Homework 3: Conjugate Gradient

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3.1

This part of the report is written in a seperate pdf file named "hw3.pdf" found within the same directory as this file.

3.2

The following is a table showing time in seconds, num iter represents the number of iterations it took for the norm of the residual residual to reach 10^{-8} and N is the size of the problem.

N	$_{ m time}$	num iter
4	0.012270	79
8	0.076803	215
16	0.737514	578
32	7.197663	1433
64	248.338108	2622
128	297.793319	1526

Below is a plot for the highest resolution resulting function u(x) for N=128. This plot matches what I would expect for the solution of this problem as the analytical solution to this problem is $u(x_1, x_2) = \sin(\pi x_1)\sin(\pi x_2)$, as shown in "hw3.pdf". There is disrepancy as the analytical solution should have its maximum value at 1 in the middle of the plot, this discrepancy is likely due to the limited convergence set by us.

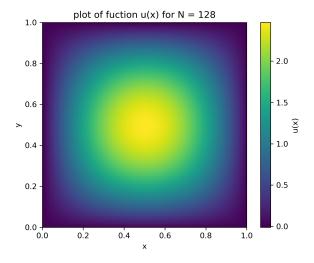


Figure 1:

3.3

In figure 2 chose to plot a semilogy plot. I plotted the error bound given in the question in dotted line and the actual error I computed, assuming the true solution to the problem is the final step in the iteration. In my plot you can see that my error is not exactly bound by the error bound in later iterations. The curves do however look like a bit like a scaled version of the bounding functions, following a vaguely similar scaled trajectory. What is good is that the error decreases as the number of iterations increases.

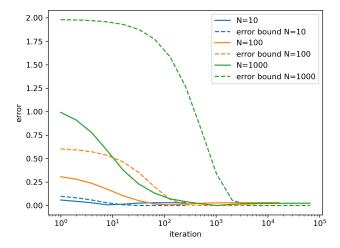


Figure 2: