

CS 340

Bitwise Operations

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Q1

~Code~
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Updates

1. Exam 1 scores are released.
 - a. More information on Campus Wire
1. MP 3 - PNG due today
1. MP 4 - UTF-8 out today (due next Tuesday)

Bitwise Operations

Today's LGs - Build on your mental model of how data is stored and interpreted on a computer (1's and 0's).

Be able to converse about bits

Be able to shift bits

Be able to apply logical operations at a bit level

Be able to use bit operations to isolate the bits you need

Be able to convert between code points and UTF-8

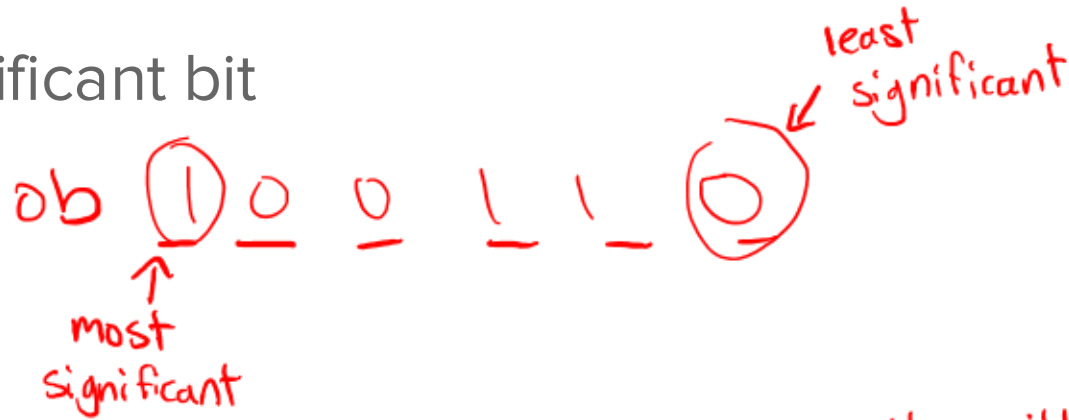
Agenda

1. Addressing misconceptions
 - a. Important terms
 - b. Representing bits versus interpreting bits
2. Bitwise Operations
 - a. Bit shifting
 - b. Bit logic operations
2. Bit Mask
3. MP4 - UTF-8

Important Terms 0b01

Bit Vector - a fixed length sequence of bits

Most/least significant bit



Clear

↳ verb - replace a bit with 0 OR replace all bits with 0

Important Terms Ob10

ith bit - The place in a bit vector

0b 01001001
 ↑ ↑
 1st 2nd
 ↑ ↑
 1st 2nd

Set - set a bit = make it 1

The 3rd bit is set = that bit is 1
a data structure

Zero - opposite of 1

a bit vector of all 0's
a single bit of value 1

> another
word to
mean clear

Representing Bits Versus Interpreting Bits

information is stored in 1's and 0's

Hex use case 1 - to indicate the 1's and 0's set

Hex use case 2 - to represent an amount

Example 0b01

Address	1000	1001	1002	1003	1004	1005	1006	1007	1008	1009
Value	F6	DC	6D	CD	58	AF	22	49	BC	E3

↓
indicates
0010 0010

but could represent
the middle of an int value

Example 0b10

bit vector =

$$01001100 = 76 = 0x4C$$

↓ amount

but the 1's and 0's could mean something else

What could the value at address 1006 be?

