Low SNR FreeDV Mode

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1 Introduction

After 10 years development and on air experience with various FreeDV waveforms, we would like to develop a new waveform that outperforms and replaces a variety of existing modes such as 700C/D/E and 1600. Requirements include [5]:

- 1. Better performance than SSB at 0dB SNR on MPP and MPD channels.
- 2. A single mode that can handle MPP, MPD, GEO (e.g. QO-100), and replace several existing FreeDV modes, simplifying the end user experience.
- 3. For compliance with Export Control regulations, the minimum speech codec bit rate is 700 bit/s.
- 4. Use of legacy analog HF radio sets with a RF bandwidth of around 2000 Hz.
- 5. Compliant with the 300 baud per carrier limit set by the United States FCC, which implies a parallel tone or OFDM modem.

It is acceptable for performance to gradually decrease as the multipath channel quality declines, but we would like the decline to be gradual, e.g. a few dB more power for operation on MPD versus MPP.

This document explores ways we can improve the existing OFDM modem waveforms in order to meet these requirements.

1.1 Glossary

Acronym	Explanation				
AWGN	Additive White Gaussian Noise - a communications				
	channel with flat frequency response and additive				
	noise				
CP	Cyclic Prefix				
FEC	Forward Error Correction				
ISI	Inter Symbol Interference				
LEO	Low earth orbit satellite channel, AWGN with large				
	freq offset and Doppler shift (high rate of change of				
	freq offset)				
GEO	Geosynchronous satellite channel, AWGN but high				
	phase noise and large freq offset				
OTA	Over The Air				
PTT	Push To Talk - voice communications where only one				
	person is transmitting at any one time. Common in				
	two way radio but not mobile telephones				
MPP	Multipath Poor channel, 1 Hz Doppler spread, 2ms				
	delay spread, typical for US and Australian inter-				
	state propogation				
MPD	Multipath Disturbed channel, 2 Hz Doppler spread,				
	4ms delay spread, typical for UK Winter NVIS pro-				
	pogation				
	1 0				

Table 1: Glossary of Acronyms

 $^{^{1}\}mathrm{Can}$ be expressed as a linear ratio E_{b}/N_{0} or $10log_{10}(E_{b}/N_{0})$ dB

Symbol	Explanation	Units
\overline{B}	Noise bandwidth	Hz
B_d	Doppler spreading bandwidth for HF channel model	$_{ m Hz}$
E_b/N_0	Energy per bit on spectral noise density	dimensionless, dB^1
N_s	Number of symbols in a <i>modem frame</i> , pilot insertion rate	dimensionless
R_b	Bit rate	Bits/second
R_s	Symbol rate	symbols/second
T_s	Symbol period	seconds
SNR	Signal to Noise Ratio	dB
S	Signal Power	Watts
N	Noise Power	Watts
N_c	Number of carriers in an OFDM waveform	

Table 2: Glossary of Symbols

2 Modem and Channel Models

In this section we will develop theoretical models to help us explore performance limits.

2.1 SNR and Bandwidth Limits

For practical PTT voice systems algorithmic delay is limited to a few 100ms, which limits the FEC codeword size and hence the performance of the code. For PSK channels a threshold $E_b/N_0 = 2 \,\mathrm{dB}$ and a code rate R = 0.5 is typical, where E_b/N_0 is the energy per payload data bit (coded E_b/N_0). The lowest (threshold) SNR for a viable voice link is given by:

$$\frac{S}{N} = \frac{E_b R_b}{N_0 B}$$

$$SNR = 10log_{10} \left(\frac{E_b}{N_0}\right) + 10log_{10} \left(\frac{R_b}{B}\right) \quad [dB]$$
(1)

where R_b is the payload data bit rate, and B is the bandwidth in which we measure SNR. Given Rb = 700 and B = 3000 we have:

$$SNR = 2 + 10log_{10}(700/3000)$$

= -4.3 dB (2)

This is ideal performance for an AWGN channel. In practice we must allocate some power to symbols used for synchronisation, such as pilot symbols used for frequency and phase estimation, or unique word bits used for frame synchronisation. Synchronisation algorithms often struggle at low SNRs, introducing additional "implementation" losses.

