest(), hist()

Choosing a Hypothesis Test

1. If response variable is QUANTITATIVE, then GOTO 2; otherwise GOTO 5.

Quantitative Response
2. If 1 POPULATION was sampled, then GOTO 3; otherwise GOTO 4.
3. If σ is KNOWN, then **1-Sample Z**; otherwise **1-Sample t**.
4. If individuals in populations are INDEPENDENT, then **2-Sample t**; otherwise, **Paired t**.

Categorical Response
5. If 1 POPULATION was sampled, then **Goodness-of-Fit**; otherwise, **Chi-Square**.

Making a Decision about H_0

If the p-value < α, then **REJECT H_0**., otherwise **DNR H_0**.

Chi-Square Test

H_0: "Distribution of individuals into response levels is the same for all populations"
H_A: "Distribution of individs into response levels is NOT the same for all populations"

Statistic: Observed frequency table

Test Statistic: $\chi^2 = \sum \frac{(\text{Observed}-\text{Expected})^2}{\text{Expected}}$ **df:** (rows-1)(columns-1)

Assumptions: $\geq$5 in each cell of the expected table

R: xtabs(), matrix(), chisq.test(), percTable()

Goodness-of-Fit Test

H_0: "Distribution of individs into response levels follows the theoretical distribution"
H_A: "Distribution of indivuals into response levels does NOT follow the theoretical distribution"

Statistic: Observed frequency table

Test Statistic: $\chi^2 = \sum \frac{(\text{Observed}-\text{Expected})^2}{\text{Expected}}$ **df:** cells-1

Assumptions: $\geq$5 in each cell of the expected table

R: xtabs(), c(), chisq.test(), percTable(), chiGOF()

11 Steps for Any Hypothesis Test

1) State the rejection criterion (α)

2) State the null & alternative hypotheses and define the parameter(s)

3) Determine which test to perform – Explain!

4) Collect the data (address type of study and randomization)

5) Check all necessary assumption(s)

6) Calculate the appropriate statistic(s)

7) Calculate the appropriate test statistic

8) Calculate the p-value

9) State your rejection decision

10) Summarize your findings in terms of the problem

11) **If rejected H_0,** compute a **100(1-α)%** *confidence region* for parameter