Address	1000	1001	1002	1003	1004	1005	1006	1007
Value	F6	DC	6D	CD	58	AF	22	49

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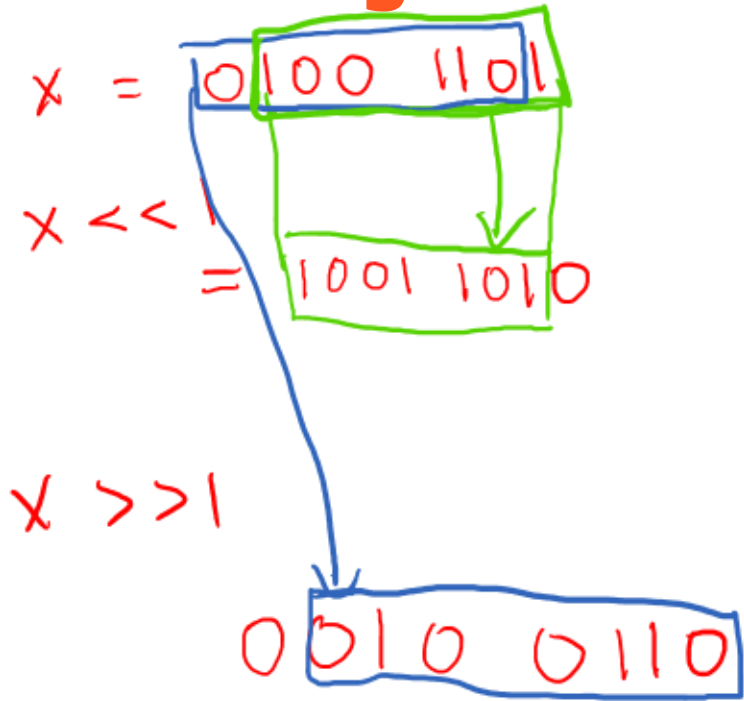
- A) A bit vector
- B) An ascii character
- C) The middle byte of an int
- D) Part of a struct

Bitwise Operations in C

1. Bit shifting << or >>

1. Bit operations (AND, OR, XOR, NOT)

Bit Shifting - shift bits left or right and add 0's



Use
unsigned!

Bit Shifting Example in C

```
int main() {  
    char x = 0x05;  
    x = x << 2;  
    printf("%#x", x);  
}
```

~~0000 0101~~

0001 0100

0x14

What prints?

```
int main() {  
    char x = 0x1E;  
    x = x >> 3;  
    printf("%#x", x);  
}
```

0001 1110
↓
0000 0011

0x03

- A) 0x01
- B) 0xE0
- C) 0x03
- D) 0x0E

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What prints (challenge)?

```
int main() {  
    int x = 6;   
    x = x << 1;  
    printf("%i", x);  
}
```

Handwritten annotations:
- An arrow points from the number 6 to the binary representation 00...0110.
- Another arrow points from the shift amount 1 to the binary representation 00...1100.

- A) 0x0C
- B) 0x12
- C) 12**
- D) 24

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Bit Operations

logic	C
AND	$\&$
OR	$ $
XOR	\wedge
NOT	\sim

9 AND 1

$$\begin{array}{r} 1001 \\ \& 0001 \\ \hline 0001 \end{array}$$

9 XOR 1

$$\begin{array}{r} 1001 \\ \wedge 0001 \\ \hline 1000 \end{array}$$

Bit Operations Example in C

```
int main() {  
    char x = 0x0F;   
    char y = 0x13;   
    char output = x | y;   
    printf("%#x", output);  
}
```

→ 0000 1111
→ 0001 0011 OR
0001 1111

→ 0x1F

What prints?

```
int main() {  
    char x = 0x0F;  
    char y = 0x13;  
    char output = x ^ y;  
    printf("%#x", output);  
}
```

Handwritten XOR calculation:

$$\begin{array}{r} 0000\ 1111 \\ \text{xor } 0001\ 0011 \\ \hline 0001\ 1100 \end{array}$$


Handwritten result: 0x1C

- A) 0x28
- B) 0x1F
- C) 0x30
- D) 0x1C

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What 8 bit value does this produce?

$((\sim 0) \ll 3)$

Handwritten annotations: A red squiggle under the 0 with an arrow pointing to it labeled "NOT". Red arrows from the parentheses point to two groups of four vertical lines, with an arrow pointing to the second group labeled "3".

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- A) 0000 0111
- B) 0000 0011
- C) 1111 1000
- D) 1111 1011

What 8 bit value does this produce?

$((\sim 0) \ll 3) \wedge ((\sim 0) \ll 5)$

1111 1000 XOR 1110 0000

A) 1111 1000

B) 1110 0000

C) 0001 1000

D) 0011 1000

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I want just the middle 4 bits from a byte to remain.