Performance on multipath channels is significantly worse, in our use cases typically 5 dB. On these channels, we may allocate some carrier power to deal with intersymbol interference (for example a cyclic prefix in OFDM modems).

A more complete model is:

$$SNR = 10log_{10}\left(\frac{E_b}{N_0}\right) + 10log_{10}\left(\frac{R_b}{B}\right) + L_p + L_{il} + L_{cp}$$
 (3)

where L_p is the loss from power allocated to pilot symbols, L_{il} is the real world implementation loss, and L_{cp} is the loss in SNR due to the power allocated to the cyclic prefix.

To combat intersymbol interference and Doppler Spread on HF multipath channels, it is convenient to use parallel tone or OFDM modems. The signal is divided into N_c carriers, each carrying R_b/N_c bits/s. Due to the spectral efficiency of OFDM, the same bit rate, symbol rate, and occupied bandwidth is required for any N_c . For example:

1. A QPSK signal of $R_s = 1000$ symbols/s and $R_b = 2R_s = 2000$ bits/s occupies B = 1000 Hz (central lobe).

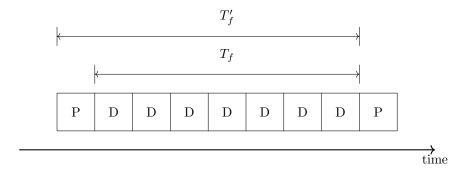
2. An OFDM signal of $N_c = 20$ carriers each at $R_s = 50$ symbol/s gives us a total $R_b = 2N_cR_s = 2000$ bits/s and occupies a RF bandwidth of $B = N_cR_s = 1000$ Hz.

This simple relationship between per-carrier and total R_s allows us to use them interchangeably for some calculations.

FreeDV signals are typically transmitted over the air using legacy HF radios. We assume an analog bandwidth of 2000 Hz is available, which allows a maximum of 4000 bit/s using QPSK. In practice the payload data rate is much less, due to various overheads that we will discuss below.

2.2 Pilot Symbol Overhead

Figure 1: Modem Frame with $N_s = 8$, the pilot of the next modem frame is also shown.



In this section we explore the effect of inserting pilot symbols on the threshold SNR (1). Consider a sequence of N_s-1 PSK data symbols that carry the modulated FEC codeword bits (e.g. data and parity bits) over the channel. We denote this sequence a modem $modem\ frame$. The frame of N_s-1 symbols has a period of $T_f=(N_s-1)T_s$ seconds, where T_s is the period of each symbol. We wish to insert a single pilot symbol after the data symbols, creating a new frame N_s symbols long, with period $T_f'=N_sT_s$. To maintain the same payload data rate:

$$T_f = T'_f$$

$$(N_s - 1)T_s = N_s T_s$$

$$R'_s = R_s \frac{N_s}{N_s - 1}$$
(4)

where the symbol rate $R_s = 1/T_s$. Expressing S/N (1) in terms of E_s and R_s :

$$\frac{S}{N} = \frac{E_s R_s}{N_0 B}$$

$$\frac{S'}{N} = \frac{E_s R'_s}{N_0 B}$$

$$= \frac{E_s R_s N_s}{N_0 B(N_s - 1)}$$

$$\frac{S'/N}{S/N} = \frac{N_s}{N_s - 1}$$
(5)

Thus when we insert pilots, the threshold S/N increases by a factor of $N_s/(N_s-1)$. Expressed in dB:

$$10log_{10}\left(\frac{S'}{N}\right) = 10log_{10}\left(\frac{S}{N}\right) + 10log_{10}\left(\frac{N_s}{N_s - 1}\right)$$

$$SNR' = SNR + 10log_{10}\left(\frac{N_s}{N_s - 1}\right)$$

$$SNR' = SNR + L_p \quad [dB]$$

$$(6)$$

where L_p can be considered the pilot symbol loss - the SNR degradation from the ideal performance (1) due to the insertion of pilot symbols. For example FreeDV 700D uses a pilot insertion rate of $N_s=8$ results in $L_p=10log_{10}(8/7)=0.58$ dB, thus we need 0.58 dB more SNR to achieve the threshold SNR for the voice link. For this example let Rs be the total symbol rate over all N_c carriers. To maintain Rs=700 data symbols/second over the channel, we require $R_s'=(700)8/7=800$ symbols/second which introduces a 100 Hz bandwidth overhead.

