

One-Way ANOVA Handout

1 Initialization

```
> library(NCStats)
> library(multcomp) # for multiple comparison methods
```

2 Raspberry Example

You must change the directory to where the following file is located.

```
> rasp <- read.table("Raspberry.txt",head=TRUE)
> str(rasp)

'data.frame':      16 obs. of  2 variables:
 $ water : int  100 100 100 100 200 200 200 200 400 400 ...
 $ weight: num  8.1 10.9 11.1 13.9 12.2 11.5 11.4 6.8 6.5 5.5 ...

> rasp$fwater <- factor(rasp$water)
> str(rasp)

'data.frame':      16 obs. of  3 variables:
 $ water : int  100 100 100 100 200 200 200 200 400 400 ...
 $ weight: num  8.1 10.9 11.1 13.9 12.2 11.5 11.4 6.8 6.5 5.5 ...
 $ fwater: Factor w/ 4 levels "100","200","400",...: 1 1 1 1 2 2 2 2 3 3 ...
```

2.1 Fitting the Linear Model

```
> lm1 <- lm(weight~fwater,data=rasp)
> anova(lm1)
```

Analysis of Variance Table

```
Response: weight
      Df Sum Sq Mean Sq F value    Pr(>F)
fwater   3 115.043   38.348   10.793 0.001004
Residuals 12  42.635    3.553
```

```
> summary(lm1)
```

```
Call:
lm(formula = weight ~ fwater, data = rasp)
```

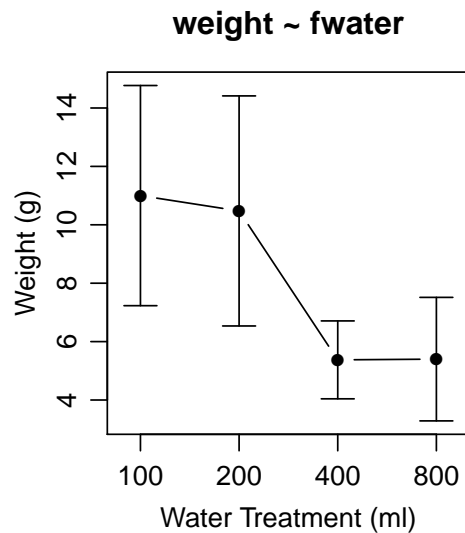
```
Residuals:
    Min       1Q   Median       3Q      Max
-3.6750 -0.5500  0.1125  1.0500  2.9000
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  11.0000     0.9425  11.672 6.58e-08
fwater200    -0.5250     1.3328  -0.394 0.70057
```

```
fwater400    -5.6250    1.3328   -4.220   0.00119
fwater800    -5.6000    1.3328   -4.202   0.00123
```

```
Residual standard error: 1.885 on 12 degrees of freedom
Multiple R-squared: 0.7296,      Adjusted R-squared: 0.662
F-statistic: 10.79 on 3 and 12 DF,  p-value: 0.001004
```

```
> fitPlot(lm1,xlab="Water Treatment (ml)",ylab="Weight (g)")
```



2.2 Multiple Comparison Tests

```
> rasp.mc <- glht(lm1, mcp(fwater = "Tukey"))
> summary(rasp.mc)
```

Simultaneous Tests for General Linear Hypotheses

Multiple Comparisons of Means: Tukey Contrasts

Fit: lm(formula = weight ~ fwater, data = rasp)

Linear Hypotheses:

	Estimate	Std. Error	t value	Pr(> t)
200 - 100 == 0	-0.525	1.333	-0.394	0.97832
400 - 100 == 0	-5.625	1.333	-4.220	0.00546
800 - 100 == 0	-5.600	1.333	-4.202	0.00586
400 - 200 == 0	-5.100	1.333	-3.826	0.01100
800 - 200 == 0	-5.075	1.333	-3.808	0.01147
800 - 400 == 0	0.025	1.333	0.019	1.00000

