# Exploiting Imprecise Information Sources in Sequential Decision Making Problems under Uncertainty

# **N.Drougard**

under D.Dubois, J-L.Farges and F.Teichteil-Königsbuch supervision
doctoral school: EDSYS institution: ISAE-SUPAERO
laboratory: ONERA-The French Aerospace Lab





retour sur innovation

Autonomous robotics

# Onera, Flight Dynamics & System control

Control Engineering, Artificial intelligence, Cognitive Sciences

 $\pi$ -modeling advancements in  $\pi$ -POMDP solver & factorization hybrid model conclusion

### Context

context

Autonomous robotics

# Onera, Flight Dynamics & System control

Control Engineering, Artificial intelligence, Cognitive Sciences

## among many other works:

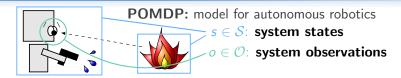
- autonomy and human factors
- decision making, planning
- experimental/industrial applications: UAVs, human-machine interaction, exploration robots

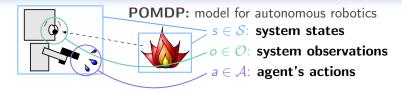




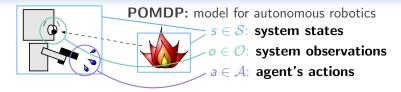


context





context



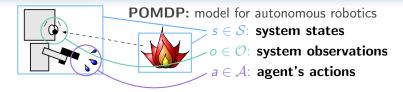


 $\pi$ -modeling advancements in  $\pi$ -POMDP solver & factorization hybrid model conclusion

#### Context

context

#### Partially Observable Markov Decision Processes (POMDPs)



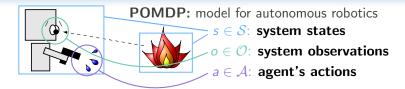
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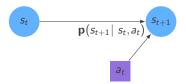
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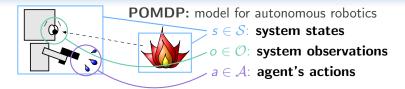
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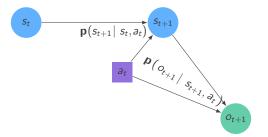
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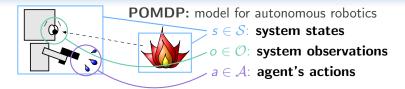


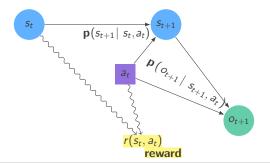
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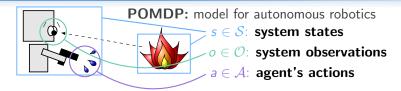


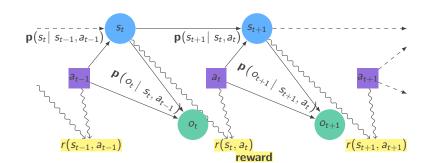
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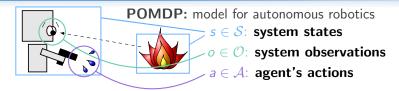


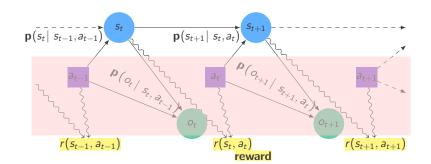
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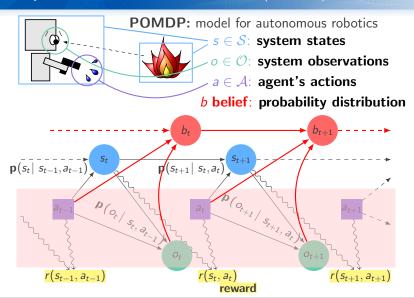


context





context



# belief state, strategy, criterion

**POMDP:**  $\langle S, A, O, T, O, r, \gamma \rangle$  (Smallwood et al. 1973)

- **transition** function  $T(s, a, s') = \mathbf{p}(s' | s, a)$
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 $\pi$ -modeling

