Therefore

Therefore, we approximate the log-likelihood as:

Not sure if this is 100% accurate as it is not clear that is independent of the other y’s in the same location, leading to the multinomial distribution.