AIFFD Chapter 9 - Size Structure

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This document contains R versions of the boxed examples from **Chapter 9** of the "Analysis and Interpretation of Freshwater Fisheries Data" book. Some sections build on descriptions from previous sections, so each section may not stand completely on its own. More thorough discussions of the following items are available in linked vignettes:

- the use of linear models in R in the preliminaries vignette,
- differences between and the use of type-I, II, and III sums-of-squares in the preliminaries vignette, and
- the use of "least-squares means" is found in the preliminaries vignette.

The following additional packages are required to complete all of the examples (with the required functions noted as a comment and also noted in the specific examples below).

```
> library(FSA)  # Summarize, fitPlot, addSigLetters, residPlot
> library(NCStats)  # chisqPostHoc
> library(lattice)  # bwplot, xyplot
> library(multcomp)  # glht, mcp
> library(nlme)  # lme
> library(pgirmess)  # kruskalmc
> library(TeachingDemos)  # chisq.detail
```

In addition, external tab-delimited text files are used to hold the data required for each example. These data are loaded into R in each example with read.table(). Before using read.table() the working directory of R must be set to where these files are located on your computer. The working directory for all data files on my computer is set with

```
> setwd("C:/aaaWork/Web/fishR/BookVignettes/aiffd2007")
```

In addition, I prefer to not show significance stars for hypothesis test output, reduce the margins on plots, alter the axis label positions, and reduce the axis tick length. In addition, contrasts are set in such a manner as to force R output to match SAS output for linear model summaries. All of these options are set with

9.1 Testing for Differences in Mean Length by Means of Analysis of Variance (ANOVA)

9.1.1 Preparing Data

The Box9 1.txt data file is read and the structure is observed below.

```
> d1 <- read.table("data/Box9_1.txt",header=TRUE)
> str(d1)

'data.frame': 360 obs. of 2 variables:
$ lake : Factor w/ 3 levels "Island","Mitchell",..: 1 1 1 1 1 1 1 1 1 1 1 ...
$ length: int 122 126 129 130 130 132 132 135 136 ...
```

9.1.2 ANOVA Results

The one-way ANOVA model is fit in R with lm() where the first argument is a formula of the form response~factor and the data= argument set equal to the data frame containing the variables. The ANOVA table with type I SS is then extracted from the lm object with anova().

```
> lm1 <- lm(length~lake,data=d1)
> anova(lm1)
```

```
Df Sum Sq Mean Sq F value Pr(>F)
lake 2 49324 24662.1 81.73 < 2.2e-16
Residuals 357 107725 301.7
Total 359 157049
```

9.1.3 Multiple Comparisons – Tukey Method

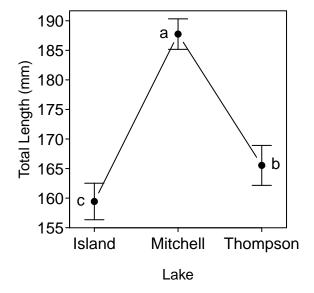
The Tukey multiple comparisons results are obtained by submitting the lm object as the first argument to glht(), from the multcomp package. This function requires a second argument that indicates which type of multiple comparison procedure to use. This second argument uses mcp() which requires the factor variable set equal to the word "Tukey" to perform the Tukey multiple comparison procedure. The saved glht object is submitted to summary() to get the difference in means with a corresponding hypothesis test p-value among each pair of groups and to confint() to get the corresponding confidence intervals for the difference in means. In addition, submitting the saved glht object to cld() will produce "significance letters" to indicate which means are different (different letters mean different means).

```
> mc1 <- glht(lm1,mcp(lake="Tukey"))</pre>
> summary(mc1)
                          Estimate Std. Error t value Pr(>|t|)
Mitchell - Island == 0
                            28.315
                                         2.371
                                                11.944
                                                          <1e-04
                                                          0.0179
Thompson - Island == 0
                             6.105
                                         2.232
                                                 2.735
Thompson - Mitchell == 0
                           -22.210
                                         2.191 -10.138
                                                          <1e-04
> confint(mc1)
                          Estimate lwr
                                             upr
Mitchell - Island == 0
                           28.3151
                                    22.7380
                                              33.8921
Thompson - Island == 0
                            6.1052
                                     0.8540 11.3565
Thompson - Mitchell == 0 -22.2098 -27.3637 -17.0559
> cld(mc1)
```

```
Island Mitchell Thompson
"a" "c" "b"
```