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# **probabilistic** belief update – a selected, o' received

$$b_{t+1}(s') \propto \mathbf{p}\left(\left.o'\left|\right. s', a\right) \cdot \sum_{s \in \mathcal{S}} \mathbf{p}\left(\left.s'\left|\right. s, a\right.\right) \cdot b_t(s)$$

context

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# action choices: strategy $\delta(b_t) = a_t \in \mathcal{A}$

maximizing  $\mathbb{E}_{s_0\sim b_0}\left[\left.\sum^{+\infty}\gamma^t\cdot r\Big(s_t,\delta(b_t)\Big)\right.
ight]$  ,  $0<\gamma<1$ 

# Flaws of the POMDP model POMDPs in practice

optimal strategy computation PSPACE-hard
 (Papadimitriou et al., 1987)

probabilities are imprecisely known in practice

prior ignorance semantic/management?

context

practical issues: Complexity, Vision and Initial Belief

 POMDP optimal strategy computation undecidable in infinite horizon (Madani et al. 1999)

solver & factorization

context

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- → optimality for "small" or "structured" POMDPs
- $\rightarrow \mathsf{approximate}\ \mathsf{computations}$

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 $\pi$ -modeling advancements in  $\pi$ -POMDP solver & factorization hybrid model conclusion

# Context

context

### practical issues: Complexity, Vision and Initial Belief

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**Lack of prior information** on the system state: initial belief state  $b_0$ 

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context

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- Lack of prior information on the system state: initial belief state  $b_0$
- $\rightarrow$  uniform probability distribution  $\neq$  ignorance!

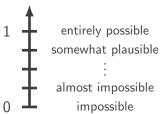
hybrid model

# Qualitative Possibility Theory presentation - (max,min) "tropical" algebra

finite scale  $\mathcal{L}$ 

 $\pi$ -modeling

usually  $\{0, \frac{1}{\nu}, \frac{2}{\nu}, \dots, 1\}$ 



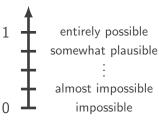
events  $e \subset \Omega$  (universe) **sorted** using possibility **degrees**  $\pi(e) \in \mathcal{L}$ quantified with frequencies  $p(e) \in [0,1]$  (probabilities) presentation - (max,min) "tropical" algebra

# finite scale $\mathcal{L}$

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context

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 (universe)

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$$\pi(e) \in \mathcal{L}$$

quantified with frequencies 
$$p(e) \in [0,1]$$
 (probabilities)

$$e_1 \neq e_2$$
, 2 events  $\subset \Omega$ 

$$\blacksquare \pi(e_1) < \pi(e_2) \Leftrightarrow \text{``e_1 is less plausible than } e_2\text{''}$$

(context)

advancements in  $\pi$ -POMDP

Probability	/ Possibility:
+	max
×	min
$X \in \mathbb{R}$	$X\in\mathcal{L}$
$\mathbb{E}[X] = \sum_{x \in X} x \cdot \mathbf{p}(x)$	optimistic: $\mathbb{S}_{\Pi}[X] = \max_{x \in X} \min \{x, \pi(x)\}$
	pessimistic:
	$\mathbb{S}_{\mathcal{N}}[X] = \min_{x \in X} \max \{x, 1 - \pi(x)\}$

# Qualitative Possibility Theory qualitative possibilistic POMDP (π-POMDP)

Sabbadin (UAI-98) introduces

# the qualitative possibilistic POMDP

 $\pi$ -POMDP:  $\langle \mathcal{S}, \mathcal{A}, \mathcal{O}, T^{\pi}, O^{\pi}, \rho \rangle$ 

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- **preference** function  $\rho: \mathcal{S} \times \mathcal{A} \to \mathcal{L}$
- belief space trick: POMDP  $\rightarrow$  MDP with **infinite** space  $\pi$ -POMDP  $\rightarrow$   $\pi$ -MDP with **finite** space
- problem becomes decidable
- $\blacksquare \ \forall s \in \mathcal{S}, \ \pi(s) = 1 \Leftrightarrow \text{total ignorance about } s$

context

# A possibilistic belief state finite belief space

$$\Pi_{\mathcal{L}}^{\mathcal{S}} = \left\{ \text{ possibility distributions } \right\}: \ \#\Pi_{\mathcal{L}}^{\mathcal{S}} \sim \#\mathcal{L}^{\#\mathcal{S}} < +\infty$$
  $\rightarrow i.e.$  **finite belief space**

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# possibilistic belief update – a selected, o' received

joint distribution on  $S \times \mathcal{O}$  from  $\beta_t$ :  $\pi$  ( o',  $s' \mid \beta_t$ , a)