2.3 Cyclic Prefix Overhead

Now we consider the SNR overhead for the Cycle Prefix (CP) used in OFDM modems to cope with delay spread on multipath channels. To achieve our payload data rate (e.g. 700 bits/s), we FEC encode and map the bits to PSK symbols D, and distribute the symbols across N_c parallel carriers. The transmitter power is spread equally across all carriers.

We send symbols D across the channel at a constant symbol rate R_s , or one symbol every $T=T_s$ seconds. To cope with delay spread, we construct a composite symbol by pre-pending a Cyclic Prefix (CP) T_{cp} seconds in duration to a new symbol D' of T_s' seconds in duration. D and D' contain the same PSK symbol, and convey the same information over the channel. The new composite symbol is now $T'=T_{cp}+T_s'$ seconds long. The CP contains no additional information, it is just a cyclic extension of the single symbol D'. Thus we still send one symbol of data over the channel every T' seconds. To maintain the payload data rate over the channel, we must send the new composite symbol at

Figure 2: Construction of composite symbol with a Cyclic Prefix CP pre-pended to a shortened data symbol D'.



the same rate as the original symbol:

$$T = T'$$

$$T_s = T_{cp} + T'_s$$

$$R'_s = \frac{R_s}{1 - T_{cp}/T_s}$$
(7)

It can be observed that $R'_s > R_s$, to account for the portion of the composite symbol allocated to the CP. For example with $R_s = 50$, $T_s = 0.02$, $T_{cp} = 0.002$, $R'_s = 50/(1 - 0.002/0.02) = 55.56$ symbols/second. Thus additional bandwidth is required to send the composite symbol including the cyclic prefix.

The increase in symbol rate does not directly affect BER performance if E_s/N_0 remains the same. For example if $Rs' = 2R_s$ we could send the symbol across the channel in $T_s/2$ seconds at power 2S, followed by $T_s/2$ seconds of silence. The energy per symbol E_s and BER would remain the same.

For the composite symbol, the transmitter power S' is spread between the CP and D'. Given a constant power S', the energy for the symbol D' is given by:

$$E'_{s} = \frac{S'}{R'_{s}}$$

$$= \frac{S'}{R_{s}} (1 - T_{cp}/T_{s})$$
(8)

For the link BER to be maintained the energy per symbol must be unchanged,

i.e. $E'_s = E_s$:

$$E_{s} = \frac{S'}{R_{s}} (1 - T_{cp}/T_{s})$$

$$\frac{S}{R_{s}} = \frac{S'}{R_{s}} (1 - T_{cp}/T_{s})$$

$$\frac{S}{N} = \frac{S'}{N} (1 - T_{cp}/T_{s})$$

$$\frac{S'}{N} = \frac{S}{N} \left(\frac{1}{1 - T_{cp}/T_{s}}\right)$$

$$SNR' = SNR - 10log_{10}(1 - T_{cp}/T_{s})$$

$$= SNR + L_{cp} \quad [dB]$$

$$L_{cp} = -10log_{10}(1 - T_{cp}/T_{s})$$
(9)

Thus to close the link with the composite symbol the S/N must be increased by a factor of $1/(1 - T_s/T_{cp})$ compared to our ideal modem, to account for the energy allocated to the CP. For example FreeDV 700E has $T_s = 0.02$, $T_{cp} = 0.006$, giving $L_{cp} = -10log10(1 - 0.006/0.02) = 1.55 dB$.

2.4 Bandwidth

Using the expressions above, we can estimate the total RF bandwidth of candidate waveforms:

$$B = \frac{R_s N_s}{(N_s - 1)(1 - T_{cp}/T_s)} \tag{10}$$

where R_s is the total symbol rate over the channel. For example for 700D, B = 700(8)/((8-1)(1-0.002/0.02)) = 888.89 Hz. In practice 700D has some extra bits allocated for frame synchronisation and auxiliary text, resulting in B = 944 Hz.