A graphic of the model results is obtained with fitPlot(), from the FSA package, and the significance letters are placed on the means plot with addSigLetters(). (addSigLetters() is from the NCStats package. You should examine the help for this function to see what each of the arguments is used for).

```
> fitPlot(lm1,ylab="Total Length (mm)",xlab="Lake",main="")
> addSigLetters(lm1,lets=c("c","a","b"),pos=c(2,2,4))
```



9.1.4 Summary Table

The summary table shown at the bottom of thebox (I would have preferred doing this at the beginning) is obtained with Summarize() from the FSA package.

> Summarize(length~lake,data=d1,digits=2)

```
lake n mean sd min Q1 median Q3 max percZero
1 Island 104 159.43 15.89 122 149 160 172.2 195 0
2 Mitchell 111 187.75 13.71 145 177 192 197.5 218 0
3 Thompson 145 165.54 20.59 123 150 165 180.0 216 0
```

9.2 Testing for Differences among Length-Frequency Distributions by Means of the Kolmogorov-Smirnov Two-Sample Test

9.2.1 Preparing Data

The Box9_1.txt data file used here is the same file used in Box 9.1 and is not re-read here. However, as the Kolmogorov-Smirnov method described in thebox is a two-sample method. Thus, three new data frames, each of which contains only one of the lakes, must be constructed. This is most easily accomplished with Subset() (from the FSA package) which requires the original data frame as the first argument and a conditioning statement as the second argument.

```
> d1I <- Subset(d1,lake=="Island")  # only Island
> d1M <- Subset(d1,lake=="Mitchell")  # only Mitchell
> d1T <- Subset(d1,lake=="Thompson")  # only Thompson</pre>
```

9.2.2 Kolmogorov-Smirnov Tests

The Kolmogorov-Smirnov Test is performed in R with ks.test(). This function requires the quantitative variable from one "group" (i.e., lake) as the first argument and the quantitative variable from the second "group" as the second argument. The Komogorov-Smirnov results in the same order as presented in thebox are shown below. You will notice that R gives a warning about computing p-values because the Kolmogorov-Smirnov Test is used to compare two *continuous* distributions in which it would theoretically be impossible to have tied values. The discrete nature of length measurements violates this assumption.

```
> ks.test(d1M$length,d1T$length)
Warning in ks.test(d1M$length, d1T$length): p-value will be approximate in the presence of ties

Two-sample Kolmogorov-Smirnov test with d1M$length and d1T$length
D = 0.5306, p-value = 8.882e-16
alternative hypothesis: two-sided
> ks.test(d1I$length,d1T$length)
```

```
Warning in ks.test(d1I$length, d1T$length): p-value will be approximate in the presence of ties

Two-sample Kolmogorov-Smirnov test with d1I$length and d1T$length

D = 0.1565, p-value = 0.1029

alternative hypothesis: two-sided
```

> ks.test(d1I\$length,d1M\$length)