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 $\pi$ -modeling

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 **next belief state:**  $\beta_{t+1}(s') = \pi (o', s' | \beta_t, a)$  unless  $s'$  maximizes  $\pi (o', s' | \beta_t, a)$ , then  $\beta_{t+1}(s') = 1$ 

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**Makovian update:** only depends on o', a and  $b_{+}^{\pi}$ 

## Overview

#### **Qualitative Possibility Theory:**

→ simplification, imprecision/prior ignorance modeling

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- introductory example: qualitative possibilistic modeling
- **2 advancements** in  $\pi$ -POMDP:

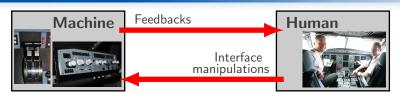
mixed-observability & indefinite horizon

**3** simplifying computations:

ADD-based solver & factorization

probabilistic-possibilistic (hybrid) approach

# Example: Human-Machine Interaction (HMI) joint work with Sergio Pizziol – Context



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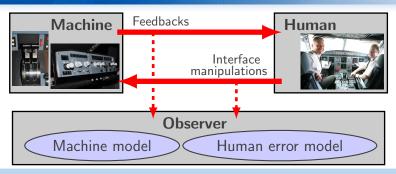


**Issue:** incorrect human assessment of the machine state

→ accident risk

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context

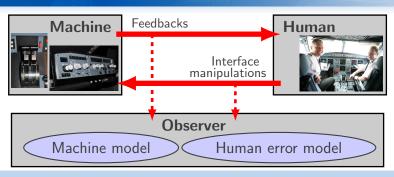


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context  $(\pi$ -modeling) advancements in  $\pi$ -POMDP solver & factorization hybrid model conclusion

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**Issue:** incorrect human assessment of the machine state

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#### $\pi$ -POMDP without actions: $\pi$ -Hidden Markov Process

- **system space**  $\mathcal{S}$ : set of human assessments  $\rightarrow$  **hidden**
- **observation space**  $\mathcal{O}$ : feedbacks/human manipulations

# Example: Human-Machine Interaction (HMI) Human error model from expert knowledge

Machine with states A, B, C, ...

state  $s_A \in \mathcal{S}$ : "human thinks machine state is A"

 $\pi$ -modeling

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#### Machine state transition $A \rightarrow B$

■ observation: machine feedback  $o'_f \in \mathcal{O}$ :

"human usually aware of feedbacks"  $o \pi\left(s_B',o_f'\mid s_A\right)=1$  "but may lose a feedback"  $o \pi\left(s_A',o_f'\mid s_A\right)=\frac{2}{3}$ 

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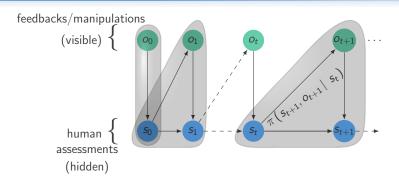
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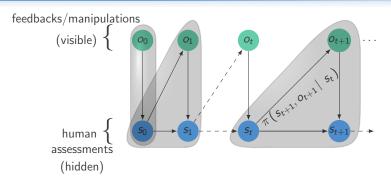
■ impossible cases: possibility degree 0

 $\pi$ -modeling



advancements in  $\pi$ -POMDP

 $\pi$ -modeling



- **estimation** of the human assessment
  - ⇔ possibilistic belief state
- detection of human assessment errors + diagnosis
- validated with pilots on flight simulator missions

 $\pi$ -modeling (advancements in  $\pi$ -POMDP) solver & factorization hybrid model conclusion

## Applicability of the $\pi$ -POMDPs three advancements

- lack of proof of optimality in indefinite horizon settings
- criterion/algorithm/proof
- curse of dimensionality:
  - $\rightarrow$  belief space size of a  $\pi$ -POMDP: exponential in  $\#\mathcal{S}$
- lacksquare in practice, part of  $s \in \mathcal{S}$  is visible
  - $\Rightarrow$  complexity reduction
- lack of possibilistic strategy evaluation
- demonstration of usefulness when probabilities are imprecise

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Indefinite Horizon, Mixed-Observability, Simulations contribution UAI 2013

context

## criterion, DP scheme, optimal strategy

#### indefinite horizon criterion:

$$orall s \in \mathcal{S}$$
, maximizing  $\mathbb{S}_{\Pi}\Big[\Psi(S_{\#\delta})\Big|S_0=s\Big]$ 

with respect to the strategy  $\delta:(t,s)\mapsto a_t\in\mathcal{A}$ .

conclusion

### Indefinite Horizon

context

criterion, DP scheme, optimal strategy

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ight\} \end{aligned}$$

context

### Indefinite Horizon

criterion, DP scheme, optimal strategy

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with respect to the strategy  $\delta:(t,s)\mapsto a_t\in\mathcal{A}$ .

