

## ANOVA Table 1

1. Table below

Source	df	SS	MS	F	p-value
Among Groups	<b>7</b>	<b>35819</b>	<b>5117</b>	<b>3.5</b>	0.0099
Within Groups	24	35088	<b>1462</b>		
Total	31	70907			

$df_{among}$  and  $SS_{among}$  come from subtracting the within value from the total value.  $MS_{among}$  comes from  $SS_{among}$  divide by  $df_{among}$ .  $F$  is then  $MS_{among}$  divided by  $MS_{within}$ . Finally the p-value comes from `distrib(3.5,distrib="f",df1=7,df2=24,lower.tail=FALSE)`.

2. The number of groups =  $7+1 = 8$  (i.e.,  $df_{among}+1$ ).
3. The number of individuals =  $31+1 = 32$  (i.e.,  $df_{total}+1$ ).
4. The variability among individuals within groups is  $s_p^s = MS_{within} = 1462$ .
5. The variabilty among individuals ignoring groups is  $s^2 = MS_{total} = \frac{70907}{31} = 2287.3$ .
6. Yes, there is a difference among the group means because the p-value is less than 0.05.

## ANOVA Table 2

1. Table below

Source	df	SS	MS	F	p-value
Among Groups	<b>3</b>	17.25	<b>5.75</b>	1.26	0.3149
Within Groups	<b>20</b>	<b>91.20</b>	4.56		
Total	23	<b>108.45</b>			

$MS_{among}$  comes from multiplying  $F$  and  $MS_{within}$ .  $df_{among}$  then comes from dividing  $SS_{among}$  by  $MS_{among}$ .  $df_{within}$  then comes from  $df_{total}-df_{among}$ .  $SS_{within}$  is then  $MS_{within}$  times  $df_{within}$ .  $SS_{total}$  is then  $SS_{among} + SS_{within}$ . Finally the p-value comes from `distrib(1.26,distrib="f",df1=3,df2=20,lower.tail=FALSE)`.

2. The number of groups =  $3+1 = 4$  (i.e.,  $df_{among}+1$ ).
3. The number of individuals =  $23+1 = 24$  (i.e.,  $df_{total}+1$ ).
4. The variability among individuals within groups is  $s_p^s = MS_{within} = 4.56$ .
5. The variabilty among individuals ignoring groups is  $s^2 = MS_{total} = \frac{108.45}{23} = 4.72$ .
6. No there is not a difference among the group means because the p-value is greater than 0.05.

## ANOVA Table 3

1. Table below

Source	df	SS	MS	F	p-value
Among Groups	5	887.05	177.41	5.25	0.0006
Within Groups	48	1621.44	33.78		
Total	53	2508.49	<del>47.33</del>		

Note that  $MS_{total}$  and  $MS_{within}$  were given by definition. The  $df_{among}$  and  $df_{total}$  were given by knowing the number of groups and total number of individuals. The  $SS$  are then obtained, the final  $MS$ , and the  $F$ . The p-value is computed with `distrib(5.25,distrib="f",df1=5,df2=48,lower.tail=FALSE)`

2. Yes, there is a difference among the group means because the p-value is less than 0.05.