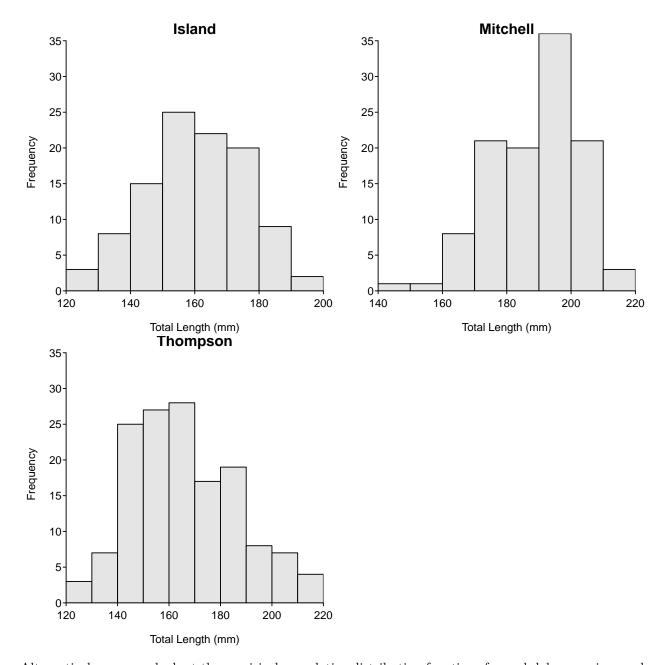
Warning in ks.test(d1I θ): p-value will be approximate in the presence of ties

Two-sample Kolmogorov-Smirnov test with d1I\$length and d1M\$length D = 0.6498, p-value < 2.2e-16 alternative hypothesis: two-sided

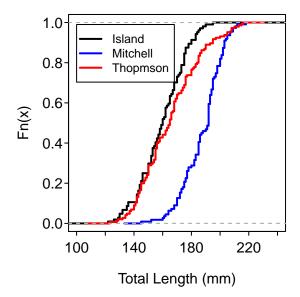
9.2.3 Length Frequency Histograms

Given that the test above is attempting to compare the *distribution* of lengths among the three lakes it would be a good idea to look at these distributions. Histograms for each lake can be easily constructed with a formula in hist() as illustrated below.

> hist(length~lake,data=d1,xlab="Total Length (mm)")



Alternatively, one can look at the empirical cumulative distribution functions for each lake superimposed upon each other. The <code>ecdf()</code> function is used to find the empirical cumulative distribution function and <code>add=TRUE</code> is used to superimpose a subsequent plot on a previous plot.



9.3 Testing for Differences among Length-Frequency Distributions by Means of the Kruskal-Wallis Test

9.3.1 Preparing Data

The Box9 1.txt data file used here is the same file used in Box 9.1 and is not re-read here.

9.3.2 Kruskal-Wallis Test

The Kruskal-Wallis Test is performed in R with kruskal.test(). This function requires the response variable as the first argument and the grouping factor variable as the second argument.

> kruskal.test(d1\$length,d1\$lake)

```
Kruskal-Wallis rank sum test with d1$length and d1$lake
Kruskal-Wallis chi-squared = 118.5671, df = 2, p-value < 2.2e-16</pre>
```

Histograms for each lake should be constructed as shown in Box 9.2.

9.4 Performing Multiple Comparisons of Length-Frequency Data

As a continuation of Box 9.3, multiple comparisons following the significant Kruskal-Wallis test can be easily computed with kruskalmc(), from the pgirmess package. This function requires the *response* variable as the first argument and the factor variable as the second argument.

> kruskalmc(d1\$length,d1\$lake)

Multiple comparison test after Kruskal-Wallis p.value: 0.05 Comparisons

obs.dif critical.dif difference

Island-Mitchell	143.47375	33.99975	TRUE
Island-Thompson	28.70153	32.01354	FALSE
Mitchell-Thompson	114.77223	31.42022	TRUE

9.5 Using Contingency Tables to Test for Differences in Length-Frequency Distributions

9.5.1 Preparing Data

As the data are presented in summarized form, it is easiest to just enter them directly into an R matrix. Doing this requires matrix() with a list of the values as the first argument, the nrow= argument to indicate the number of rows in the matrix, and the byrow=TRUE argument to tell R that the values should be placed in the matrix by rows and then by columns. The columns and rows can be named with colnames() and rownames() respectively.

```
> d5 <- matrix(c(85,77,44,124,34,251),nrow=3,byrow=TRUE)
> colnames(d5) <- c("Q","S-Q")
> rownames(d5) <- c("1996","1997","1998")
> d5
```

```
Q S-Q
1996 85 77
1997 44 124
1998 34 251
```