#### Dynamic Programming scheme: # iterations $< \# \mathcal{S}$

- $\blacksquare$  assumption:  $\exists$  artificial "stay" action as in classical planning/ $\gamma$  counterpart
- criterion non decreasing with iterations

context

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#### indefinite horizon criterion:

$$\begin{split} \forall s \in \mathcal{S}, \text{ maximizing } \mathbb{S}_{\Pi} \Big[ \Psi(S_{\#\delta}) \Big| S_0 &= s \Big] \\ &= \max_{(s_1, \dots, s_{\#\delta})} \min \left\{ \min_{t=0}^{\#\delta - 1} \pi\Big(s_{t+1} \Big| s_t, \delta_t(s_t)\Big), \Psi(s_{\#\delta}) \right\} \end{split}$$

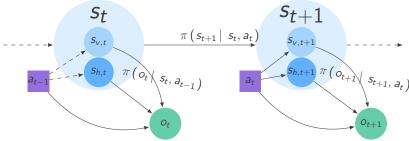
with respect to the strategy  $\delta:(t,s)\mapsto a_t\in\mathcal{A}$ .

#### Dynamic Programming scheme: # iterations $< \#\mathcal{S}$

- $\blacksquare$  assumption:  $\exists$  artificial "stay" action as in classical planning/ $\gamma$  counterpart
- criterion non decreasing with iterations
- action update for states increasing the criterion
- proof of optimality of the resulting stationary strategy

#### Mixed-Observability (MOMDP, Ong et al., 2005) $\pi$ -Mixed-Observable Markov Decision Process ( $\pi$ -MOMDP)

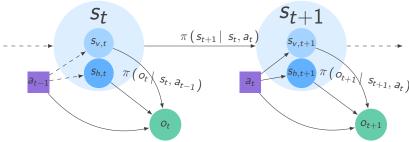
**graphical model** of a  $\pi$ -MOMDP:



**Mixed-Observability:** system state  $s \in \mathcal{S} = \mathcal{S}_v \times \mathcal{S}_h$ i.e. state s = visible component  $s_v$  & hidden component  $s_h$ 

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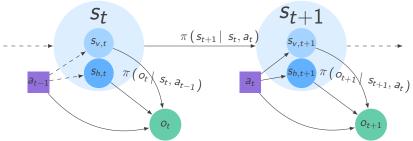
context

hybrid model

### Mixed-Observability (MOMDP, Ong et al., 2005)

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- belief states only over  $S_h$  (component  $s_v$  observed)
- $\blacksquare \to \pi$ -POMDP: belief space  $\Pi_c^S \qquad \#\Pi_c^S \sim \#\mathcal{L}^{\#S}$ 
  - $\to \pi$ -MOMDP: computations on  $\mathcal{X} = \mathcal{S}_{\nu} \times \Pi_{c}^{\mathcal{S}_{h}}$

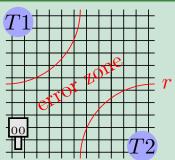
 $\#\mathcal{X} \sim \#\mathcal{S}_{v} \cdot \#\mathcal{L}^{\#\mathcal{S}_{h}} \ll \#\Pi_{\mathcal{L}}^{\mathcal{S}}$ 

 $\pi$ -modeling (advancements in  $\pi$ -POMDP) solver & factorization hybrid model conclusion

## $\pi$ -MOMDP for robotics with imprecise probabilities simulations with machine vision behavior imprecisely known

- **goal:** reach the object A = T1 or T2
- noisy observations of the location of the object A

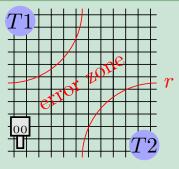
### Recognition mission: robot on a grid, targets T1 & T2



