

# Back-Calculation of Previous Length

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# Definition of Back-Calculation

Francis (1990) defined *back-calculation* as,

*“... the dimensions of one or more marks in some hard part of the fish, together with its current body length, are used to estimate its length at the time of formation of each of the marks. ...”*

# Mathematical Definitions

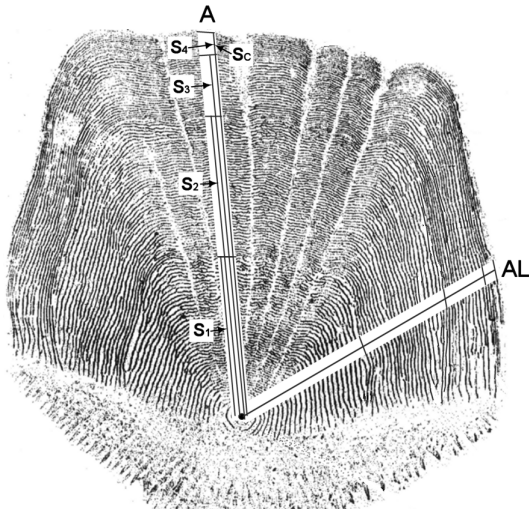
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- Algebraically re-arrange to get simplest back-calculation model.

$$L_i = \frac{S_i}{S_C} L_C$$

# Fraser-Lee (Corrected Direct Proportion) Method

- Derived from “structure grows in direct proportion to the fish length after an initial adjustment for  $L$  when  $S = 0$ .”

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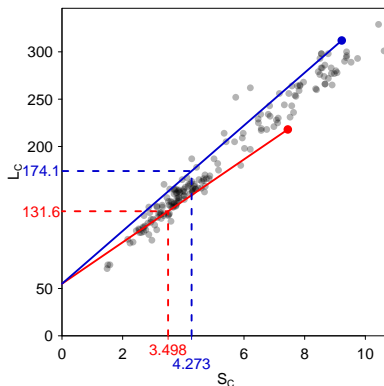
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- $k$  from
  - Known  $L$  when structure forms.
  - Published values (e.g., Carlander (1982)).
  - Intercept of  $L$  on  $S$  regression (i.e.,  $a$ ).

# Fraser-Lee (Corrected Direct Proportion) Method

- Geometrically,  $L_i$  comes from a line between  $(S_C, L_C)$  and  $(0, k)$ .
  - In this example for Walleye,  $k = 55$  as from Carlander (1982).



# References

- Carlander, K. D. 1982. Standard intercepts for calculating lengths from scale measurements for some centrarchid and percid fishes. *Transactions of the American Fisheries Society* 111:332–336.
- Francis, R. 1990. Back-calculation of fish length: a critical review. *Journal of Fish Biology* 36:883–902.