Question 4.6 (15 pts)

a. It is difficult to ultimately assess independence with the amount of information given. However, under the assumption that all 618 children were unique (no child was measured twice) then it seems that the data are at least roughly independent. There is some evidence for a slight non-linearity (Figure 1). The residual plot suggests a heteroscedasticity (Figure 1). The residuals do not appear to be normal (Anderson Darling p<0.00005) and are right-skewed (Figure 2). I did not test for outliers given the violations of the normality and homoscedasticity assumptions.
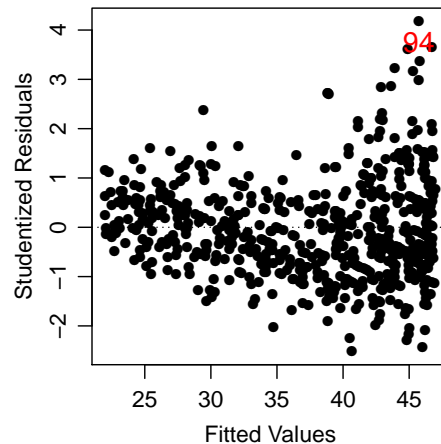

Figure 1. Residual plot for the simple linear regression of respiratory rate on child's age.
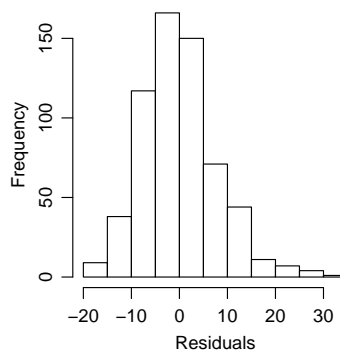

Figure 2. Histogram of residuals from the simple linear regression of respiratory rate on child's age.

b. The ratio of maximum to minimum age was 360 suggesting that the age variable sould be transformed to logarithms. However, the trial-and-error method suggested leaving age untransformed and transforming respiratory rate to logarithms would provide an adequate fit. With only log-transformed respiratory rate there was no visual evidence for a non-linearity (Figure 3), the residuals appeared homoscedastic (Figure 3) and normal (Anderson-Darling p=0.3093; Figure 4), and there was no evidence for significant outliers (outlier test p=0.8544). Thus, the assumptions appear to be adequately met on this transformed scale.

c. There is a signficant relationship between the log respiratory rate and the age of a child (p<0.00005; Table 1; Figure 5). Specifically, as the age of the child increases by one month then the average log respiratory rate *decreases* between 0.018 and 0.020.
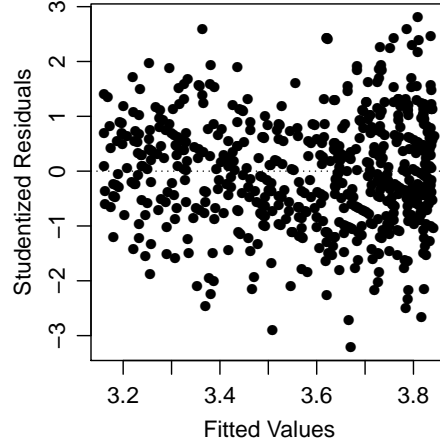
Figure 3. Residual plot for the simple linear regression of log-transformed respiratory rate on child's age.
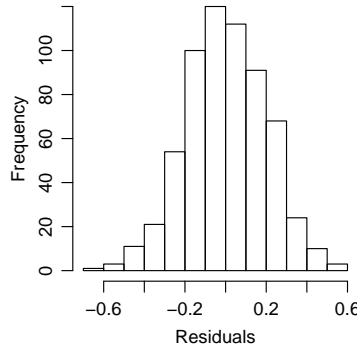

Figure 4. Histogram of residuals from the simple linear regression of log-transformed respiratory rate on child's age.

Table 1. ANOVA table for simple linear regression results of log-transformed respiratory rate on child's age.

```
          Df Sum Sq Mean Sq F value    Pr(>F)
age        1  34496   34496  560.92 < 2.2e-16
Residuals 616  37884      61
```

    d. The predicted respiratory rate, corrected for back-transformation bias, for four different ages is shown in Table 2. For example, the predicted respiratory rate for a five month old child is between 29.5 and 63.8.

Table 2. Respiratory rates for variously aged children predicted from the simple linear regression of log-transformed respiratory rate on child's age.

```
   obs age      fit      lwr      upr
1    1   5 43.35232 29.46384 63.78746
2    2   6 42.53602 28.91028 62.58371
3    3  21 31.98339 21.73783 47.05793
4    4  22 31.38116 21.32759 46.17388
```
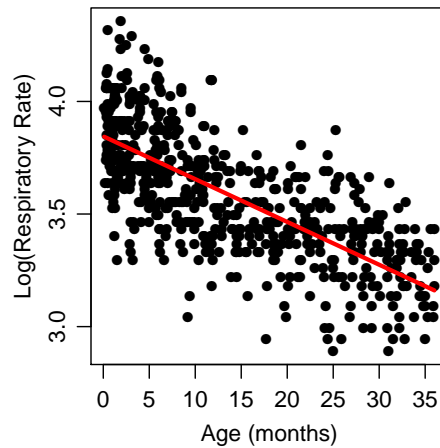
2

Figure 5. Fitted line plot for the simple linear regression of log-transformed respiratory rate on child's age.

R Commands

```
> rusc <- read.table("http://www.ncfaculty.net/dogle/R/Data_Master/R/Rusconi.txt",header=TRUE)
> lm1 <- lm(rate~age,data=rusc)
> adTest(lm1$residuals)
> residPlot(lm1,main="")
> hist(lm1$residuals,main="Residuals",main="")
> max(age)/min(age)
> transChooser(lm1)
> rusc$log.rate <- log(rusc$rate)
> lm2 <- lm(log.rate~age,data=rusc)
> fitPlot(lm2,xlab="Age (months)",ylab="Log(Respiratory Rate)",main="")
> residPlot(lm2,main="")
> hist(lm2$residuals,main="Residuals",main="")
> anova(lm2)
> summary(lm2)
> confint(lm2)
> nd <- data.frame(age=c(5,6,21,22))
> p.rate <- predict(lm2,nd,interval="prediction")
> exp(p.rate)*exp(anova(lm2)[2,3]/2)
```

Notes from Professor

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