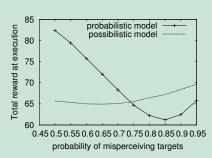
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context



in reality, misperception probability in the error zone:  $P_{bad}>rac{1}{2}$ 

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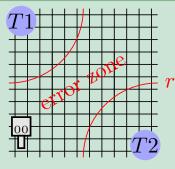
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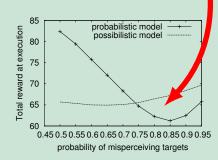
- **goal:** reach the object *A* - noisy observations of the

context

probabilistic model inappropriate with too imprecise probabilities

Recognition mission: robot on a grid, targets  $T1\ \&\ T2$ 



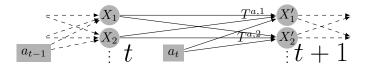


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# Factored $\pi$ -MOMDP and computations with ADDs qualitative possibilistic models to reduce complexity

context

**contribution (AAAI-14):** factored  $\pi$ -MOMDP  $\Leftrightarrow$  state space  $\mathcal{X} = \mathcal{S}_{\nu} \times \Pi_{\mathcal{L}}^{\mathcal{S}_h} = \text{Boolean variables } (X_1, \dots, X_n) + \text{independence assumptions} \Leftarrow \text{graphical model}$ 

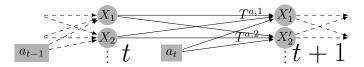


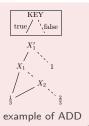
### Factored $\pi$ -MOMDP and computations with ADDs

qualitative possibilistic models to reduce complexity

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# Simplify computations with $\pi$ -MOMDPs Resulting $\pi$ -MOMDP solver: PPUDD

- probabilistic model: + and × ⇒ new values created
   ⇒ number of ADDs leaves potentially huge
- possibilistic model: min and max  $\Rightarrow$  values  $\in \mathcal{L}$  finite  $\Rightarrow$  number of leaves bounded, **ADDs smaller**.

 $\pi$ -modeling advancements in  $\pi$ -POMDP (solver & factorization) hybrid model conclusion

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### PPUDD: Possibilistic Planning Using Decision Diagrams

■ factorization ⇒ each DP steps divided into n stages
 → smaller ADDs ⇒ faster computations

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### PPUDD: Possibilistic Planning Using Decision Diagrams

- factorization ⇒ each DP steps divided into n stages
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- computations on trees: CU Decision Diagram Package.

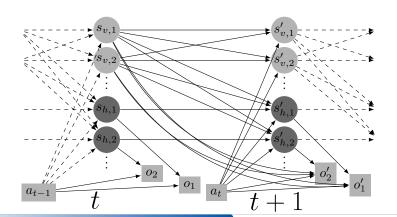
text  $\pi$ -modeling advancements in  $\pi$ -POMDP (solver & factorization) hybrid model conclusion

### Simplifying computations with $\pi$ -MOMDPs

Natural factorization: belief independence

### contribution (AAAI-14):

independent sensors, hidden states,  $\ldots \Rightarrow$  graphical model



### Simplifying computations with $\pi$ -MOMDPs

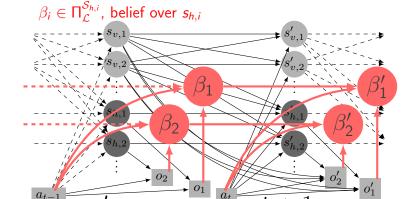
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context

independent sensors, hidden states,  $... \Rightarrow$  graphical model

d-Separation 
$$\Rightarrow$$
  $(s_v, \beta) = (s_{v,1}, \dots, s_{v,m}, \beta_1, \dots, \beta_l)$ 



 $\pi$ -modeling advancements in  $\pi$ -POMDP (solver & factorization) hybrid model conclusion

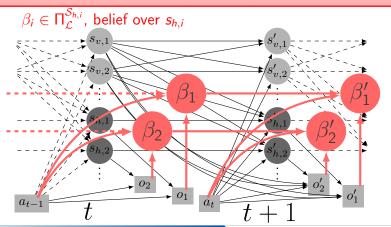
### Simplifying computations with $\pi$ -MOMDPs

Natural factorization: belief independence

context

⊥⊥ assumptions on state & observation variables

- → belief variable factorization
- ightarrow additional computation savings



context π-modeling advancements in π-POMDP (solver & factorization) hybrid model conclusion