(Adjusted p values reported -- single-step method)

```
> confint(rasp.mc)
```

Simultaneous Confidence Intervals

Multiple Comparisons of Means: Tukey Contrasts

```
Fit: lm(formula = weight ~ fwater, data = rasp)
```

```
Quantile = 2.9679
```

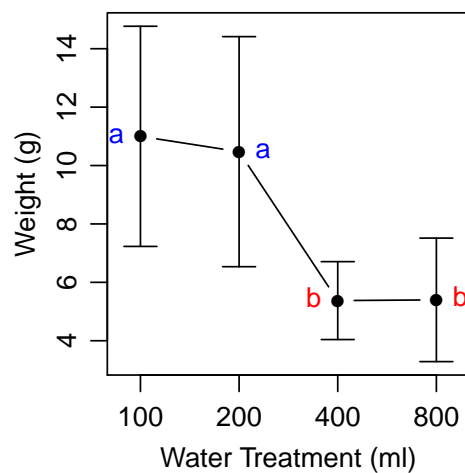
```
95% family-wise confidence level
```

```
Linear Hypotheses:
```

	Estimate	lwr	upr
200 - 100 == 0	-0.5250	-4.4807	3.4307
400 - 100 == 0	-5.6250	-9.5807	-1.6693
800 - 100 == 0	-5.6000	-9.5557	-1.6443
400 - 200 == 0	-5.1000	-9.0557	-1.1443
800 - 200 == 0	-5.0750	-9.0307	-1.1193
800 - 400 == 0	0.0250	-3.9307	3.9807

```
> fitPlot(lm1,xlab="Water Treatment (ml)",ylab="Weight (g)",main="")
```

```
> addSigLetters(lm1,lets=c("a","a","b","b"),pos=c(2,4,2,4),col=c("blue","blue","red","red"))
```



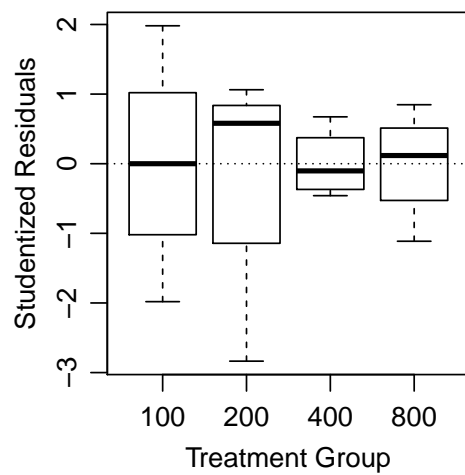
2.3 Checking the Assumptions

```
> leveneTest(lm1)
```

```
Levene's Test for Homogeneity of Variance (center = median)
```

	Df	F value	Pr(>F)
group	3	0.3256	0.8069
	12		

```
> residPlot(lm1)
```



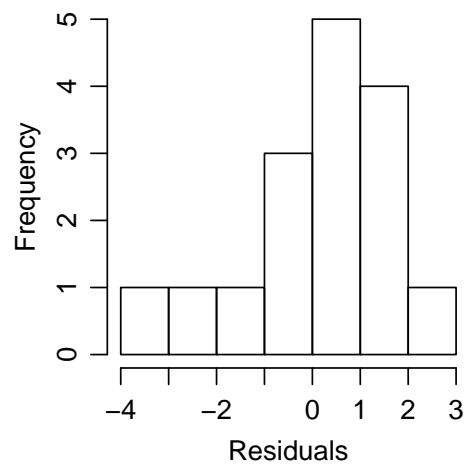
```
> adTest(lm1$residuals)
```

Anderson-Darling normality test

data: lm1\$residuals

A = 0.4308, p-value = 0.2688

```
> hist(lm1$residuals,xlab="Residuals",main="")
```



```
> outlierTest(lm1)
```