9.5.2 Chi-Square Test I

Chi-square tests are performed in R with chisq.test(). For this analysis, this function requires a matrix of the data as the only argument. The expected values and residuals $(\frac{observed-expected}{\sqrt{expected}})$ are obtained by appending \$expected and \$residuals to the saved chisq.test object.

```
> ( chi1 <- chisq.test(d5) )</pre>
```

```
Pearson's Chi-squared test with d5
X-squared = 87.154, df = 2, p-value < 2.2e-16
```

> chi1\$expected

```
Q S-Q
1996 42.93659 119.0634
1997 44.52683 123.4732
1998 75.53659 209.4634
```

> chi1\$residuals

```
Q S-Q
1996 6.41934584 -3.85491990
1997 -0.07895125 0.04741149
1998 -4.77916601 2.86996567
```

The final test statistic and p-value, cell contributions to the chi-square test statistic, and a combined table of observed and expected values can also be constructed with chisq.detail(), from the TeachingDemos package.

> chisq.detail(d5)

observed expected

```
S-Q Total
1996
       85
              77
                       162
       42.94 119.06
1997
       44
             124
                       168
       44.53 123.47
1998
       34
             251
                       285
       75.54 209.46
Total 163
             452
                       615
Cell Contributions
               S-0
         Q
1996 41.21 + 14.86 +
1997 0.01 + 0.00 +
1998 22.84 + 8.24 = 87.15
df = 2 P-value = 0
```

9.5.3 Chi-Square Tests II

The authors of the box discuss but do not show the 2x2 chi-square tests used to identify differences between pairs of years. These three tests can be constructed with chisqPostHoc(), from the NCStats package. This function requires the saved chisq.test() object as the first argument and a method to use for adjusting p-values for inflation due to multiple comparisons in the control= argument (see ?p.adjust for more discussion on the different methods for controlling the error rate with multiple comparisons). Finally, if the populations or groups to be compared were not in the rows of the original observed table (the groups in this example, i.e., the years, do form the rows so this argument is not required) then use the popsInRows=FALSE argument. The results below indicate that the PSD differs significantly among all years in the study.

```
> chisqPostHoc(chi1,digits=6)
```

Adjusted p-values used the fdr method.

```
comparison raw.p adj.p
1 1996 vs. 1997 0.000002 0.000003
2 1996 vs. 1998 0.000000 0.000000
3 1997 vs. 1998 0.000174 0.000174
```

9.6 Testing for Differences in Size Structure by Treating Groups of Fish Caught in Each Unit of Effort as Samples

9.6.1 Preparing Data

The Box9_6.txt data file is read and the structure is observed below. The authors create a new variable, LOGIT, that is the log of the ratio of PREF to QUAL after 0.5 had been added to each value to account for zeroes in the data.

```
METHOD QUAL PREF
                           LOGIT
                   2 -0.3364722
    TOURN
              3
1
2
    TOURN
                   4 -1.8458267
             28
3
    TOURN
             13
                   1 -2.1972246
4
    TOURN
              8
                   0 -2.8332133
5
    TOURN
                  16 -1.3156768
             61
6
    TOURN
             76
                  12 -1.8115621
7
    TOURN
                  10 -1.2992830
             38
8
    TOURN
             49
                  12 -1.3762440
9
                  24 -0.9364934
    TOURN
             62
10
    TOURN
                  10 -1.4213857
             43
                  18 -1.1682056
11
    TOURN
             59
12
    TOURN
             24
                   5 -1.4939250
13
     ELEC
             23
                  12 -0.6312718
14
     ELEC
             22
                   2 -2.1972246
15
     ELEC
             35
                   8 -1.4294665
16
     ELEC
              6
                   2 -0.9555114
17
     ELEC
                   1 -2.0368819
             11
                   7 -0.7259370
18
     ELEC
             15
19
     ELEC
             12
                   3 -1.2729657
20
     ELEC
              9
                   6 -0.3794896
21
     ELEC
                   5 -1.5339304
             25
22
     ELEC
             25
                   8 -1.0986123
23
     ELEC
              9
                   1 -1.8458267
24
     ELEC
              7
                   1 -1.6094379
```

