

(6.9)

$$TC = 1000 + 2X$$

$X$  = number of units produced

$$E(X) = 500$$

$$V(X) = 900$$

$$E(TC) = E(1000) + 2E(X)$$

$$= 1000 + 2(500) = 2000$$

$$V(TC) = V(1000) + 4V(X)$$

$$= 0 + 4(900) = 3600$$

(6.10)

$$\Pi = 1000 - 2X$$

$$E(X) = 50$$

$X$  = number of units

$$V(X) = 90$$

produced

$$E(\Pi) = E(1000) - 2E(X)$$

$$= 1000 - 2(50) = 900$$

$$V(\Pi) = V(1000) + 4V(X)$$

$$= 0 + 4(90) = 360$$

(6.11)

$$\Pi = 2000 - 2X$$

$$E(X) = 500$$

$X$  = number of units

$$V(X) = 900$$

produced

$$E(\Pi) = E(2000) - 2E(X) = 2000 - 2(500) = 1000$$

$$V(\Pi) = V(2000) + 4V(X) = 0 + 4(900) = 3600$$

$$(6.12) \quad \Pi = 6000 - 3X \quad E(X) = 1000$$

$$V(X) = 900$$

$$E(\Pi) = E(6000) - 3E(X) = 6000 - 3(1000) = 3000$$

$$V(\Pi) = V(6000) + 9V(X) = 0 + 9(900) = 8100$$

$$(6.13) \quad P = 10,000 + 1.5X \quad E(X) = 30,000$$

$$S(X) = 8,000$$

$$E(P) = 10,000 + 1.5E(X) = 10,000 + 1.5(30,000)$$

$$= 10,000 + 45,000 = 55,000$$

$$V(P) = 0 + (1.5)^2 V(X) = 2.25(64,000,000)$$

$$= 144,000,000$$

$$S(P) = \sqrt{144,000,000} = 12,000.$$

$$(6.14) \quad TC = 20 + X \quad E(X) = 4 \quad E(TC) = -10E(TC)$$

$$S(X) = 1$$

$$\Pi = B - TC \quad E(TC) = 20 + E(X)$$

$$E(\Pi) = B - E(TC) \quad = 20 + 4 = 24$$

$$-10E(TC) = B - E(TC) \quad \text{Then } 1.1(24) = B$$

$$1.1E(TC) = B \quad 26.4 = B$$

$$V(\pi) = V(B) + V(TC) \quad \text{where } V(B) = 0 \quad (B \text{ is const.})$$

$$\left. \begin{aligned} & V(TC) = V(zo) + V(x) \\ & = 0 + 1 = 1 \end{aligned} \right\}$$

$$S(\pi) = \sqrt{1} = 1$$

6.15

$$W = 60 + (-.20)M \quad E(M) = 700$$

$$S(M) = 130$$

$$\begin{aligned} E(W) &= 60 + (.20)E(M) \\ &= 60 + (.20)(700) = 60 + 140 = 200 \end{aligned}$$

$$V(W) = 0 + (-.20)^2 V(M) = (-.04)(130)^2 = 676$$

$$S(W) = 26.$$

6.16

$$S = 6000 + (-.08)O \quad E(O) = 600,000$$

$$S(O) = 180,000$$

$$\begin{aligned} E(S) &= 6000 + (.08)E(O) = 6000 + (.08)600,000 = 6000 + 48000 \\ &= 54,000. \end{aligned}$$

$$V(S) = 0 + (-.08)^2 V(O) = -.0064(180,000)^2 = 207360000$$

$$S(S) = \sqrt{207360000} = 14,400$$



$$V(\pi) = V(B) + V(TC)$$

where  $V(B) = 0$  ( $B$  is const.)

$$V(TC) = V(20) + V(x)$$

$$= 0 + 1 = 1$$

$$\approx 0 + 1$$

$$S(\pi) = \sqrt{1} = 1$$

$$(6.15) \quad W = 60 + (-.20)M \quad E(W) = 700$$

$$S(M) = 130$$

$$E(W) = 60 + (.20)E(M)$$

$$= 60 + (.20)(700) = 60 + 140 = 200$$

$$V(W) = 0 + (-.20)^2 V(M) = (-.04)(130)^2 = 676$$

$$S(W) = 26$$

$$(6.16) \quad S = 6000 + (-.08)O \quad E(O) = 600,000$$

$$S(O) = 180,000$$

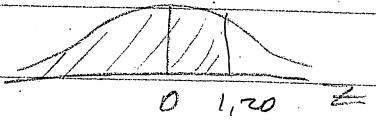
$$E(S) = 6000 + (.08)E(O) = 6000 + (.08)(600,000) = 6000 + 48000$$

$$= 54,000$$

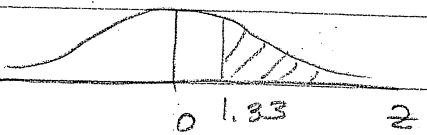
$$V(S) = 0 + (.08)^2 V(O) = -.0064(180,000)^2 = 207360000$$

$$S(S) = \sqrt{207360000} = 14,400$$

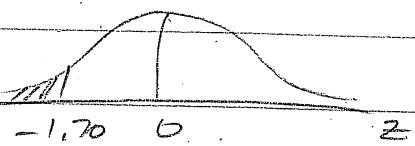
(b) a.  $P(z < 1.20) = .8849$



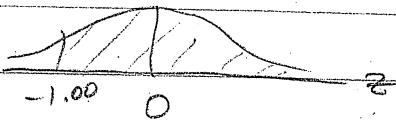
b.  $P(z > 1.33) = 1 - P(z < 1.33)$   
 $= 1 - .9082 = .0918$



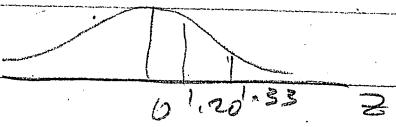
c.  $P(z < -1.70) = P(z > 1.70)$   
 $= 1 - P(z < 1.70)$   
 $= 1 - .9554 = .0446$



