

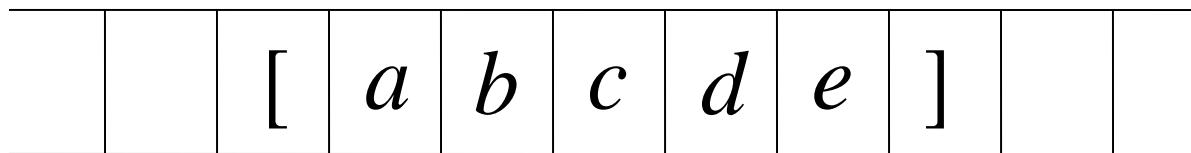
# Linear Bounded Automata LBAs

Linear Bounded Automata (LBAs)  
are the same as Turing Machines  
with one difference:

The input string tape space  
is the only tape space allowed to use

# Linear Bounded Automaton (LBA)

Input string



Left-end  
marker

Working space  
in tape

Right-end  
marker

All computation is done between  
end markers

We define LBA's as NonDeterministic

## Open Problem:

NonDeterministic LBA's  
have same power with  
Deterministic LBA's ?

# Example languages accepted by LBAs:

$$L = \{a^n b^n c^n\}$$

$$L = \{a^{n!}\}$$

LBA's have more power than NPDA's

LBA's have also less power  
than Turing Machines

# The Chomsky Hierarchy

# Unrestricted Grammars:

Productions

$$u \rightarrow v$$



String of variables  
and terminals

String of variables  
and terminals

Example unrestricted grammar:

$$S \rightarrow aBc$$

$$aB \rightarrow cA$$

$$Ac \rightarrow d$$

## Theorem:

A language  $L$  is recursively enumerable if and only if  $L$  is generated by an unrestricted grammar

# Context-Sensitive Grammars:

## Productions

$$u \rightarrow v$$



String of variables  
and terminals

String of variables  
and terminals

and:  $|u| \leq |v|$

The language  $\{a^n b^n c^n\}$

is context-sensitive:

$$S \rightarrow abc \mid aAbc$$

$$Ab \rightarrow bA$$

$$Ac \rightarrow Bbcc$$

$$bB \rightarrow Bb$$

$$aB \rightarrow aa \mid aaA$$

Theorem:

A language  $L$  is context sensitive  
if and only if  
 $L$  is accepted by a Linear-Bounded  
automaton

Observation:

There is a language which is  
context-sensitive  
but not recursive

# The Chomsky Hierarchy

Non-recursively enumerable

Recursively-enumerable

Recursive

Context-sensitive

Context-free

Regular