9.6.2 Summary Statistics

The summary statistics of the LOGIT values for each collection type is computed with Summarize() with the first argument containing a formula of the form response~factor and the argument data= set to the data frame containing the variables (these simple statistics are different from what is presented in the box. I do not know why, as the raw data show above and the results of the linear model shown below perfectly match the results in the box).

> Summarize(LOGIT~METHOD,data=d6,digits=4)

```
METHOD n mean sd min Q1 median Q3 max percZero

1 ELEC 12 -1.3097 0.5718 -2.197 -1.669 -1.351 -0.8981 -0.3795 0

2 TOURN 12 -1.5030 0.6294 -2.833 -1.820 -1.399 -1.2670 -0.3365 0
```

9.6.3 Model Fitting

The model fit in the box can be fit in R with lm() using the same formula and data= arguments used in Summarize() as above. The authors used a regression weighted on the number of quality fish collected. These weights are used in lm() by setting the weights= argument to QUAL. The ANOVA table is extracted from the saved lm object with anova().

```
> lm1 <- lm(LOGIT~METHOD,data=d6,weights=QUAL)
> anova(lm1)
```

```
Df Sum Sq Mean Sq F value Pr(>F)
METHOD 1 1.391 1.3908 0.2612 0.6144
Residuals 22 117.151 5.3250
Total 23 118.542
```

9.7 Using Repeated-Measures ANOVA to Test for Size Structure Differences with Time-Dependent Data

9.7.1 Preparing Data

The Box9_7.txt data file is read and the structure is observed below. The level names in sizegrp are observed with levels() and the site and year variables were converted to factors with factor()

The authors then created a new variable, period, that indicates whether the data came from a year prior to implementation of the management regulation (i.e., prior to 1990) or after the implementation. This variable is created by first filling the variable with "APRE" and then replacing this name with "BPOST" for all years after 1990. The new variable is then converted to a factor and the new data frame is viewed to see what was accomplished. Finally, as noted by the authors, all age-0 fish were removed from the analysis (using Subset() and noting that != means "not equals").

```
> d7$period <- "APRE"  # initially fill completely with "APRE"
> d7$period[d7$year>1990] <- "BPOST"  # then replace post-1990 with "BPOST"
> d7$period <- factor(d7$period)  # explicitly make a factor
> view(d7)
```

```
year site sizegrp count fsite fyear period
                                     1988
12
                  slot
                           7
28 1989
                                     1989
                  age0
                           4
                                            APRE
            1
                                  1
198 1993
                                     1993
                                           BPOST
           12
                  slot
                          11
                                 12
204 1994
            2
                           2
                                  2
                                     1994
                                           BPOST
                  slot
218 1994
            7
                   und
                           3
                                  7
                                     1994
                                           BPOST
278 1996
                                     1996
                                           BPOST
                   und
                           3
```

```
> d7a <- Subset(d7,sizegrp!="age0")</pre>
```

This data frame, which has the count "stacked" for both the slot and und group must now be unstacked so that the logit of the ratio of fish in the slot to fish in the undersized category can be computed. The reshape() function is a handy, if not cumbersome, method for converting between the stacked (what reshape() calls "long") format to unstacked (what reshape() calls "wide") format. For our purposes, reshape() requires four arguments:

- data: the data frame to be converted from (note that this is the first argument)
- direction: this is the format to be converted to (i.e., we are converting from "long" to "wide")
- timevar: this is the variable that contains the information on how the "long" data should be split into "wide" data. In this case, we want to have count separated into two columns, one for undersized fish and one for slot length fish.
- idvar: this is the variable or variables that will are repeated in the "long" format and should occur only once in the "wide" format.