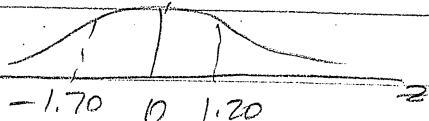
d.  $P(z > -1.00) = P(z < 1.00)$   
 $= .8413$



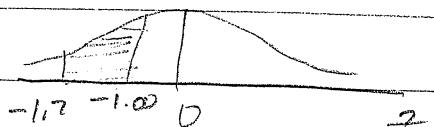
e.  $P(1.20 < z < 1.33)$   
 $= P(z < 1.33) - P(z < 1.20)$   
 $= .9082 - .8849 = .0233$



f.  $P(-1.70 < z < 1.20)$   
 $= P(z < 1.20) - P(z < -1.70)$   
 $= .8849 - .0446 = .8403$

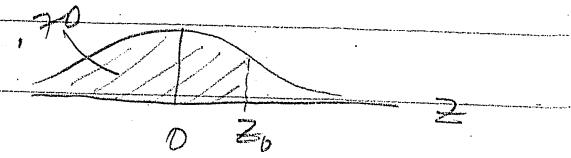


g.  $P(-1.70 < z < -1.00)$   
 $= P(z < -1.00) - P(z < -1.70) = .1587 - .0446 = .1141$



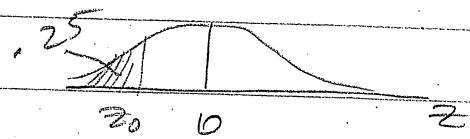
(6.18) a.  $P(Z < z_0) = .70$

$z_0 = .52$



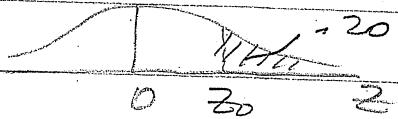
b.  $P(Z < z_0) = .25$

$z_0 = -.67$



c.  $P(Z > z_0) = .20$

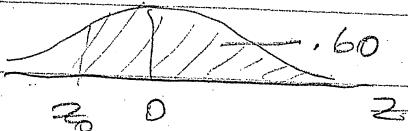
$z_0 = .84$



d.  $P(Z > z_0) = .60$

$P(Z < z_0) = .40$

$z_0 = -.25$



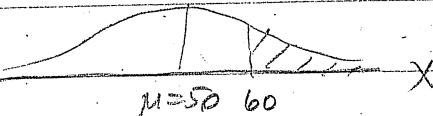
$$(6.19) \quad \mu = 50 \quad \sigma^2 = 64$$

$$a. P(X > 60) = P(Z > \frac{60-50}{8})$$

$$= P(Z > \frac{10}{8}) = P(Z > 1.25)$$

$$= 1 - P(Z < 1.25) = 1 - .8944$$

$$= .1056$$



$$\mu = 50$$

$$60$$

$$0$$

$$1.25$$

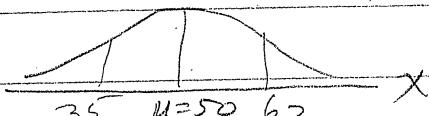
$$b. P(35 < X < 62)$$

$$= P\left(\frac{35-50}{8} < Z < \frac{62-50}{8}\right)$$

$$= P(-1.88 < Z < 1.5)$$

$$= P(Z < 1.5) - P(Z < -1.88)$$

$$= .9332 - .0301 = .9031$$

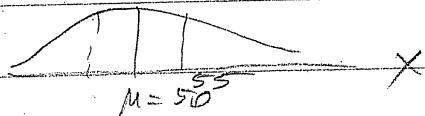


$$35 \quad \mu = 50 \quad 62$$

$$-1.88 \quad 0 \quad 1.5$$

$$c. P(X < 55) = P(Z < \frac{55-50}{8})$$

$$= P(Z < .63) = .7357$$



$$\mu = 50$$

$$55$$

$$0.63$$

$$d. P(X > x_0) = .20$$

$$P(Z > z_0) = .20$$

$$P(Z < z_0) = .80$$

$$z_0 = .84$$

$$x_0 = (.84)(8) + 50 = 56.72$$



$$x_0$$

$$50$$

$$.84$$

$$0 \quad z_0$$

c.  $P(X_1 < X < X_2) = .05$

$P(X < X_1) = .475$

$P(Z < Z_1) = .475$

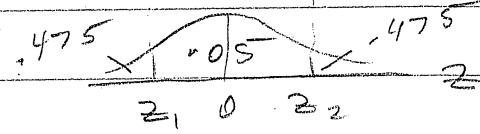
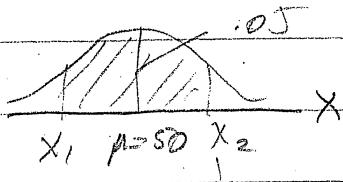
$Z_1 = -.06$

$X_1 = (-.06)(8) + 50 = 49.52$

$P(Z < Z_2) = .525$

$Z_2 = .06$

$X_2 = (.06)(8) + 50 = 50.48$



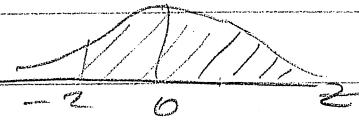
6-20

$\mu = 80 \quad \sigma^2 = 100$

a.  $P(X > 60) = P(Z > \frac{60-80}{10})$

$= P(Z > -2) = 1 - P(Z < -2)$

$= 1 - .0228 = .9772$

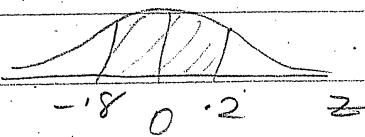


b.  $P(72 < X < 82)$

$= P\left(\frac{72-80}{10} < Z < \frac{82-80}{10}\right)$

$= P(-.8 < Z < .2)$

$= P(Z < .2) - P(Z < -.8) = .5793 - .2119 = .3674$

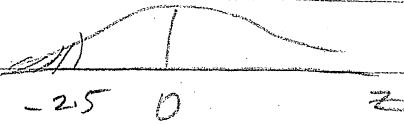


$$c. P(X < 55)$$

$$= P\left(Z < \frac{55-80}{10}\right)$$

$$= P(Z < -2.5)$$

$$= .0062$$



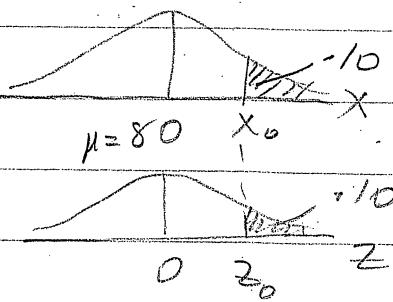
$$d. P(X > X_0) = .10$$

$$P(Z > Z_0) = .10$$

$$P(Z < Z_0) = .90$$

$$Z_0 = 1.28$$

$$X_0 = (1.28)(10) + 80 = 92.80$$



$$e. P(X_1 < X < X_2) = .08$$

$$P(X < X_1) = .46$$

$$P(Z < Z_1) = .46$$

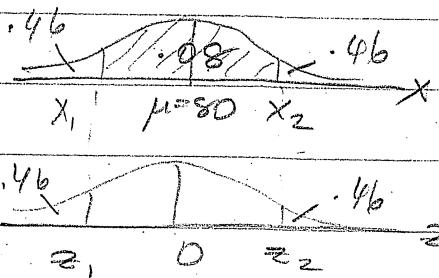
$$Z_1 = -.10$$

$$X_1 = (-.10)(10) + 80 = 79$$

$$P(Z < Z_2) = .54$$

$$Z_2 = .10$$

$$X_2 = (.10)(10) + 80 = 81$$

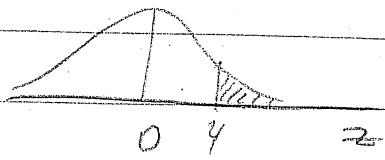


(6.21)

$$\mu = .2 \quad \sigma^2 = .0025$$

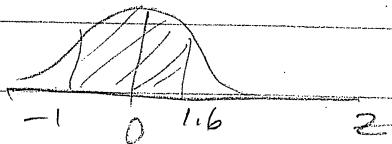
$$\sigma = .05$$

$$a. P(X > .4) = P(Z > \frac{.4 - .2}{.05}) \\ = P(Z > 4) = 0$$



$$b. P(.15 < X < .28)$$

$$= P\left(\frac{.15 - .2}{.05} < Z < \frac{.28 - .2}{.05}\right)$$



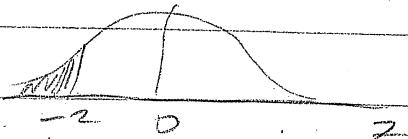
$$= P(-1 < Z < 1.6) = P(Z < 1.6) - P(Z < -1)$$

$$= .9452 - .1587 = .7865$$

$$c. P(X < .10) = P(Z < \frac{.10 - .2}{.05})$$

$$= P(Z < -2)$$

$$= .0228$$



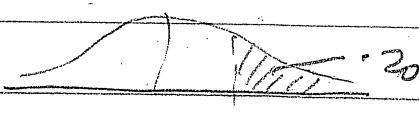
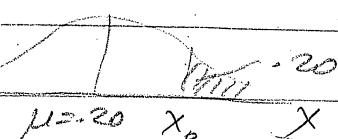
$$d. P(X > X_0) = .20$$

$$P(Z > Z_0) = .20$$

$$P(Z < Z_0) = .80$$

$$Z_0 = .84$$

$$X_0 = (.84)(.05) + .20 = .242$$



c.  $P(X_1 < X < X_2) = .05$

$P(Z_1 < Z < Z_2) = .05$

$P(Z < Z_1) = .475$

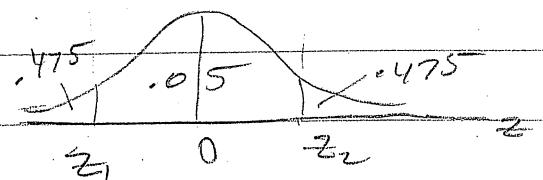
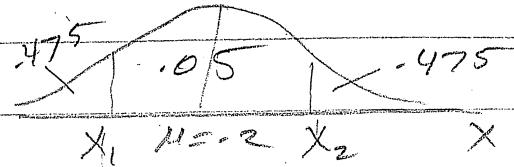
$Z_1 = -.06$

$X_1 = (-.06)(.05) + .20 = .197$

$P(Z < Z_2) = .525$

$Z_2 = .06$

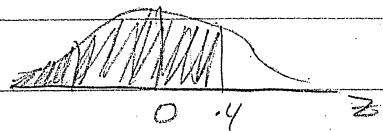
$X_2 = (-.06)(.05) + .20 = .203$



(6.22)

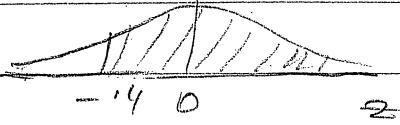
$\mu = 380 \quad \sigma = 50$

a.  $P(X < 400) = P(Z < \frac{400-380}{50})$



$= P(Z < 0.4) = .6554$

b.  $P(X > 360) = P(Z > \frac{360-380}{50})$



$= 1 - P(Z > -0.4) = 1 - .3446 = .6554$

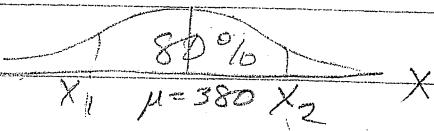
c. See pic's

d.  $P(300 < X < 400) = P\left(\frac{300-380}{50} < Z < \frac{400-380}{50}\right)$

$= P(-1.6 < Z < 0.4) = P(Z < 0.4) - P(Z < -1.6)$

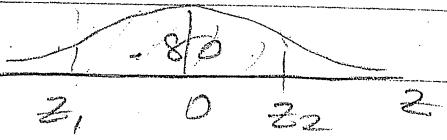
$= .6554 - .0548 = .6006$

$$e. P(X_1 < X < X_2) = .80$$



$$= P(Z_1 < Z < Z_2) = .80$$

$$P(Z < z_1) = .10$$



$$z_1 = -1.28$$

$$z_1 \quad 0 \quad z_2 \quad z$$

$$X_1 = (-1.28)(50) + 380$$

$$= 316$$

$$P(Z < z_2) = .90$$

$$z_2 = 1.28$$

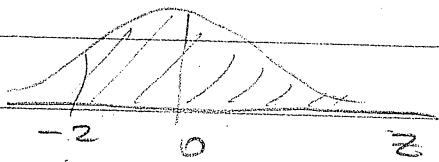
$$X_2 = (1.28)(50) + 380$$

$$= 444$$

6.23

$$\mu = 1200 \quad \sigma = 100$$

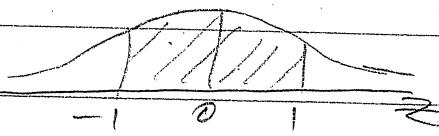
$$a. P(X > 1000) = P(Z > \frac{1000 - 1200}{100})$$



$$= P(Z > -2) = P(Z < 2)$$

$$= .9772$$

$$b. P(1100 < X < 1300)$$

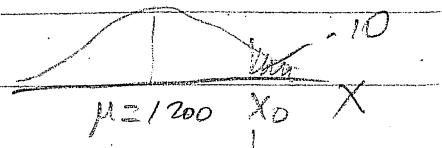


$$= P(\frac{1100 - 1200}{100} < Z < \frac{1300 - 1200}{100})$$

$$= P(-1 < Z < 1) = P(Z < 1) - P(Z < -1) = .8413 - .1587$$

$$= .6826$$

$$c. P(X > X_0) = .10$$

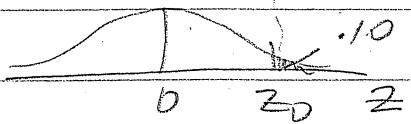


$$P(Z > Z_0) = .10$$

$$P(Z < Z_0) = .90$$

$$Z_0 = 1.28$$

$$X_0 = (1.28)(100) + 1200 = 1328$$



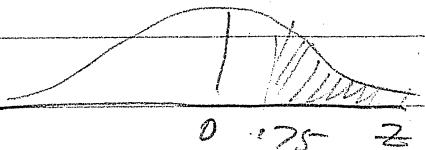
(6.24)  $\mu = 35,000 \quad \sigma = 4000$

$$a. P(X > 38,000)$$

$$= P\left(Z > \frac{38,000 - 35,000}{4000}\right)$$

$$= P(Z > .75) = 1 - P(Z < .75)$$

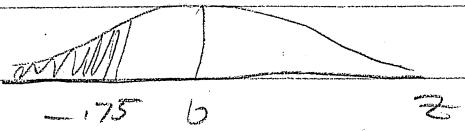
$$= 1 - .7734 = .2266$$



$$b. P(X < 32,000)$$

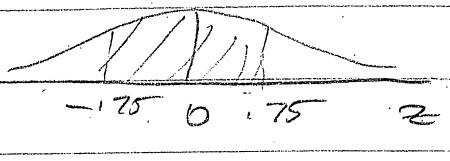
$$= P\left(Z < \frac{32,000 - 35,000}{4000}\right)$$

$$= P(Z < -.75) = .2266$$



$$c. P(32,000 < X < 38000)$$

$$= P\left(\frac{32000 - 35000}{4000} < Z < \frac{38000 - 35000}{4000}\right) = P(-0.75 < Z < 0.75)$$



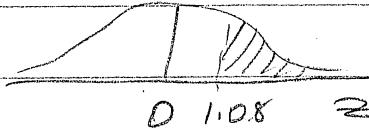
$$= P(-0.75 < Z < 0.75)$$

$$= P(Z < 0.75) - P(Z < -0.75) = .7734 - .2266 = .5468$$

(6.25)

$$\mu = 12.2 \quad \sigma = 7.2$$

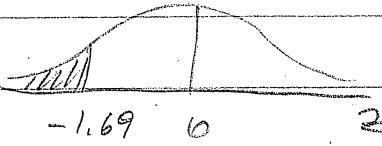
$$a. P(X > 20) = P\left(Z > \frac{20 - 12.2}{7.2}\right)$$



$$= P\left(Z > \frac{7.8}{7.2}\right) = P(Z > 1.08)$$

$$= 1 - .8599 = .1401$$

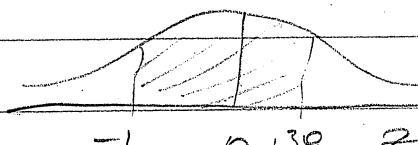
$$b. P(X < 0) = P\left(Z < \frac{0 - 12.2}{7.2}\right)$$



$$= P(Z < -1.69) = .0455$$

$$c. P(5 < X < 15) = P\left(\frac{5 - 12.2}{7.2} < Z < \frac{15 - 12.2}{7.2}\right)$$

$$= P(-1 < Z < 0.39)$$



$$= P(Z < 0.39) - P(Z < -1)$$

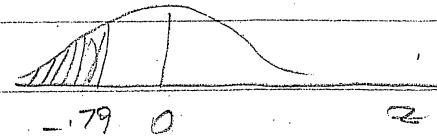
$$= .6517 - .1587$$

$$= .493$$

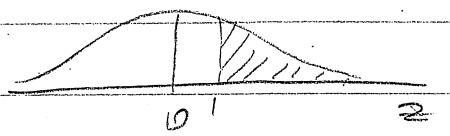
6.2b

$$\mu = 12.2 \quad \sigma = 2.8$$

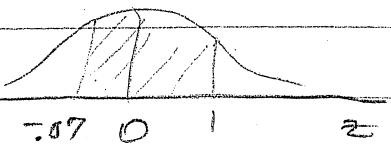
$$\begin{aligned} a. \quad P(X < 10) &= P\left(Z < \frac{10-12.2}{2.8}\right) \\ &= P(Z < -0.79) = .2148 \end{aligned}$$



$$\begin{aligned} b. \quad P(X > 15) &= P\left(Z > \frac{15-12.2}{2.8}\right) \\ &= P(Z > 1) \\ &= 1 - P(Z < 1) = 1 - .8413 = .1587 \end{aligned}$$



$$\begin{aligned} c. \quad P(12 < X < 15) &= P\left(\frac{12-12.2}{2.8} < Z < \frac{15-12.2}{2.8}\right) \\ &= P(-0.07 < Z < 1) \\ &= P(Z < 1) - P(Z < -0.07) \\ &= .8413 - .4772 = .3692 \end{aligned}$$