2.5 Latency

Latency is delay experienced by end users when using a speech processing system such as a FreeDV mode. Latency is an important trade off for real time, Push To Talk (PTT) speech communication. Speech compression and FEC tend to work better with latency, but perceptual quality tends to decrease whenever there is delay in conversational speech.

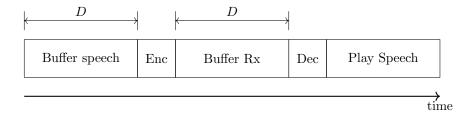
The algorithmic delay is defined as the number of seconds D of signal that must be collected in order to start processing. A typical speech codec will collect 20-40ms of speech samples before starting analysis. FEC codeword sizes spanning several seconds are common for HF data modes in order to ride over fades. All bits in the codewords must be received before FEC decoding starts. In FreeDV 700D, there is a one frame look ahead for pilot symbols, which also contributes to algorithmic delay.

Consider a FreeDV mode with algorithmic delay D seconds (Figure 3)

- 1. First we must collect D seconds of speech samples.
- 2. The speech samples are encoded and a buffer of D seconds of modem samples generated.
- 3. The modem samples are sent over the radio channel, where they are buffered at the receiver.
- 4. When a D second buffer of modem samples is collected at the receiver, the modem samples can be decoded to a buffer of output speech samples.
- 5. The output speech samples are played to a listener.

Latency is the time from when a speech sample enters the input buffer to when it is played at the receiver. If we assume infinite CPU such that the encode and decode times are zero, and zero propagation delay across the channel, the minimum latency experienced by an end user is twice the algorithmic delay, or 2D.

Figure 3: Latency of a waveform with algorithmic delay D seconds



2.6 Summary of FreeDV modes

Using the framework developed above, we can analyse the existing FreeDV waveforms, using the information in [1].

Mode	N_s	R_s	Ts	T'_s	T_{cp}	$L_p \text{ (dB)}$	L_{cp} (dB)
700C	3	75	0.013	0.013	0.000	1.77	0.00
700D	8	50	0.020	0.018	0.002	0.58	0.46
700E	4	50	0.020	0.014	0.006	1.24	1.55
datac4	5	50	0.020	0.014	0.006	0.97	1.38

Table 3: Summary of FreeDV waveforms, note the differences in the overheads L_p and L_{cp} . R_s and T_s is per-carrier. 700C is a parallel tone modem with no cyclic prefix, the modem frame is comprised of two pilot symbols and 4 data symbols

TODO: L_{il} estimate using lin2 modelling below, likely to be greater for 700C/E. We could also include N_c , total R_s , and SNR estimates.

2.7 HF Channel Model

A common two path HF channel model [2] is given by:

$$y(t) = x(t)G_1(t) + x(t-d)G_2(t)$$
(11)

where G_1 and G_2 are two time varying, complex, Gaussian filtered random variables with *Doppler Spread* bandwidth B_d Hz, d is the path delay in seconds. Other models with varying delay, number of paths, and fixed frequency offset components are also possible, for example Appendix B of [4].

As $B_d \ll R_s$ we assume G_1 and G_2 are complex constants for the duration of a single symbol. Expressed in discrete time for the current symbol:

$$y(n) = x(n)G_1 + x(n - dF_s)G_2$$
(12)

where F_s is the sample rate in Hz. Taking the z-transform:

$$Y(z) = X(z)G_1 + X(z)z^{-dF_s}G_2$$

$$\frac{Y(z)}{X(z)} = G_1 + z^{-dF_s}G_2$$

$$H(z) = G_1 + z^{-dF_s}G_2$$

$$H(e^{j\omega}) = G_1 + e^{-j\omega dF_s}G_2$$
(13)