Thus, the appropriate reshape() command for this example is shown below with the resulting data frame viewed. Notice that the counts of under- and slot-sized fish are contained in the count.und and count.slot variables for each year, site, and period combination.

```
> d7b <- reshape(d7a,direction="wide",timevar="sizegrp",idvar=c("site","year","fyear","period"))
> view(d7b)
```

```
year site fyear period count.und fsite.und count.slot fsite.slot
41
    1990
             1
                1990
                       APRE
                                      4
55
    1990
            8
                1990
                       APRE
                                      3
                                                8
                                                            2
                                                                        8
57
   1990
                1990
                       APRE
                                     6
                                                9
                                                            1
                                                                        9
85 1991
                1991
                                    12
                                               12
                                                            8
                                                                       12
           12
                      BPOST
173 1995
                1995
                      BPOST
                                      4
                                               10
                                                            3
                                                                       10
           10
195 1996
                1996
                      BPOST
                                     7
                                                9
                                                           11
                                                                        9
```

Finally, the undert, slott, total, and LOGIT variables, as described in the box, are constructed.

```
> d7b$undert <- d7b$count.und+0.5
> d7b$slott <- d7b$count.slot+0.5
> d7b$total <- d7b$undert + d7b$slott
> d7b$LOGIT <- log(d7b$slott/d7b$undert)
> head(d7b)  # first 6 rows
```

```
year site fyear period count.und fsite.und count.slot fsite.slot undert
  1988
           1
               1988
                      APRE
                                    4
                                               1
                                                           1
                                                                             4.5
1
                                                                       1
                                               2
               1988
                      APRE
                                    9
                                                           2
                                                                       2
                                                                             9.5
3
  1988
           2
  1988
               1988
                      APRE
                                   11
                                               3
                                                           1
                                                                       3
                                                                           11.5
5
           3
                                                           7
7
   1988
           4
               1988
                      APRE
                                    8
                                               4
                                                                       4
                                                                            8.5
  1988
           6
              1988
                      APRE
                                   15
                                               6
                                                           2
                                                                       6
                                                                           15.5
9
11 1988
           7
              1988
                      APRE
                                   10
                                               7
                                                           0
                                                                       7
                                                                           10.5
   slott total
                     LOGIT
1
     1.5
             6 -1.0986123
3
             12 -1.3350011
     2.5
5
     1.5
             13 -2.0368819
7
     7.5
             16 -0.1251631
9
     2.5
             18 -1.8245493
     0.5
             11 -3.0445224
11
```

9.7.2 Normality Tests

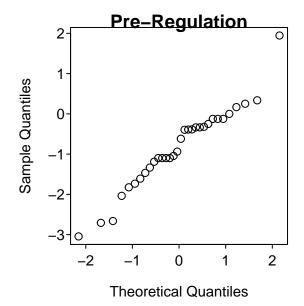
A variety of normality tests are available in R (see Box 3.9 in the Chapter 3 vignette). The Shapiro-Wilks test (the authors of the box refer to a "Wilk's Lambda" test of normality. I do not believe that this is the correct term; Wilk's Lambda is used in multivariate means testing – see this short online article and assume that they mean Shapiro-Wilks normality test) is conducted with shapiro.test(). The only required argument is a vector on which to test normality.

```
> shapiro.test(d7b$LOGIT[d7b$period=="APRE"])
Shapiro-Wilk normality test with d7b$LOGIT[d7b$period == "APRE"]
W = 0.9579, p-value = 0.2402
> shapiro.test(d7b$LOGIT[d7b$period=="BPOST"])
```