#### Simplify computations with $\pi$ -MOMDPs Experiments – perfect sensing: Navigation problem

PPUDD vs SPUDD (Hoey et al., 1999)

Navigation benchmark: reach a goal – spots with accident risk M1 (resp. M2) optimistic (resp. pessimistic) criterion

## Simplify computations with $\pi\text{-MOMDPs}$

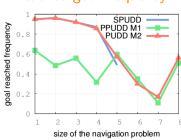
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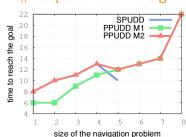
#### Performances, function of the problem index

#### reached goal frequency



the higher the better

# steps to reach the goal



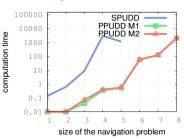
the lower the better

 $\pi$ -modeling advancements in  $\pi$ -POMDP solver & factorization hybrid model conclusion context

## Simplify computations with $\pi$ -MOMDPs

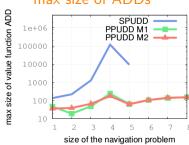
Experiments – perfect sensing: Navigation problem

#### computation time



the lower the better

## max size of ADDs



the lower the better

- PPUDD + M2 (pessimistic criterion) faster with same performances as SPUDD
- SPUDD only solves the first 5 instances
- verified intuition: ADDs are smaller

## Simplify computations with $\pi$ -MOMDPs

Experiments – imperfect sensing: RockSample problem

PPUDD vs APPL (*Kurniawati et al.*, 2008, solver MOMDP) symbolic HSVI (*Sim et al.*, 2008, solver POMDP)

RockSample benchmark: recognize and sample "good" rocks

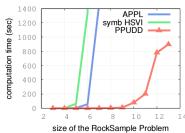
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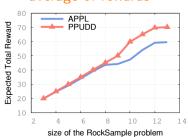
RockSample benchmark: recognize and sample "good" rocks

#### computation time:



the lower the better

#### average of rewards

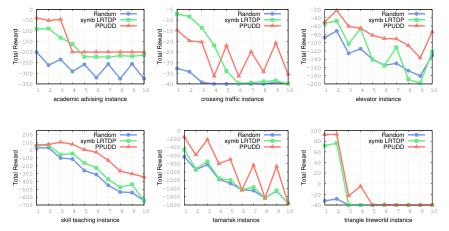


the higher the better

approximate model + exact resolution solver can be
 better than exact model + approximate resolution solver

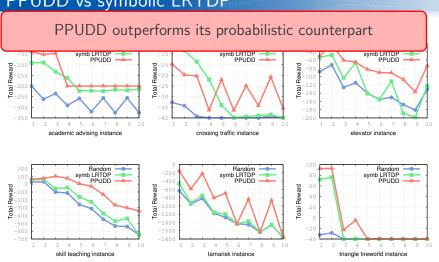
# IPPC 2014 – ADD-based approaches: PPUDD vs symbolic LRTDP

PPUDD + BDD mask over reachable states.



average of rewards over simulations — the higher the better

# IPPC 2014 – ADD-based approaches: PPUDD vs symbolic LRTDP



average of rewards over simulations - the higher the better

## Qualitative possibilistic approach: benefits/drawbacks towards a hybrid POMDP

granulated belief space (discrete)

- lacktriangleright efficient problem **simplification** (PPUDD  $2\times$  better than LRTDP with ADDs)
- ignorance and imprecision modeling

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- granulated belief space (discrete)
- lacktriangleright efficient problem **simplification** (PPUDD  $2\times$  better than LRTDP with ADDs)
- ignorance and imprecision modeling
- choice of the qualitative criterion (optimistic/pessimistic)
- preference → non additive degrees
   → same scale as possibility degrees (commensurability)
- coarse approximation of probabilistic model
   → no frequentist information

## A hybrid model a probabilistic POMDP with possibilistic belief states

#### hybrid approach

- agent knowledge = possibilistic belief states
- probabilistic dynamics & quantitative rewards

## A hybrid model

context

a probabilistic POMDP with possibilistic belief states

#### hybrid approach

- agent knowledge = possibilistic belief states
- probabilistic dynamics & quantitative rewards

#### Usefullness

- → heuristic for solving POMDPs: results in a standard (finite state space) MDP
- → problem with qualitative & quantitative uncertainty

context

(hybrid model)