Lets examine the effects of intersymbol interference due to the delay spread. Consider the transmitter sample x(0) where we transition from one PSK phase ϕ_1 to the next ϕ_2 . Near the transition we can define x(n) in terms of a step function s(n):

$$x(n) = \begin{cases} e^{j(\omega n + \phi_1)}, & n < 0 \\ e^{j(\omega n + \phi_2)}, & n \ge 0 \end{cases}$$

$$= s(n)e^{j(\omega n + \phi_2)} + (1 - s(n))e^{j(\omega n + \phi_1)}$$

$$s(n) = \begin{cases} 0, & n < 0 \\ 1, & n \ge 0 \end{cases}$$
(14)

where $\omega = 2\pi c R_s/F_s$ is the frequency of OFDM carrier c. Substituting into (12):

$$y(n) = G_1 s(n) e^{j(\omega n + \phi_2)} + G_1 (1 - s(n)) e^{j(\omega n + \phi_1)}$$

$$+ G_2 s(n - dF_s) e^{j(\omega (n - dF_s) + \phi_2)} + G_2 (1 - s(n - dF_s)) e^{j(\omega (n - dF_s) + \phi_1)}$$

$$\tag{15}$$

At n = 0 we have a mixture of both symbols:

$$y(0) = G_1 s(n) e^{j(\omega n + \phi_2)} + G_2 e^{j(\omega(n - dF_s) + \phi_1)}$$
(16)

However by $y(dF_s)$ the ISI from ϕ_1 has gone:

$$y(dF_s) = G_1 s(n) e^{j(\omega dF_s + \phi_2)} + G_2 e^{j\phi_2}$$
(17)

Or more generally for $n \geq dF_s$:

$$y(n) = G_1 s(n) e^{j(\omega n + \phi_2)} + G_2 e^{j(\omega (n - dF_s) + \phi_2)}$$

$$= e^{j(\omega n + \phi_2)} [G_1 + G_2 e^{-j\omega dF_s}]$$

$$= e^{j(\omega n + \phi_2)} H(e^{j\omega})$$
(18)

Thus if we start detecting y(n) after the longest delay term dF_s we can recover the transmitted PSK symbol without ISI, and equalise it by estimating a single complex coefficient $H(e^{j\omega})$. In practice detection means integration over a complete symbol T_s , therefore the symbol $e^{j\omega n + \phi_n}$ must be transmitted for $d + T'_s = T_{cp} + T'_s$ seconds, with the cyclic prefix length $T_{cp} \geq d$.

3 Waveform Improvements

In this section waveform improvements are presented.

The general strategy is to propose an innovation, and explore with analysis/maths and Octave simulation. Try low risk approaches to start with, then iterate. To simulate performance with voice codec, use a threshold of PER=0.1, BER=0.01.

3.1 Equalisation

Pilot symbols are used to the estimate the channel, and equalise (correct) the phase of the received symbols. We require an equalisation system that works with $B_d = 2$ Hz Doppler Spread that has a low implementation loss L_{il} on noisy channels, and has a reasonable latency (we can't use symbols far in the future).

If we detect symbols after ISI has settled, the channel for each OFDM carrier resolves to a single complex constant H_c . This can be considered a complex random variable with bandwidth B_d .

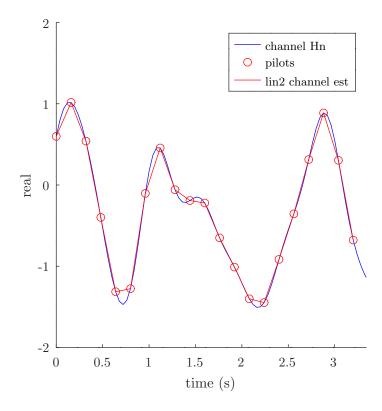
Consider the two path time domain channel model (12). Two additive terms of bandwidth B add linearly, so by linearity the result also has bandwidth B. The sum is a random modulation of bandwidth B_d about the symbol centre frequency. The Doppler bandwidth B_d therefore defines the bandwidth required for equalisation. One caveat - if B_d an appreciable fraction of R_s the DFT orthogonality may break down to some extent as energy falls into adjacent DFT bins.