6.27

$$\mu = 500,000 \quad \sigma = 50,000$$

$$460,000 \quad 540,000$$

$$\mu = 500,000$$

a.  $P(460,000 < X < 540,000)$

$$= P\left(\frac{460,000 - 500,000}{50,000} < Z < \frac{540,000 - 500,000}{50,000}\right)$$

$$-1.2 \quad 0 \quad 1.2$$

$$= P(-1.2 < Z < 1.2)$$

$$= P(Z < 1.2) - P(Z < -1.2)$$

$$= .7881 - .2119 = .5762$$

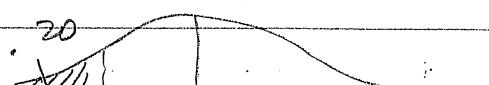
b.  $P(X < X_0) = .20$

$$P(Z < Z_0) = .20$$

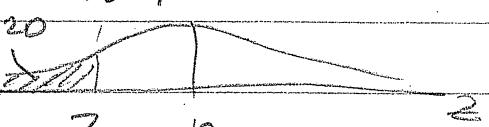
$$Z_0 = -0.84$$

$$X_0 = (-0.84)(50,000) + 500,000$$

$$= 458,000$$



$$X_0 \quad \mu = 500,000$$



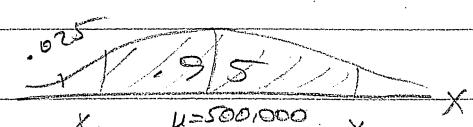
$$Z_0 \quad 0$$

c.  $P(X_1 < X < X_2) = .95$

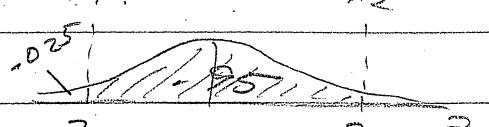
$$P(X < X_1) = .025$$

$$P(Z < Z_1) = .025$$

$$Z_1 = -1.96$$



$$X_1 \quad \mu = 500,000 \quad X_2$$



$$Z_1 \quad 0 \quad Z_2 \quad Z$$

$$X_1 = (-1.96)(50,000) + 500,000$$

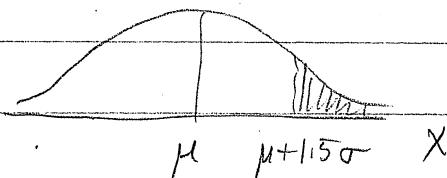
$$= 402,000$$

$$P(Z < z_1) = .975$$

$$z_1 = 1.96$$

$$X_1 = (1.96)(50,000) + 500,000 = 598,000$$

6.28



$$x = \mu + 1.5\sigma$$

$$z = \frac{x - \mu}{\sigma} = \frac{\mu + 1.5\sigma - \mu}{\sigma} = 1.5$$

$$\begin{aligned} P(Z > 1.5) &= 1 - P(Z < 1.5) \\ &= 1 - .9332 \end{aligned}$$

$$= .0668$$

6.29

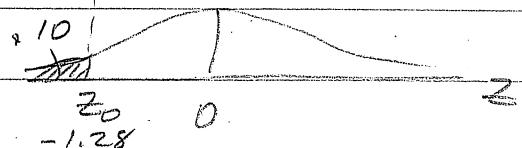
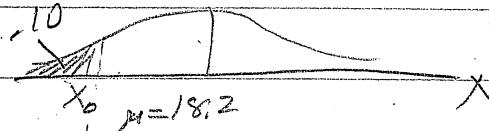
$$\mu = 18.2 \quad \sigma = 1.6$$

$$P(X < x_0) = .10$$

$$P(Z < z_0) = .10$$

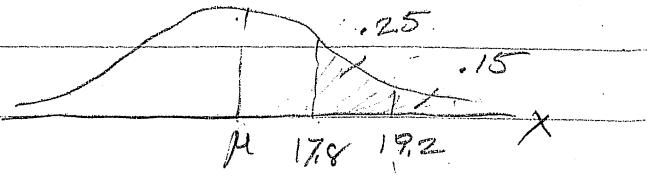
$$z_0 = -1.28$$

$$x_0 = (-1.28)(1.6) + 18.2 = 16.15$$



$$6.30 \quad P(X > 17.8) = .25$$

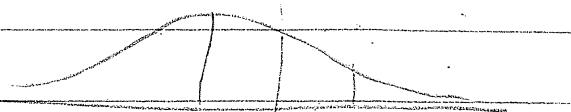
$$P(X > 19.2) = .15$$



$$\mu = ? \quad \sigma = ?$$

$$P(Z < z_1) = .75$$

$$z_1 = \frac{17.8 - \mu}{\sigma} = .67 \Rightarrow 17.8 = .67\sigma + \mu \quad (1)$$



$$P(Z < z_2) = .85$$

$$z_2 = \frac{19.2 - \mu}{\sigma} = 1.04 \Rightarrow 19.2 = 1.04\sigma + \mu \quad (2)$$

