

## Math 160 Review Sheet for the Final Exam

Date & Time of Final Exam (*You must take the final exam with your own section.*):

Tuesday, May 8 at 9:00 am (*11:00 am section*)

Saturday, May 5 at 7:00 pm (*1:30 pm section*)

Book Sections: 1.1-1.3, 1.5-1.8, 2.1-2.6, 2.8, 3.1-3.5, 3.7, 3.9, 4.1-4.5, 6.1-6.4, Appxs. D, E.

The specific topics are as follows:

1. Domain of a function, vertical line test, linear functions, graphing transformations, composition of functions, piecewise defined functions, trigonometry examples using “useful triangles”. (1.1, 1.2, 1.3, App. D)
2. Different types of limits, including one-sided limits, infinite limits, and limits at infinity. Calculating limits using Limit Laws. Squeeze Theorem. (1.5, 1.6, 3.4)
3. Continuity and types of discontinuities. Intermediate Value Theorem. (1.8)
4. Computing  $f'$  using the definition of derivative. Tangent lines, velocity, and instantaneous rates of change. (2.1, 2.2)
5. Graphing  $f'$  using the graph of  $f$ . Points of non-differentiability. (2.2)
6. Derivative formulas #1-8. (2.3)
7. Derivatives involving trig functions. (2.4)
8. Derivatives using the Chain Rule. (2.5)
9. Implicit differentiation. (2.6)
10. Related Rates. (2.8)
11. Relative maxima/minima and absolute maxima/minima. (3.1)
12. Mean Value Theorem. (3.2)
13. Graphing using the following five steps: I. Find intercepts. II. Find asymptotes. III. Find relative extrema and intervals where increasing/decreasing. IV. Find inflection points and intervals where concave up/down. V. Connect the important points using concavity and intervals of increase/decrease. (3.3-3.5)
14. Optimization (Applied Max/Min) Problems. (3.7)
15. Indefinite integrals using Integration Rules 1-10 and using substitution. (3.9, 4.4, 4.5)
16.  $\Sigma$  notation and properties of sums. (App.E)

17. Connection between the definite integral  $\int_a^b f(x) dx$  and area. (4.1, 4.2)
18. Approximating  $\int_a^b f(x) dx$  by Riemann sums. (4.1, 4.2)
19. Formal definition of  $\int_a^b f(x) dx$  and computing  $\int_a^b f(x) dx$  using the definition. (4.2)
20. Fundamental Theorem of Calculus. (4.3)
21. Definite integrals by substitution. (4.5)
22. Net Change Theorem. (4.4)
23. Relationship between  $\int_a^x f(t) dt$  and  $f(x)$ . (4.3)
24. Comparison Properties of  $\int_a^b f(x) dx$ . (4.2)
25. Symmetry Properties of  $\int_a^b f(x) dx$ . (4.5)
26. Exponential functions and the definition of  $e$ . Derivatives and integrals of functions involving  $e^x$ . (6.2)
27. One-to-one functions and their inverse functions. (6.1)
28. Relationships between logarithmic and exponential functions. (6.3)
29. Logarithmic differentiation. Derivative of general exponential functions and general logarithmic functions. Integration rule:  $\int \frac{1}{x} dx = \ln |x| + C$ . (6.4)
30. I will ask you to prove that  $e = \lim_{n \rightarrow \infty} (1 + \frac{1}{n})^n$  using the fact that  $\frac{d}{dx} \ln x = \frac{1}{x}$ . (6.4)
31. Formal definition of limit. (1.7)