#### Transitions and rewards

belief-based transition and reward functions

possibility distribution  $\beta \to \text{probability distribution } \beta$ using poss-prob tranformations (Dubois et al., FSS-92)

#### Transition function on belief states

$$\Rightarrow \mathbf{p}\Big(\beta'\Big|\overline{\beta},a\Big) = \sum_{\substack{o' \text{ t.q.} \\ \textit{update}(\beta,a,o') = \beta'}} \mathbf{p}\left(o' \mid \overline{\beta},a\right)$$

solver & factorization

 $\pi$ -modeling

context

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 $\blacksquare$  reward cautious according to  $\beta$ 

#### Pessimistic Choquet Integral

$$r(\beta, a) = \sum_{i=1}^{\#\mathcal{L}-1} (I_i - I_{i+1}) \cdot \min_{\substack{s \in \mathcal{S} \text{ s.t.} \\ \beta(s) \geqslant I_i}} r(s, a)$$

## Resulting MDP

context

translation from hybrid POMDP to MDP – contribution (SUM-15):

input: a POMDP  $\langle \mathcal{S}, \mathcal{A}, \mathcal{O}, T, O, r, \gamma \rangle$  output: the MDP  $\langle \tilde{\mathcal{S}}, \mathcal{A}, \tilde{T}, \tilde{r}, \gamma \rangle$ :

conclusion

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- state space  $\tilde{\mathcal{S}} = \Pi_c^{\mathcal{S}}$ , the set of the possibility distributions over  $\mathcal{S}$
- $\forall \beta, \beta'$  possibilistic belief states  $\in \Pi_c^S$ ,  $\forall a \in A$ , transitions  $\tilde{T}(\beta, a, \beta') = \mathbf{p}(\beta'|\beta, a)$

(hybrid model)

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- reward  $\tilde{r}(a,\beta) = \underline{Ch}(r(a,.))$ ,

criterion: 
$$\mathbb{E}_{\beta_{t} \sim \tilde{T}}\left[\sum_{t=0}^{+\infty} \gamma^{t} \cdot \tilde{r}\left(\beta_{t}, d_{t}\right)\right]$$
.

3 classes of state variables - contribution (SUM-15)

variable: **visible**  $s'_v \in \mathbb{S}_v$ 



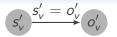
inferred hidden  $s_h' \in \mathbb{S}_h$ 





3 classes of state variables - contribution (SUM-15)

variable: visible  $s'_v \in \mathbb{S}_v$ 



inferred hidden  $s'_h \in \mathbb{S}_h$ 





3 classes of state variables - contribution (SUM-15)

variable: visible  $s'_v \in \mathbb{S}_v$ 

$$s'_{v} \xrightarrow{s'_{v} = o'_{v}} o'_{v}$$

$$\beta_{t+1}(s'_v) = \mathbb{1}_{\{s'_v = o'_v\}}(s'_v)$$

inferred hidden  $s'_h \in \mathbb{S}_h$ 





context

#### Belief variable factorization

3 classes of state variables - contribution (SUM-15)

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⇔ deterministic belief variable

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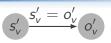
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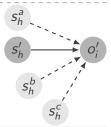
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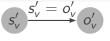
context

## 3 classes of state variables - contribution (SUM-15)

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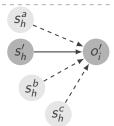
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$$\beta_{t+1}\Big(parents(o_i')\Big) = \beta_{t+1}(s_h, s_h^a, s_h^b, s_h^c)$$





context

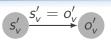
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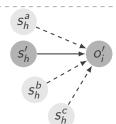
⇔ deterministic belief variable

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## inferred hidden $s'_h \in \mathbb{S}_h$

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 $\propto^{\pi} \pi\Big(o_i', extit{parents}(o_i')\Big|eta_t, a\Big)$ 



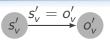


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 $\wedge \mathcal{P}(o_i)$  may contain visible variables.

fully hidden 
$$s'_f \in \mathbb{S}_f$$



context

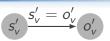
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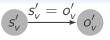
 $\pi$ -modeling

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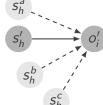


## inferred hidden $s'_h \in \mathbb{S}_h$

$$\beta_{t+1}\Big(parents(o'_i)\Big) = \beta_{t+1}(s_h, s_h^a, s_h^b, s_h^c)$$

$$\propto^{\pi} \pi \Big( o_i', parents(o_i') \Big| \beta_t, a \Big)$$

 $\wedge \mathcal{P}(o'_i)$  may contain visible variables.



