## Question 2.1

a. Table below

Source	df	SS	MS	F	p-value
Among Groups	7	35819	5117	3.5	0.0099
Within Groups	24	35088	1462		
Total	31	70907			

 $df_{among}$  and  $SS_{among}$  come from subtracting the within value from the total value.  $MS_{among}$  comes from  $SS_{among}$  divide by  $df_{among}$ . F is then  $MS_{among}$  divided by  $MS_{within}$ . Finally the p-value comes from distrib(3.5,distrib="f",df1=7,df2=24,lower.tail=FALSE).

- b. The number of groups = 7+1 = 8 (i.e.,  $df_{among}+1$ ).
- c. The number of individuals = 31+1 = 32 (i.e.,  $df_{total}+1$ ).
- d. The variability among individuals within groups is  $s_p^s = MS_{within} = 1462$ .
- e. The variabilty among individuals ignoring groups is  $s^2 = MS_{total} = \frac{70907}{31} = 2287.3$ .
- f. Yes, there is a difference among the group means because the p-value is less than 0.05.

## Question 2.2

a. Table below

Source	df	SS	MS	F	p-value
Among Groups	3	17.25	5.75	1.26	0.3149
Within Groups	20	91.20	4.56		
Total	23	108.45			

 $MS_{among}$  comes from multiplying F and  $MS_{within}$ .  $df_{among}$  then comes from dividing  $SS_{among}$  by  $MS_{among}$ .  $df_{within}$  then comes from  $df_{total}$ - $df_{among}$ .  $SS_{within}$  is then  $MS_{within}$  times  $df_{within}$ .  $SS_{total}$  is then  $SS_{among} + SS_{within}$ . Finally the p-value comes from distrib(1.26,distrib="f",df1=3,df2=20,lower.tail="distrib").

- b. The number of groups = 3+1 = 4 (i.e.,  $df_{among}+1$ ).
- c. The number of individuals = 23+1 = 24 (i.e.,  $df_{total}+1$ ).
- d. The variability among individuals within groups is  $s_p^s = MS_{within} = 4.56$ .
- e. The variabilty among individuals ignoring groups is  $s^2 = MS_{total} = \frac{108.45}{23} = 4.72$ .
- f. No there is not a difference among the group means because the p-value is greater than 0.05.

## Question 2.3

a. Table below

Source	df	SS	MS	F	p-value
Among Groups	5	887.05	177.41	5.25	0.0006
Within Groups	48	1621.44	33.78		
Total	53	2508.49	47.33		

Note that  $MS_{total}$  and  $MS_{within}$  were given by definition. The  $df_{among}$  and  $df_{total}$  were given by knowing the number of groups and total number of individuals. The SS are then obtained, the final MS, and the F. The p-value is computed with distrib(5.25, distrib="f", df1=5, df2=48, lower.tail=FALSE)

b. Yes, there is a difference among the group means because the p-value is less than 0.05.