Solve simultaneously equations (1) + (2) for  $\mu + \sigma$

$$\text{From (1)} \quad \mu = 17.8 - .67\sigma$$

$$\text{Sub. into (2)} \quad 19.2 = 1.04\sigma + 17.8 - .67\sigma$$

$$19.2 - 17.8 = .37\sigma$$

$$1.4 = .37\sigma$$

$$\frac{1.4}{.37} = \sigma$$

$$\sigma = 3.78 \quad \boxed{\sigma^2 = 14.32}$$

$$\text{Then } \mu = 17.8 - .67(6) = 17.8 - .67(3.78)$$

$$\mu = 17.8 - 2.53$$

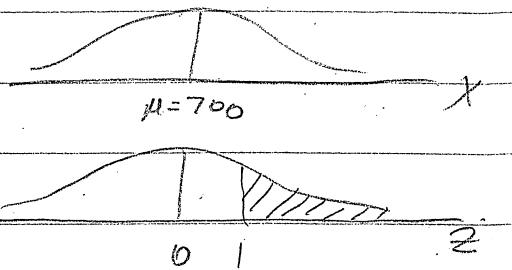
$$\boxed{\mu = 15.26}$$

(6.31)  $\mu = 700 \quad \sigma = 120$

$$a. P(X > 820) = P\left(z > \frac{820 - 700}{120}\right)$$

$$= P(z > 1) = 1 - P(z < 1)$$

$$= 1 - .8413 = .1587$$

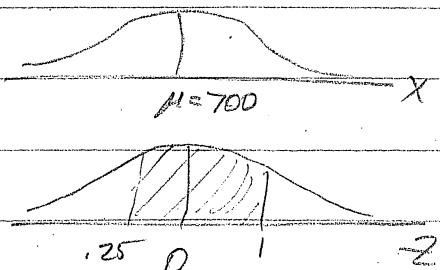


b.  $P(730 < X < 820)$

$$= P\left(\frac{730 - 700}{120} < z < \frac{820 - 700}{120}\right)$$

$$= P(.25 < z < 1)$$

$$= P(z < 1) - P(z < .25)$$



$$= .8413 - .5987 = .2426 \quad \text{prob. any one student gets a B.}$$

$E(X) = n P(x) = 100 (.2426) = 24.26$  average number of  
B's in 100 students.

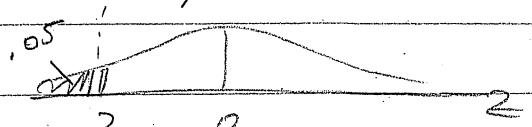
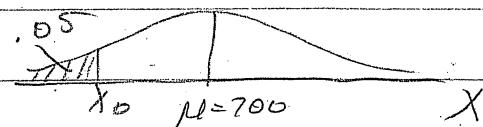
c.  $P(X < x_0) = .05$

$$P(z < z_0) = .05$$

$$z_0 = -1.645$$

$$x_0 = (-1.645)(120) + 700$$

$$= 502.6$$



(6.32)

$$A: P(X \geq 10) = P(Z \geq \frac{10 - 10}{\sqrt{0.12}}) = P(Z \geq -0.33)$$

$$= 1 - P(Z \leq -0.33)$$

$$= 1 - .3707 = .6293$$

$$B: P(X \geq 10) = P(Z \geq \frac{10 - 11}{\sqrt{0.04}}) = P(Z \geq -2.5)$$

$$= 1 - P(Z \leq -2.5)$$

$$= 1 - .4013 = .5987$$

Investment A has higher likelihood of earning at least 10%

(6.33)

$$A: P(X < .05) = P(Z < \frac{.05 - .044}{\sqrt{.004}}) = P(Z < 1.5)$$

$$= .9332$$

$$B: P(X < .05) = P(Z < \frac{.05 - .042}{\sqrt{.006}}) = P(Z < 1.33)$$

$$= .9082$$

Supplier A has more likelihood of less than 5% impurity.

6.34

$$\mu = 150 \quad \sigma = 40$$

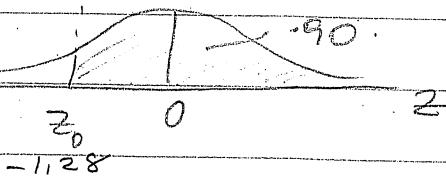
a.  $P(X > X_0) = .90$

$$P(Z > Z_0) = .90$$

$$P(Z < Z_0) = .10$$

$$Z_0 = -1.28$$

$$X_0 = (-1.28)(40) + 150 = 98.80$$

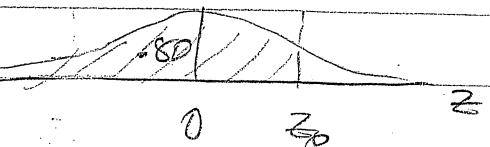
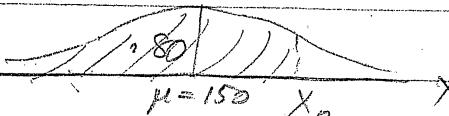


b.  $P(X < X_0) = .80$

$$P(Z < Z_0) = .80$$

$$Z_0 = .84$$

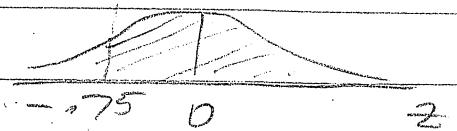
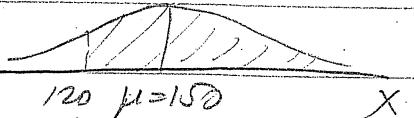
$$X_0 = (.84)(40) + 150 = 183.6$$



c.  $P(X > 120) = P(Z > \frac{120 - 150}{40})$

$$= P(Z > -.75)$$

$$= P(Z < .75) = .7734$$



$$P(\text{at least one student}) = P(\text{only one student}) - P(\text{both students})$$