FreeDV 700D samples pilots and hence H_c at $1/(N_sTs) = 6.25$ Hz. As we are sampling a complex signal, this implies a Nyquist bandwidth of 6.25 Hz, which should be adequate to recover H_c which has a maximum $B_d = 2$ Hz on the MPD channel. 700D currently uses a block average over a 2D array (4 pilots in time, across 3 carriers in frequency) of 12 pilots, this can be interpreted as

a 2D FIR filter with all coefficients $c_i = 1/12$. It is effective on MPP channels $(B_d = 1 \text{ Hz})$, but breaks down on MPD channels $(B_d = 2 \text{ Hz})$. This suggests a resampler with a wider bandwidth might enable a waveform similar to 700D to be used on MPD channels.

To explore pilot resampling algorithms, a simulation was written to evaluate candidate algorithms by comparing uncoded BER versus E_b/N_0 curves. One interpretation of resampling 4 pilots in time is a 4 point FIR filter. This was explored, along with the existing mean12 resampler (700D), and 2 point linear lin2 resampler (as used in FreeDV 700E). Figure 4 shows the lin2 resampler in action.

Figure 4: lin2 resampler in action for a MPD channel. The blue continuous line is the simulated channel H_c at each symbol, the red dots are the pilot symbols, and the red line the channel estimates from the linearly interpolated pilots. Just the real part is plotted.



Attempts were made to design 4 sample FIR filters (e.g. with a sinc() impulse response) however these performed poorly. The mean12 algorithm used for 700D works well on AWGN and MPP channels, but has a sluggish frequency

response, and can't follow fading with $B_d > 1$ Hz. However on AWGN and slower fading channels it filters the channel noise well, resulting in good low SNR performance. This is consistent with on air reports of 700D. The lin2 algorithm (700E) doesn't filter channel noise very well, but is hard to beat on fast fading channels, and even works with $B_d > 2$ Hz.

Attempts were therefore made to improve the performance of lin2 on AWGN and slower fading channels. Simple averaging of pilots from adjacent carriers is used in FreeDV 700D to reduce estimation noise. Consider (13) when the carriers are spaced R_s Hz apart such that $\omega_c = 2\pi c R_s / F_s$:

$$H(e^{j\omega_c}) = G_1 + G_2 e^{-j2\pi cR_s d}$$

$$H(e^{j\omega_{c-1}}) = G_1 + G_2 e^{-j2\pi cR_s d + 2\pi cR_s d}$$

$$H(e^{j\omega_{c+1}}) = G_1 + G_2 e^{-j2\pi cR_s d - 2\pi cR_s d}$$
(19)

We can see some symmetry in the RH term in the phase between carrier c-1 and carrier c+1 which supports averaging over adjacent carriers to estimate $H(e^{j\omega_c})$, especially when the term $2\pi R_s d$ is small. A more robust approach is to perform a least squares fit [3] of three equations with G_1 and G_2 as the two unknowns, and treating the three pilot samples centred around the current carrier as samples of the channel at three frequencies $H(e^{j\omega_{c-1}}), H(e^{j\omega_{c-1}}), H(e^{j\omega_{c+1}})$:

$$G_{1} + G_{2}e^{-j\omega_{c-1}dF_{s}} = H(e^{j\omega_{c-1}})$$

$$G_{1} + G_{2}e^{-j\omega_{c}dF_{s}} = H(e^{j\omega_{c}})$$

$$G_{1} + G_{2}e^{-j\omega_{c+1}dF_{s}} = H(e^{j\omega_{c+1}})$$

$$\begin{bmatrix} 1 & e^{-j\omega_{c-1}dF_{s}} \\ 1 & e^{-j\omega_{c}dF_{s}} \\ 1 & e^{-j\omega_{c+1}dF_{s}} \end{bmatrix} \begin{bmatrix} G_{1} \\ G_{2} \end{bmatrix} = \begin{bmatrix} H(e^{j\omega_{c-1}}) \\ H(e^{j\omega_{c}}) \\ H(e^{j\omega_{c+1}}) \end{bmatrix}$$

$$Ag = h$$

$$g = (A^{T}A)^{-1}A^{T}h$$

$$\overline{H(e^{j\omega_{c}})} = G_{1} + G_{2}e^{-j\omega_{c}dF_{s}}$$

$$(20)$$

where $\overline{H(e^{j\omega_c})}$ is the smoothed estimate of the channel at ω_c . Note that the channel delay d is actually an unknown (and indeed the entire model is an approximation of the real channel). It was found that in simulation, choosing d=0.002 or d=0.004 produced reasonable results, possibly due to the symmetry of the RHS of (13), and the dominance of channel over resampler noise at low SNRs. If d is approximated with a known value, the $(A^TA)^{-1}A^T$ term can then be precomputed as all the parameters of A are known.