$$S'_f \longrightarrow O'_i$$

$$\beta_{t+1}(s_f') = \pi(s_f' \mid \beta_t, a)$$

3 classes of state variables - contribution (SUM-15)

## variable: visible $s'_{\nu} \in \mathbb{S}_{\nu}$

⇔ deterministic belief variable

$$\beta_{t+1}(s'_v) = \mathbb{1}_{\{s'_v = o'_v\}}(s'_v)$$



$$\beta_{t+1}\Big(parents(o'_i)\Big) = \beta_{t+1}(s_h, s_h^a, s_h^b, s_h^c)$$

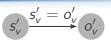
$$\propto^{\pi} \pi \Big( o_i', parents(o_i') \Big| \beta_t, a \Big)$$

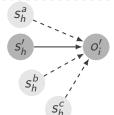
 $\wedge \mathcal{P}(o'_i)$  may contain visible variables.

### fully hidden $s'_f \in \mathbb{S}_f$

 $\rightarrow$  observations don't inform belief state on  $s'_f$ .

$$\beta_{t+1}(s_f') = \pi(s_f' \mid \beta_t, a)$$







global belief state from marginal belief variables

advancements in  $\pi$ -POMDP

#### bound over the global belief state

$$\beta_{t+1}(s'_1,\ldots,s'_n) = \pi(s'_1,\ldots,s'_n | a_0,o_1,\ldots,a_t,o_{t+1})$$

$$\leqslant \min \Biggl\{ \min_{s_j' \in \mathbb{S}_v} \Biggl[ \mathbb{1}_{\left\{s_j' = o_j'\right\}} \Biggr], \min_{s_j' \in \mathbb{S}_f} \Biggl[ \beta_{t+1}(s_j') \Biggr], \min_{o_i' \in \mathbb{O}_h} \Biggl[ \beta_{t+1} \left( parents(o_i') \right) \Biggr] \Biggr\}$$

global belief state from marginal belief variables

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- min of marginals = a **less informative** belief state
- computed using marginal belief states
  - → factorization & smaller state space

## Conclusion contributions

context

lacktriangleright modeling efforts: ightarrow human-machine interaction

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- lacktriangledown modeling efforts: ightarrow human-machine interaction
- advancements: → mixed-observability modeling → indefinite horizon + optimality proof

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- modeling efforts: → human-machine interaction
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- **experimentations**: realistic problems
  - → robust recognition mission with possibilistic beliefs
  - ightarrow validation of the computation time reduction
  - → IPPC 2014

#### Conclusion contributions

- **modeling efforts**: → human-machine interaction
- advancements: → mixed-observability modeling  $\rightarrow$  indefinite horizon + optimality proof
- **simplifying computations**: factorization work & PPUDD algorithm
- **experimentations**: realistic problems
  - → robust recognition mission with possibilistic beliefs
  - → validation of the computation time reduction
  - $\rightarrow$  IPPC 2014
- - → probabilities on possibilistic belief states pessimistic rewards (Choquet integral)
  - → factored POMDP \*\* factored finite MPD

## Conclusion perspectives

- refined criteria (Weng 2005, Dubois et al. 2005) ⇒ finer  $\pi$ -POMDP
- combination with reinforcement learning

- refined criteria (Weng 2005, Dubois et al. 2005)  $\Rightarrow \text{ finer } \pi\text{-POMDP}$
- combination with reinforcement learning

quantitative information may be available: hybrid work

- IPPC problems (factored POMDPs);
- tests of this approach:
  - **1 simplification:**  $\pi$  distributions definition?
  - **2 imprecision:** robust in practice?



context





## Thank you!

#### produced work:

- Qualitative Possibilistic Mixed-Observable MDPs,
   UAI-2013
- Structured Possibilistic Planning Using Decision Diagrams, AAAI-2014
- Planning in Partially Observable Domains with Fuzzy
   Epistemic States and Probabilistic Dynamics, SUM-2015
- Processus Décisionnels de Markov Possibilistes à Observabilité Mixte, Revue d'Intelligence Artificielle (RIA journal)
- A Possibilistic Estimation of Human Attentional Errors, submitted to IEEE-TFS journal