$$= 2(.7734) - (.7734)^2$$

$$= 1.5468 - .5981$$

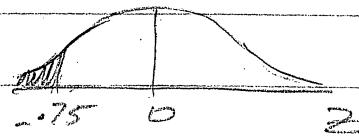
$$= .9487$$

6.35

$$\mu = 75 \quad \sigma = 20$$

$$a. P(X < 60) = P\left(Z < \frac{60-75}{20}\right)$$

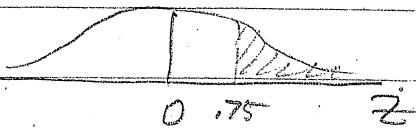
$$= P(Z < -0.75) = .2266$$



$$b. P(X > 90) = P\left(Z > \frac{90-75}{20}\right)$$

$$= P(Z > 0.75)$$

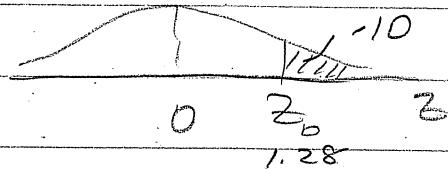
$$= 1 - P(Z < 0.75) = 1 - .7734 = .2266$$



$$d. P(X > X_0) = .10$$

$$P(Z > Z_0) = .10$$

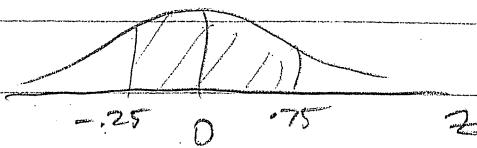
$$Z_0 = 1.28$$



$$X_0 = (1.28)(20) + 75 = 25.6 + 75 = 100.60$$

(6.3b)

$$\mu = 420 \quad \sigma = 80$$



a.  $P(400 < X < 480)$

$$= P\left(\frac{400-420}{80} < z < \frac{480-420}{80}\right)$$

$$= P(-0.25 < z < 0.75) = P(z < 0.75) - P(z < -0.25)$$

$$= .7734 - .4013 = .3721$$

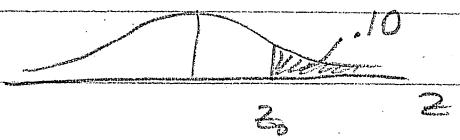
b.  $P(X > X_0) = .10$

$$P(z > z_0) = .10$$

$$P(z < z_0) = .90$$

$$z_0 = 1.28$$

$$X_0 = (1.28)(80) + 420 = 102.4 + 420 = 522.4$$



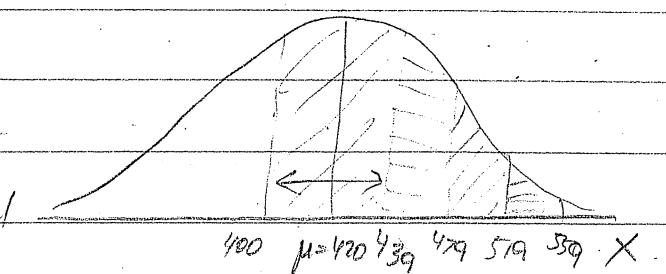
c.

400 - 439 has highest

probability of an individual

being in this range.

because this range has largest area under the curve.

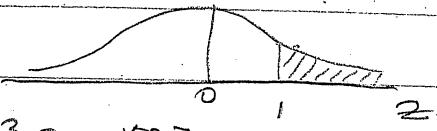


$$400 \quad \mu = 439 \quad 479 \quad 519 \quad 559 \quad x$$

d. 520 - 559 is the least likely range.

$$c. P(X > 500) = P(z > \frac{500 - 420}{80})$$

$$= P(z > 1) = 1 - P(z < 1) = 1 - .8413 = .1587$$



probability of any one  
person's score exceeding  
500.

$$P(\text{at least one of two}) = P(\text{one}) + P(\text{the other one}) - P(\text{both})$$

$$= .1587 + .1587 - (.1587)^2$$

$$= .2922$$

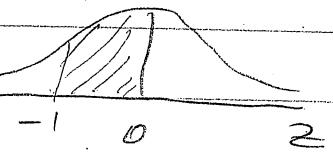
(6.37)

$$\mu = 200 \quad \sigma = 20$$

$$a. P(180 < X < 200) = P\left(\frac{180 - 200}{20} < z < \frac{200 - 200}{20}\right)$$

$$= P(-1 < z < 0) = P(z < 0) - P(z < -1)$$

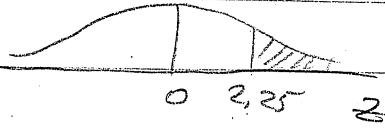
$$= .50 - .1587 = .3413$$



$$b. P(X > 245) = P(z > \frac{245 - 200}{20})$$

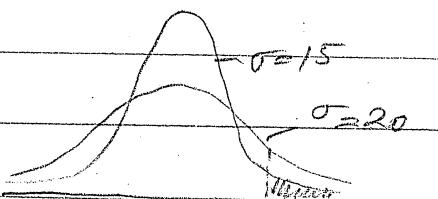
$$= P(z > 2.25) = 1 - P(z < 2.25)$$

$$= 1 - .9878 = .0122$$



c. As  $\sigma$  gets smaller, less

of the area (probability) will be under the curve  
for  $z > 2.25$

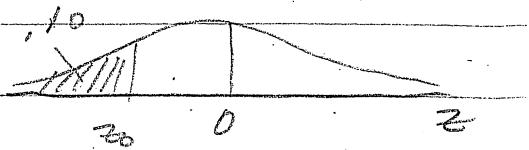


d.  $P(X < X_0) = .10$

$P(Z < Z_0) = .10$

$Z_0 = -1.28$

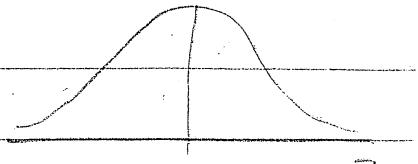
$X_0 = (-1.28)(20) + 200 = 174.40$



(6.38)

$\mu = 70$

$P(X < 85) = .9332$



$P(Z < \frac{85-70}{\sigma}) = .9332$

$Z = 1.5 = \frac{85-70}{\sigma}$

$\sigma = \frac{15}{1.5} = 10$

$P(X > 80) = P(Z > \frac{80-70}{10}) = P(Z > 1) = 1 - P(Z < 1)$

$= 1 - .8413 = .1587$  prob. of any one student

Scoring more than 80.