No Studentized residuals with Bonferonni $p < 0.05$

Largest |rstudent|:

	rstudent	unadjusted p-value	Bonferonni p
8	-2.836044	0.016196	0.25914

3 Benthic Infaunal Example

It is assumed that the initialization steps shown in Section 1 have already been followed and that the working directory has been changed to where the external data file is located.

```
> ben <- read.table("BenthicInfaunal.txt",head=TRUE)
> ben$fsite <- factor(ben$site)
> str(ben)

'data.frame':      72 obs. of  3 variables:
 $ site      : int  1 1 1 1 1 1 1 1 2 2 ...
 $ abundance: num  14.4 20.4 21.2 17.6 29 ...
 $ fsite     : Factor w/ 9 levels "1","2","3","4",...: 1 1 1 1 1 1 1 1 2 2 ...

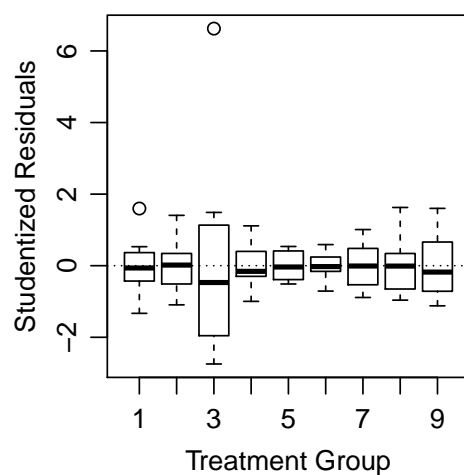
> lm2 <- lm(abundance~fsite,data=ben)
```

3.1 Assumption Checking with Possible Transformations

```
> leveneTest(lm2)

Levene's Test for Homogeneity of Variance (center = median)
      Df F value    Pr(>F)
group  8  3.2452 0.003726
      63

> residPlot(lm2)
```

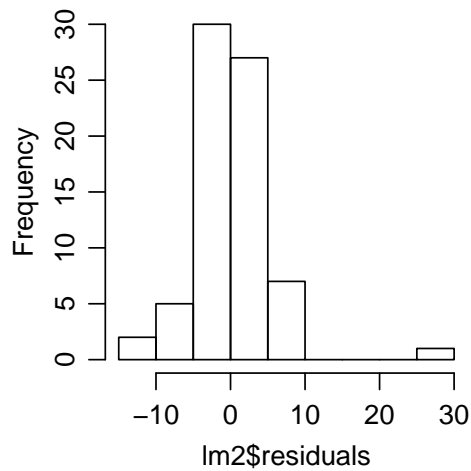


```
> adTest(lm2$residuals)

Anderson-Darling normality test

data:  lm2$residuals
A = 1.6389, p-value = 0.0002996
```

```
> hist(lm2$residuals,main="")
```



```
> outlierTest(lm2)
```

```
      rstudent unadjusted p-value Bonferonni p
20 6.624666      9.5554e-09    6.8799e-07
```

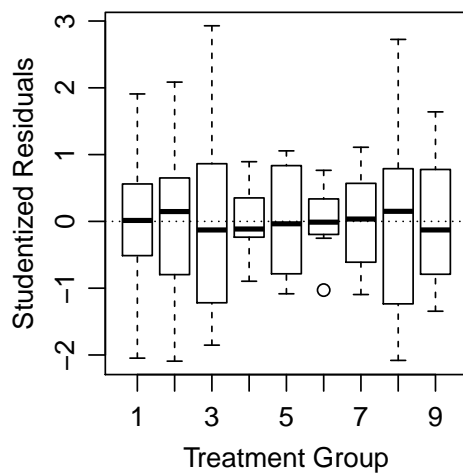
The following function was used to determine that a log transformation would most likely lead to the assumptions being met. This function cannot be illustrated in a handout because it requires interactions from the user.

```
> transChooser(lm2,show.stats=TRUE)
```

```
> ben$logab <- log(ben$abundance)
> lm3 <- lm(logab~fsite,data=ben)
> leveneTest(lm3)
```

```
Levene's Test for Homogeneity of Variance (center = median)
      Df F value Pr(>F)
group  8  1.5339 0.1636
      63
```

```
> residPlot(lm3)
```



```
> adTest(lm3$residuals)
```

Anderson-Darling normality test

```
data: lm3$residuals
```

```
A = 0.3323, p-value = 0.5062
```

```
> outlierTest(lm3)
```

