

## Exercise – Simple Linear Regression

Answer the following questions with R code by creating (*and editing if you make a mistake*) an R script and iteratively running the code in RStudio.

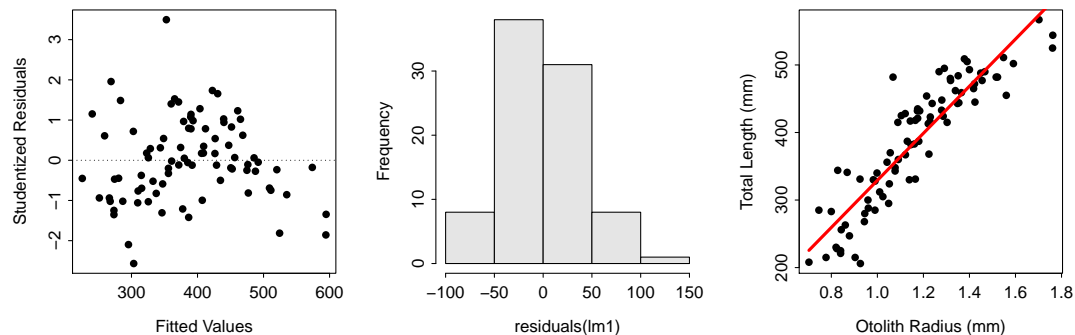
1. Load the data in the **LakeTroutALTER.csv** file into a data frame in R.

```
> setwd("C:/aaaWork/Web/fishR/courses/Vermont2014/CourseMaterial/Exercises")
> lkt <- read.csv("Data/LakeTroutALTER.csv")
> str(lkt)

'data.frame': 86 obs. of 8 variables:
 $ id      : int  18 512 307 52 84 37 80 36 17 59 ...
 $ tl      : int  225 247 256 268 285 288 295 324 328 330 ...
 $ fl      : int  202 226 235 241 262 265 270 295 297 299 ...
 $ sl      : int  185 212 209 228 240 244 243 273 278 280 ...
 $ w       : int   76 138 120 170 185 182 205 275 285 297 ...
 $ otorad : num   0.84 0.879 0.843 0.944 0.99 ...
 $ age     : int   8 6 6 9 7 9 7 10 7 10 ...
 $ sex     : Factor w/ 2 levels "F","M": 1 1 1 1 1 1 1 1 1 1 ...
```

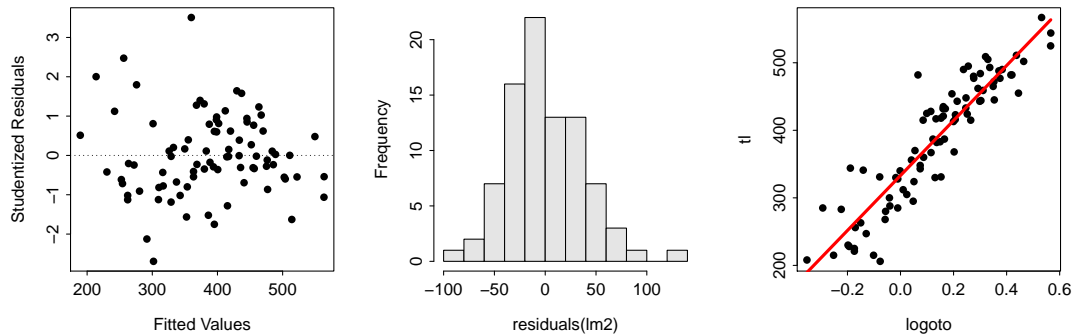
2. Fit the linear model between total length (dependent variable) and otolith radius. Assess the appropriateness of this model.

```
> lm1 <- lm(tl~otorad,data=lkt)
> residPlot(lm1) # Left
> hist(~residuals(lm1)) # Middle
> fitPlot(lm1,ylab="Total Length (mm)",xlab="Otolith Radius (mm)",pch=16) # Right
```



3. Fit the linear model between total length (dependent variable) and the natural log of otolith radius. Assess the appropriateness of this model.

```
> lkt$logoto <- log(lkt$otorad)
> lm2 <- lm(tl~logoto,data=lkt)
> residPlot(lm2)
> hist(~residuals(lm2))
> fitPlot(lm2)
```



4. Answer the following questions with the total length and natural log of otolith radius model.

- (a) Is the relationship between total length and otolith radius significant? How much variability in total length is explained by otolith radius?

```
> summary(lm2)
```

Call:  
lm(formula = tl ~ logoto, data = lkt)

Residuals:

Min	1Q	Median	3Q	Max
-95.87	-22.42	-2.86	23.02	122.15

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	333.07	4.78	69.7	<2e-16
logoto	407.03	19.46	20.9	<2e-16

Residual standard error: 37.3 on 84 degrees of freedom  
Multiple R-squared: 0.839, Adjusted R-squared: 0.837  
F-statistic: 438 on 1 and 84 DF, p-value: <2e-16  
The relationship between total length and log otolith radius is statistically significant ( $p < 0.00005$ ) with 83.9% of the variability in total length explained by log otolith radius.

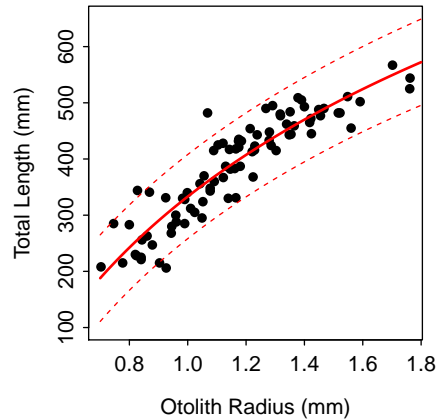
- (b) Predict the total length if the scale radius is 1.2 mm.

```
> ( p1.2 <- predict(lm2,data.frame(logoto=log(1.2)),interval="predict") )
      fit      lwr      upr
1 407.3 332.6 482
```

The predicted total length if the otolith radius is 1.2 mm is between 333 and 482, with a best guess of 407.

- (c) Construct a plot that illustrates the model with prediction intervals on the original scale.

```
> xs <- seq(0.7,1.8,0.01)
> pTL <- predict(lm2,data.frame(logoto=log(xs)),interval="prediction")
> plot(tl~otorad,data=lkt,pch=16,ylim=c(100,650),
       ylab="Total Length (mm)",xlab="Otolith Radius (mm)")
> lines(pTL[, "fit"]~xs,col="red",lwd=2)
> lines(pTL[, "lwr"]~xs,col="red",lty=2)
> lines(pTL[, "upr"]~xs,col="red",lty=2)
```



5. *If time permits ...* fit the length-weight regression for the Lake Trout data.

```
> lkt <- within(lkt,{
  logW <- log(w)
  logTL <- log(tl)
})
> lm3 <- lm(logW~logTL,data=lkt)
> summary(lm3)
```

Call:

```
lm(formula = logW ~ logTL, data = lkt)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.5330	-0.0754	0.0238	0.0684	0.2118

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-12.9744	0.2943	-44.1	<2e-16
logTL	3.2295	0.0496	65.1	<2e-16

Residual standard error: 0.12 on 84 degrees of freedom

Multiple R-squared: 0.981, Adjusted R-squared: 0.98

F-statistic: 4.24e+03 on 1 and 84 DF, p-value: <2e-16

```
> fitPlot(lm3)
```