This algorithm is denoted *lin2ls*. It's BER performance is plotted in Figure 5 and three resamplers summarised in Table 3.1.

The new *lin2ls* resampler has the following benefits:

1. Using a single waveform design, it can operate from AWGN to beyond MPP with low SNR performance similar to 700D.

Algorithm	Mode	Colour	AWGN	MPP	MPD
mean12	700D	blue	0.0	0.5	unusable
lin2	700E	green	1.5	2.0	2.0
lin2ls	700X	magenta	0.5	0.5	0.5

Table 4: Comparison of equaliser algorithms for $N_s=8$. The last three numbers are implementation loss in dB, smaller is better. 700X has the advantage of low implementation loss across channels with a single waveform, but is 0.5dB poorer than 700D on the (rare) AWGN channel. The 700E results are an approximation, as that waveform uses $N_s=5$.

- 2. On fast fading (Doppler Spread $B_d > 2$ Hz) channels it will outperform 700E at low SNRs.
- 3. The $N_s = 8$ pilot insertion rate means the pilot symbol loss $L_p = 0.58 \text{dB}$ is low, giving good low SNR performance.
- 4. Large N_s means the amount of bandwidth used per carrier is small, reducing on air RF bandwidth and giving us options for transmit diversity in the 2000 Hz SSB radio bandwidth.
- 5. The new estimator could be applied to the raw data modes to improve low SNR FreeDATA performance.
- 6. It uses 2 pilots in time centred around the current modem frame rather than 4 used in mean12 so will have lower algorithmic delay (one modem frame less) than 700D.

The algorithm used to combine adjacent carriers (20) is new and makes an assumption around the estimate of d, so it should be carefully tested OTA on real world channels using objective, controlled tests.

3.2 Multipath

This section WIP, currently in note form. For the n=2 diversity simulation (Figure 6), the signal was split into 2 copies, with half the power going to each copy. The 2nd copy was shifted 1000 Hz higher in frequency.

- 1. We are talking about fast fading here no much we can do about slow because latency
- 2. Maximum Ratio Combining (MRC) seems to get us about 0.5dB over Equal Gain Combining (EGC).
- 3. The curves represent the average BER across the entire simulation. In practice we are limited by the ability of the FEC to correct errors in a single FEC codeword which is limited by latency to a few 100 ms. So we need a way to test the PER and compare to existing waveforms to see

- if we have any gain. Perhaps simulate all carriers or even include LDPC code.
- 4. Does n=4 diversity give us any gains? We would need a lower code rate for that.
- 5. Current simulation is single carrier so a bit weak, might be best to test with multiple carriers.
- 6. Key question is independence of channel $H(e^{j\omega_c})$ at 1 kHz (ish) separation of narrow band carriers. This is actually difficult to simulate as with our model $H(e^{j\omega_c})$ is periodic.
- 7. n = 2 diversity might also cause PAPR problems as twice as many carriers, we should simulate this, and establish overall performance.
- 8. initial PER curves (all carriers) based on 10% per packet threshold show a 2dB gain over no diversity. 6dB off AWGN. Gain is greater at higher Eb/No is it possible to shift our operating point there, e.g. lower code rate? Goal is lower SNR I guess, we need model to investigate.
- 9. Clear from spectrogram that $H(e^{j\omega_c})$ are indeed correlated it's quite common to have the entire channel fall over at all frequencies. This limits the benefits from frequency diversity. This suggest we need to try time diversity (however we need a way to deal with latency).
- 10. First pass long latency (10 modem frame) PER results are very impressive, around 6dB over mean12 (700D). Rule I guess is interleaver twice the length of fading period so this makes sense. Losing 2 seconds of speech would have a significant cost. How could we architect this for minimum latency (2 and a bit seconds), e.g. buffering just one modem frame? How to make usable for PTT as well?
- 11. Good to include actual FEC code at some point, to test FEC simulation (just measuring BER for the packet).