$P(\text{at least one of four}) = P(1 \text{ of four}) + P(2 \text{ of } 4) + P(3 \text{ of } 4) + P(4 \text{ of } 4)$

$= 1 - P(0 \text{ of } 4) = 1 - (1 - .1587)^4$

$= 1 - .5010 = .4990$

6.59

$$\mu_x = 100 \quad \sigma_x^2 = 100 \quad \mu_y = 200 \quad \sigma_y^2 = 400 \quad \rho_{xy} = .50$$

$$W = 5X + 4Y$$

$$E(W) = 5\mu_x + 4\mu_y = 5(100) + 4(200) = 1300$$

$$V(W) = (25)\sigma_x^2 + 16\sigma_y^2 + 2(5)(4) \text{cov}_{xy}$$

$$\text{where } \rho_{xy} = \frac{\text{cov}_{xy}}{\sigma_x \sigma_y}$$

$$.50 = \frac{\text{cov}_{xy}}{\sqrt{100} \sqrt{400}}$$

$$\text{cov}_{xy} = (.50)(10)(20)$$

$$= 100$$

$$V(W) = (25)(100) + (16)(400) + 40(100) = 12,900$$

(6.60)

$$\mu_x = 100 \quad \sigma_x^2 = 100 \quad \mu_y = 200 \quad \sigma_y^2 = 400 \quad \rho_{xy} = -.50$$

$$W = 5X + 4Y$$

$$E(W) = 5\mu_x + 4\mu_y = 5(100) + 4(200) = 1300$$

$$V(W) = (25)\sigma_x^2 + (16)\sigma_y^2 + 2(5)(4)\text{cov}_{xy}$$

$$\text{where } \rho_{xy} = \frac{\text{cov}_{xy}}{\sigma_x \sigma_y} = \frac{\text{cov}_{xy}}{\sqrt{100} \cdot \sqrt{400}}$$

$$-.50 = \frac{\text{cov}_{xy}}{200}$$

$$\text{cov}_{xy} = (-.50)(-100)$$

$$= -100$$

$$V(W) = 25(100) + (16)(400) + 40(-100)$$

$$= 2500 + 6400 - 4000$$

$$= 8900 - 4000 = 4900.$$

(6.61)

$$\begin{aligned}\mu_x &= 100 & \mu_y &= 200 & \rho_{xy} &= -0.5 \\ \sigma_x^2 &= 100 & \sigma_y^2 &= 400\end{aligned}$$

$$W = 5X - 4Y$$

$$\begin{aligned}E(W) &= 5(\mu_x) - 4(\mu_y) = 5(100) - 4(200) \\ &= 500 - 800 = -300\end{aligned}$$

$$V(W) = (25)\sigma_x^2 + 16(\sigma_y^2) - 2(5)(4) \text{cov}_{X,Y}$$

$$\text{where } \rho_{XY} = \frac{\text{cov}_{X,Y}}{\sigma_X \cdot \sigma_Y} = \frac{\text{cov}_{X,Y}}{\sqrt{100} \sqrt{400}}$$

$$-0.5 = \frac{\text{cov}_{X,Y}}{200}$$

$$\text{cov}_{X,Y} = 100$$

$$V(W) = (25)(100) + (16)(400) - 40(100)$$

$$= 2500 + 6400 - 4000 = 4900$$

(6.62)

$$\mu_x = 500 \quad \sigma_x^2 = 100 \quad \rho_{xy} = .50$$

$$\mu_y = 200 \quad \sigma_y^2 = 400$$

$$W = 5X - 4Y$$

$$E(W) = 5\mu_x - 4\mu_y = 5(500) - 4(200) = 2500 - 800 = 1700$$

$$V(W) = (25)\sigma_x^2 + (16)\sigma_y^2 - 2(5)(4)\text{cov}_{xy}$$

$$\text{where } \rho_{xy} = \frac{\text{cov}_{xy}}{\sigma_x \cdot \sigma_y} = \frac{\text{cov}_{xy}}{\sqrt{100} \sqrt{400}}$$

$$.5 = \frac{\text{cov}_{xy}}{(10)(20)} = \frac{\text{cov}_{xy}}{200}$$

$$\text{cov}_{xy} = (.5)(.200) = 100$$

$$V(W) = (25)(100) + (16)(400) - 40(100)$$

$$= 2500 + 6400 - 4000$$

$$= 4900$$

(6.63)

$$\mu_x = 100 \quad \sigma_x^2 = 500 \quad \rho_{xy} = -0.5$$

$$\mu_y = 200 \quad \sigma_y^2 = 400$$

$$W = 5X - 4Y$$

$$\mathbb{E}(W) = 5\mu_x - 4\mu_y = 5(100) - 4(200) = 500 - 800 = -300$$

$$V(W) = (25)\sigma_x^2 + (16)\sigma_y^2 - 2(5)(4)\text{cov } XY$$

$$\text{where } \rho_{xy} = \frac{\text{cov } XY}{\sigma_x \cdot \sigma_y} = \frac{\text{cov } XY}{\sqrt{500} \sqrt{400}}$$

$$-0.5 = \frac{\text{cov } XY}{(22.36)(20)} = \frac{\text{cov } XY}{447.21}$$

$$\text{cov } XY = (-0.5)(447.21)$$

$$= -223.61$$

$$V(W) = (25)(500) + (16)(400) - 40(-223.61)$$

$$= 12500 + 6400 - 8944.4 = 9955.6$$

6.64

$$\pi = 10,000 + 100,000x \quad x \sim N(-18, .06)$$

$$E(\pi) = 10,000 + 100,000 E(x) = 10,000 + 18000 = 28,000$$

$$\begin{aligned} V(\pi) &= 0 + (100,000)^2 V(x) & V(x) = \sigma^2 = .0036 \\ &= 0 + 100,000,000 (.0036) \\ &= 36,000,000 \end{aligned}$$

$$S(\pi) = \sqrt{36,000,000} = 6000$$