Mask!

$$X = 10010011$$

$$\text{Mask} = 00011000$$

$$X \& \text{mask} = 00010000$$

How would I get only the 8 least significant bits from x? goal: 0x00 00 00 F0

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Q8

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```
int main() {  
    //4 bytes - 8 hex digits  
    int x = 0x1560A0F0;  
    int mask = 0x000000FF;  
    int output = x & mask;  
    printf("%#x", output);  
}
```

```
int main() {  
    //4 bytes - 8 hex digits  
    int x = 0x1560A0F0;  
    int mask = 0xFFFFFFFF00;  
    int output = x ^ mask;  
    printf("%#x", output);  
}
```

Okay... but why?

To use bits within a byte!

UTF-8

bit sets

UTF-8

Char - 1 byte value — values 0-255

ASCII - mapping from 0-127 values to characters

Unicode - bigger ascii table!

UTF-8 - variable length encoding for unicode



UTF-8


Code Point - a number that can be held in an int

UTF-8 - 1-4 bytes representing a code point

(Encoding) Code point -> UTF-8

~~3001 -> [0x67][78][96]~~

code point	# of bits
2	2 bits
512	10 bits
0x1F33D	17 bits



Bits needed	Groups used
0-7	1
8-11	2
12-16	3
17-21	4

(Encoding) Code point -> UTF-8

group 1 = 0xxxx xxxxx
group 2 = 110x xxxxx 10xx xxxxx
group 3 = 1110 xxxxx 10xx xxxxx 10xx xxxxx
group 4 = 1111 0xxxx 10xx xxxxx 10xx xxxxx 10xx xxxxx

Byte	Meaning
0xxxxxxx	only byte of character
10xxxxxx	second, third, or fourth byte of a character
110xxxxx	first byte of a two-byte character
1110xxxx	first byte of a three-byte character
11110xxx	first byte of a four-byte character
11111xxx	invalid

Bits needed	Groups used
0-7	1
8-11	2
12-16	3
17-21	4

(Encoding) Code point -> UTF-8

'a' = 0x61 = 0110 0001 = 7 bits = group 1

0 1 1 0 0 0 0 1
↑
header

Byte	Meaning
0xxxxxxx	only byte of character
10xxxxxx	second, third, or fourth byte of a character
110xxxxx	first byte of a two-byte character
1110xxxx	first byte of a three-byte character
11110xxx	first byte of a four-byte character
11111xxx	invalid

Bits needed	Groups used
0–7	1
8–11	2
12–16	3
17–21	4

(Encoding) Code point -> UTF-8

ஸ்

1011 1011 1001 = 3001
12 bits

1110 0000 1010 1110 1011 1001

fill in
the rest
w/0's

Byte	Meaning
0xxxxxxx	only byte of character
10xxxxxx	second, third, or fourth byte of a character
110xxxxx	first byte of a two-byte character
1110xxxx	first byte of a three-byte character
11110xxx	first byte of a four-byte character
11111xxx	invalid

Bits needed	Groups used
0-7	1
8-11	2
12-16	3
17-21	4

If I need 9 bits to represent a code point, how many bytes will I need to encode it to UTF-8?

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Bits needed	Groups used
0–7	1
8–11	2
12–16	3
17–21	4

How many X slots are there in a 4-group UTF-8 character?

21

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Byte	Meaning
0xxxxxxx	only byte of character
10xxxxxx	second, third, or fourth byte of a character
110xxxxx	first byte of a two-byte character
1110xxxx	first byte of a three-byte character
11110xxx	first byte of a four-byte character
11111xxx	invalid

Bits needed	Groups used
0–7	1
8–11	2
12–16	3
17– <u>21</u>	4

(Decoding) Code point -> UTF-8

Byte	Meaning
0xxxxxxx	only byte of character
10xxxxxx	second, third, or fourth byte of a character
110xxxxx	first byte of a two-byte character
1110xxxx	first byte of a three-byte character
11110xxx	first byte of a four-byte character
11111xxx	invalid

Bits needed	Groups used
0–7	1
8–11	2
12–16	3
17–21	4

(Decoding) Code point -> UTF-8

0000 1000 1110 0100 1000 0001 1001 0000

✓
1 character

2nd character

~~1000~~ 1000 0000
1000 0000
1111 1111

Byte	Meaning
0xxxxxxx	only byte of character
10xxxxxx	second, third, or fourth byte of a character
110xxxxx	first byte of a two-byte character
1110xxxx	first byte of a three-byte character
11110xxx	first byte of a four-byte character
11111xxx	invalid

Bits needed	Groups used
0–7	1
8–11	2
12–16	3
17–21	4

MP4 - UTF-8

~ 11111 0

~ ~~11111~~

~ 0 0 0 0 0 1

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