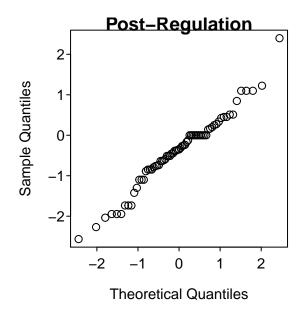
Shapiro-Wilk normality test with d7b\$LOGIT[d7b\$period == "BPOST"] W = 0.9734, p-value = 0.1486

The two normal quantile plots (presumably produced in the SAS program shown in the box) are constructed with qqnorm().

```
> qqnorm(d7b$L0GIT[d7b$period=="APRE"],main="Pre-Regulation")
```



> qqnorm(d7b\$L0GIT[d7b\$period=="BPOST"],main="Post-Regulation")



9.7.3 Repeated Measures ANOVA

THIS SECTION HAS NOT YET BEEN CONVERTED

Reproducibility Information

Compiled Date: Thu May 14 2015 Compiled Time: 5:45:03 PM Code Execution Time: 5.38 s

R Version: R version 3.2.0 (2015-04-16)

```
System: Windows, i386-w64-mingw32/i386 (32-bit)
Base Packages: base, datasets, graphics, grDevices, methods, stats, utils
Required Packages: FSA, NCStats, lattice, multcomp, nlme, pgirmess,
  TeachingDemos and their dependencies (boot, car, codetools, dplyr,
 FSAdata, gdata, gplots, graphics, grDevices, grid, Hmisc, knitr,
 lmtest, mvtnorm, plotrix, relax, rgdal, sandwich, sciplot, sp, spdep,
  splancs, stats, survival, TH.data, utils)
Other Packages: car_2.0-25, FSA_0.6.13, FSAdata_0.1.9, knitr_1.10.5,
  lattice 0.20-31, multcomp 1.4-0, mvtnorm 1.0-2, NCStats 0.4.3,
  nlme_3.1-120, pgirmess_1.6.0, survival_2.38-1, TeachingDemos_2.9,
  TH.data_1.0-6
Loaded-Only Packages: acepack_1.3-3.3, assertthat_0.1, bitops_1.0-6,
  boot_1.3-16, caTools_1.17.1, cluster_2.0.1, coda_0.17-1,
  codetools_0.2-11, colorspace_1.2-6, DBI_0.3.1, deldir_0.1-9,
  digest_0.6.8, dplyr_0.4.1, evaluate_0.7, foreign_0.8-63, formatR_1.2,
 Formula_1.2-1, gdata_2.16.1, ggplot2_1.0.1, gplots_2.17.0, grid_3.2.0,
  gridExtra_0.9.1, gtable_0.1.2, gtools_3.4.2, highr_0.5, Hmisc_3.16-0,
 htmltools 0.2.6, KernSmooth 2.23-14, latticeExtra 0.6-26,
 LearnBayes_2.15, lme4_1.1-7, lmtest_0.9-33, magrittr_1.5, MASS_7.3-40,
 Matrix 1.2-0, mgcv 1.8-6, minqa 1.2.4, munsell 0.4.2, nloptr 1.0.4,
 nnet_7.3-9, parallel_3.2.0, pbkrtest_0.4-2, plotrix_3.5-11, plyr_1.8.2,
 proto_0.3-10, quantreg_5.11, RColorBrewer_1.1-2, Rcpp_0.11.6,
 relax_1.3.15, reshape2_1.4.1, rgdal_0.9-2, rmarkdown_0.6.1,
 rpart_4.1-9, sandwich_2.3-3, scales_0.2.4, sciplot_1.1-0, sp_1.1-0,
 SparseM_1.6, spdep_0.5-88, splancs_2.01-37, splines_3.2.0,
  stringi_0.4-1, stringr_1.0.0, tools_3.2.0, yaml_2.1.13, zoo_1.7-12
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