## Learning Objective Assessment: I2 (version 3)

MATH2603: Discrete Mathematics

I2: I can determine the output of a recursive algorithm for small input values, and use pattern recognition to determine the output in general. I can list elements contained in a recursively defined set, or give a recursive definition of an explicitly defined set.

1. A recursive algorithm is given below; the algorithm takes as input a pair (b, a) of natural numbers. Determine the output of GogoRhythm on inputs (0,3), (1,3), (2,3), and (4,3). Then state in a sentence what GogoRhythm does in general.

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GogoRhythm(b,a)

if b=0:
    Return( 1 )
r:= GogoRhythm(a,b-1)
Return( a*r )
```

2. Consider the function  $f: \mathbb{N} \to \mathbb{R}$  which is defined below. Find the values of f(n) for  $n \in \{1, 2, 3, 4, 5\}$ , then give a formula for the output in general (you may use any functions we have used in class).

$$f(n) = \begin{cases} 0 & \text{if } n = 0 \\ 0 & \text{if } n = 1 \\ 1 + f(n-2) & \text{if } n > 1 \end{cases}$$

3. Let  $A = \{a, b, c\}$ . Let  $S \subset A^*$  be the set of strings over A in which no a ever appears to the right of a b or a c: so you can never see a substring ... bca ..., but ... abcbb ... is acceptable. Give a list of six different elements of S. Then give a recursive definition for S.

Place work in this box.	Continue on back if needed.
Critoria for Satisfact	ory: On questions 1 (resp. 2), no errors may be present in the computation

Criteria for Satisfactory: On questions 1 (resp. 2), no errors may be present in the computation of outputs of the algorithm (resp. function). On question 3, all strings listed must be valid elements of  $A^*$ . Of the three questions, at least two of three generalizations must be correct.