3.3 Delay Spread (ISI)

- 1. We need a CP long enough to handle MPD (4ms plus guard)
- 2. Try longer T_s which will mean less overhead. However this implies lower R_s which may be impacted by frequency spreading effect of Doppler. Caveat (as in equalisation section) is possible issues with Doppler spread and frequency offset tracking as R_s reduces.
- 3. Measure implementation loss or EVM against ISI, we might be able to get away with some ISI, it is acceptable to have performance drop off for MPD, but it needs to be gradual rather than breaking.
- 4. 700C had just 13ms symbols but dealt with ISI pretty well this might be worth exploring.

3.4 Timing estimation

TODO: make sure the current algorithm is doing sensible things on HF channels with complex impulse responses and large delay spreads.

3.5 Acquisition

TODO: also include frequency offset estimation and tracking. Sensitivity of Doppler spread, freq offset errors with reduced R_s . Can we use othogonality property to track freq offset, e.g. iterative adjustments of offset to peak OFDM carriers?

4 Further Work

This section presents topics useful to explore in future.

- Can we include PAPR into model? What can we do about improving PAPR, e.g. successive clipper/filter of ECSSB.
- Expression for Fading channels, block error rate, why 2020 is a lemon.
- Test against simulations other channel models, for example Appendix B of [4].
- Table of FreeDV waveforms and values, plugged into formula, effect of increasing pilot symbol rate.
- Where we can gain, diversity, PAPR reduction, reduced overheads for fast fading and ISI (discuss)
- Wades MAP techniques (ref). This has a lot of promise, need an effective way to simulate and establish benefit with a modest amount of work. Can we combine MAP with extra bits for FEC? Index optimisation also a simple approach.
- Extending (20) to more carriers, it is essentially estimating the entire channel. Literature search, I'm sure this is nothing new. Determine if (20) is a reasonable approximation for real HF channels we have derived it from a simulation model.

5 References

- [1] Codec 2 repo, modem codec frame design spreadsheet. https://github.com/drowe67/codec2/blob/main/doc/modem_codec_frame_design.ods.
- [2] ITU-R F.1487: Testing of HF modems with bandwidths of up to about 12 kHz using ionospheric channel simulators, 2000.

- [3] P Bergadà, RM Alsina-Pagès, JL Pijoan, M Salvador, JR Regué, D Badia, and S Graells. Digital transmission techniques for a long haul HF link: DSSS versus OFDM. *Radio Science*, 49(7):518–530, 2014.
- [4] ES ETSI. 201 980 v4. 2.1 (2021-01) digital radio mondiale (drm). System Specification. European Broadcast Union.
- [5] David Rowe. FreeDV-020 WP4000 Low SNR Mode.

Figure 5: Uncoded BER performance curves for equaliser algorithms over various channels. mean12 is the algorithm used for 700D, and lin2 for 700E. Note mean12 (blue) is very close to theory for AWGN but breaks down on MPP. The lin2ls algorithm performs quite well on MPP and MPD, and about 0.5dB poorer than mean12 on AWGN.

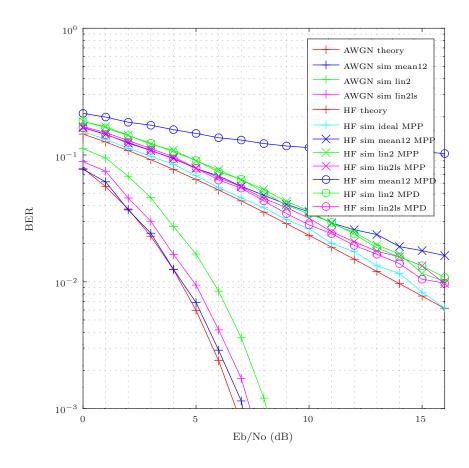


Figure 6: n=2 diversity simulation results, all using the lin2lks resampler and the MPP channel. At BER=0.1 (where FEC usually falls over) n=2 diversity MRC (cyan) has a gain of about 2dB over no diversity (purple). At BER=0.05 about 3dB gain.