No Studentized residuals with Bonferonni $p < 0.05$

Largest $|rstudent|$:

	$rstudent$	unadjusted p-value	Bonferonni p
20	2.928889	0.004754	0.34229

3.2 Model Summarization

```
> anova(lm3)
```

Analysis of Variance Table

Response: logab

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
fsite	8	8.6683	1.08353	29.066	< 2.2e-16
Residuals	63	2.3485	0.03728		

```
> ben.mc <- glht(lm3, mcp(fsite = "Dunnett"))
```

```
> summary(ben.mc)
```

Simultaneous Tests for General Linear Hypotheses

Multiple Comparisons of Means: Dunnett Contrasts

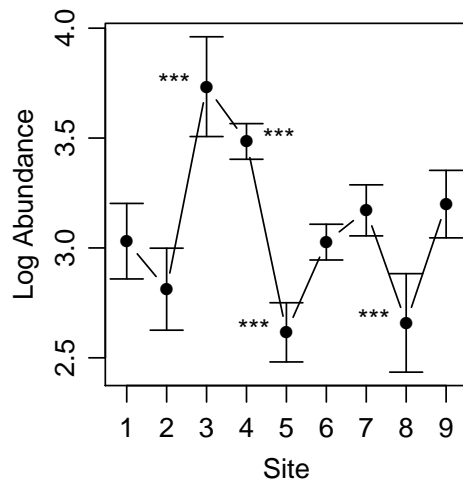
Fit: $lm(\text{formula} = \text{logab} \sim \text{fsite}, \text{data} = \text{ben})$

Linear Hypotheses:

	Estimate	Std. Error	t value	Pr(> t)
2 - 1 == 0	-0.218435	0.096537	-2.263	0.14558
3 - 1 == 0	0.703189	0.096537	7.284	< 0.001
4 - 1 == 0	0.453836	0.096537	4.701	< 0.001
5 - 1 == 0	-0.414859	0.096537	-4.297	< 0.001
6 - 1 == 0	-0.004238	0.096537	-0.044	1.00000
7 - 1 == 0	0.140280	0.096537	1.453	0.57978
8 - 1 == 0	-0.371867	0.096537	-3.852	0.00197
9 - 1 == 0	0.168668	0.096537	1.747	0.37988

(Adjusted p values reported -- single-step method)

```
> fitPlot(lm3,ylab="Log Abundance",xlab="Site",main="")
> addSigLetters(lm3,lets=c("", "", "***", "***", "***", "", "", "***", "" ),pos=c(2,4,2,4,2,2,4,2,4))
```



```
> logdiff <- confint(ben.mc)$confint
> logdiff
```

	Estimate	lwr	upr
2 - 1	-0.21843454	-0.48181178	0.0449427
3 - 1	0.70318863	0.43981139	0.9665659
4 - 1	0.45383639	0.19045915	0.7172136
5 - 1	-0.41485933	-0.67823657	-0.1514821
6 - 1	-0.00423765	-0.26761489	0.2591396
7 - 1	0.14028047	-0.12309677	0.4036577
8 - 1	-0.37186732	-0.63524456	-0.1084901
9 - 1	0.16866808	-0.09470916	0.4320453

```
attr("conf.level")
[1] 0.95
attr("calpha")
[1] 2.728245
attr("error")
[1] 8.127829e-05
```

```
> exp(logdiff)
```


		Estimate	lwr	upr
2	- 1	0.8037761	0.6176633	1.0459679
3	- 1	2.0201841	1.5524144	2.6289010
4	- 1	1.5743404	1.2098050	2.0487168
5	- 1	0.6604332	0.5075112	0.8594333
6	- 1	0.9957713	0.7652024	1.2958147
7	- 1	1.1505965	0.8841781	1.4972914
8	- 1	0.6894457	0.5298059	0.8971878
9	- 1	1.1837272	0.9096375	1.5404049

```

attr("conf.level")
[1] 0.95
attr("calpha")
[1] 2.728245
attr("error")
[1] 8.127829e-05

```