

Building Game Theoretical Software in a Research Environment

And applying it to healthcare modelling

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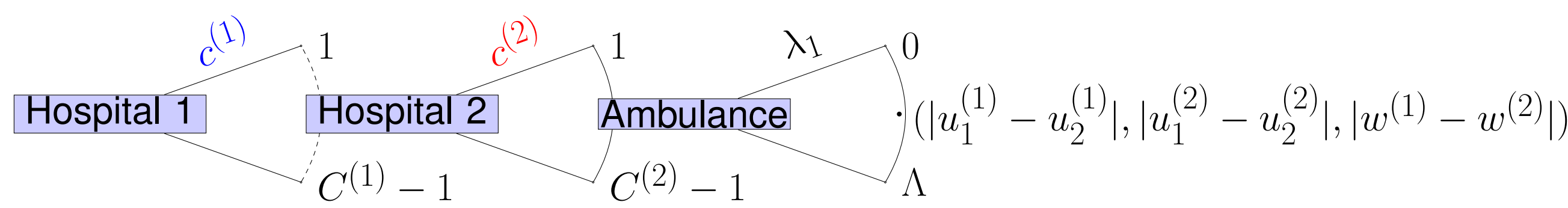


Figure 1: Underlying Stackelberg Game

Sage, Open Source Software

Sage: "Creating a viable free open source alternative to Magma, Maple, Mathematica and Matlab". Ref? The areas of Game Theory that we decided to implement in Sage were Matching Games, Co-operative Games and Normal Form Games. Matching Games allow us to solve problems where players need to be paired with each other, but they have their own preferences. We normally look for stable matching where no player has any incentive to change their pairing. Co-operative Games are used in situations where players each contribute to a system and those seperate contributions require their own payoff. Normal Form Games involve players choosing different strategies against each other and obtaining a payoff. Nash equilibria occur when no player has any incentive to change which strategy they play.

Markov Chain

Stackelberg game

The issue of waiting times for ambulances at at two hospitals can be modelled as a simple Stackelberg game where each hospital has its own AE and Ward. Patients arrive at the AE at rate λ and if there is space in the queue they join it. If there is no space in the queue that patient is lost. Each patient

has an AE service time, μ , which represents how long their treatment in AE will last. A proportion, p , of patients are then dismissed immediately. Those who are not dismissed are admitted to the ward if there is space, otherwise they will wait in AE, continuing to occupy a bed. Once admitted, they are treated in the ward with a service time $\hat{\mu}$ and then dismissed without delay.

Limitations of MC

The main problem with the Markov Chain approach is that calculating the payoffs required for the associated Normal Form Game is very CPU intensive. It therefore required use of the Cardiff Univeristy supercomputer, RAVEN. If the Normal Form Games themselves became too large, solving them to obatin Nash Equilibria could also take a significant amount of time.

Markov Decision Process

A Markov Decision Process is a model of decision making in a dynamic framework in which a decision maker makes decisions based on a particular system state [?]. The process is that an agent starts off in a particular state, makes a decision, and then has a probabilistic transition whose probabilities may depend on the previous decision.

Q-Learning

Q-learning is the process of assigning a state-action value or Q-value to the combination of being in a state, taking an action and observing a reward. The Q-value is then updated by assessing the maximum value of being in the new state. The higher the Q-value the more likely a player is to choose action a when in state s .