MATHIZIO: HOMEWORK SOLUTIONS 82.5

1.
$$\frac{d}{dx} \left[(1+x)^{15} \right] = 15(x+1)^{14}$$

3.
$$\frac{d}{dx} \left[(3-2x)^5 \right] = 5(3-2x)^4(-2)$$

5.
$$\frac{d}{dx} \left[(x^3 - 2x^2 + 3x + 1)^n \right] = 11 \left(x^3 - 2x^2 + 3x + 1 \right)^n \left(3x^2 - 4x + 3 \right)$$

7.
$$\frac{d}{dx} \left[(x+3)^{-5} \right] = \frac{-5}{(x+3)^6}$$

9.
$$\frac{d}{dx} \left[sin(x^2 + x) \right] = cos(x^2 + x)(2x+1)$$

11.
$$D_{\chi} \left[\cos^3 \chi \right] = -3\cos^2 \chi \sin \chi$$

13.
$$D_{x}\left[\left(\frac{x+1}{x-1}\right)^{3}\right] = 3\left(\frac{x+1}{x-1}\right)^{2}\left(\frac{-2}{(x-1)^{2}}\right)$$

15.
$$D_{x} \left[\cos \left(\frac{3x^{2}}{x+2} \right) \right] = -\sin \left(\frac{3x^{2}}{x+2} \right) \cdot \left[\frac{(x+2)(6x) - 3x^{2}(1)}{(x+2)^{2}} \right]$$

17.
$$D_{x}\left[(3x-2)^{2}(3-x^{2})^{2}\right] = 2(3x-2)(3)(3-x^{2})^{2} + (3x-2)^{2}(2)(3-x^{2})(-2x^{2})$$

19.
$$D_{\chi}\left[\frac{(\chi+1)^2}{3\chi-4}\right] = \frac{(3\chi-4)}{2(\chi+1)} - \frac{(\chi+1)^2}{(3\chi-4)^2}$$

$$21.$$
 $y' = 2(x^2 + 4)(2x)$

23.
$$D_t\left(\left[\frac{3t-2}{t+5}\right]^3\right) = 3\left(\frac{3t-2}{t+5}\right)^2 \cdot \frac{(t+5)(3)-(3t-2)}{(t+5)^2}$$

25.
$$\frac{d}{dt} \left[\frac{(3t-2)^3}{t+5} \right] = \frac{(t+5)(3)(3t-2)^2(3) - (3t-2)^3}{(t+5)^2}$$

27.
$$\frac{dy}{dx} = 3\left(\frac{\sin x}{\cos 2x}\right)^2 \frac{\cos(2x)\cos(x) + \sin(x)\sin(2x)}{\left(\cos 2x\right)^2}$$

29.
$$f'(x) = 3\left(\frac{\chi^2+1}{\chi+2}\right)^2 \cdot \frac{(\chi+2)(2\chi) - (\chi^2+1)}{(\chi+2)^2}$$

 $f'(3) = 3\left(\frac{10}{5}\right)^2 \left(\frac{5\cdot 6-10}{25}\right) = \frac{3\cdot 4\cdot 20}{25} = \frac{48}{5}$

31.
$$F'(t) = cos(t^2 + 3t + 1)(2t + 3)$$

 $F'(1) = 5 cos(5)$

33.
$$D_{x} \left[sin^{4} (x^{2} + 3x) \right] = 4 sin^{3} (x^{2} + 3x) (2x + 3)$$

35.
$$D_t[\sin^3(\cos t)] = 3\sin^2(\cos t) \cdot (\cos(\cos t))(-\sin t)$$

37.
$$D_{\Theta}\left[\cos^{4}\left(\sin(\Theta^{2})\right)\right] = 4\cos^{3}\left(\sin(\Theta^{2})\right)\left(-\sin\left(\sin(\Theta^{2})\right)\right)\cos(\Theta^{2}).(2\Theta)$$

$$\frac{39}{dx} \left[\sin(\cos(\sin(2x))) \right] = \cos[\cos(\sin(2x))] \left(-\sin[\sin(2x)] \right)$$

$$\cdot \cos(2x) \cdot 2$$

43.
$$(fg)'(2) = f'(2)g(2) + f(2)g'(2) \approx 1 \cdot 1 + 3 \cdot 0 = 1$$

45.
$$(f \circ g)'(6) = f'(g(6)) \cdot g'(6) \approx f'(2) \cdot g'(6) \approx 1 \cdot -1 = -1$$

47.
$$D_x(F(2x)) = 2F'(2x)$$

49.
$$D_{+}((F(t))^{-2}) = \frac{-2}{(F(t))^{3}} \cdot F'(t)$$

51.
$$\frac{d}{dz} \left[(1+F(2z))^2 \right] = 2(1+F(2z)) \cdot F'(2z) \cdot (2)$$

53.
$$\frac{d}{dx}(F(\cos x)) = F'(\cos x) \cdot (-\sin x)$$

55.
$$D_x(+an(F(2x))) = sec^2(F(2x)) \cdot F'(2x) \cdot 2$$

55.
$$D_x(f(x)) = sec^2(F(2x)) \cdot F'(2x) \cdot 2$$

57. $D_x(F(x) \cdot sin^2(F(x))) = F'(x) \cdot sin^2(F(x)) + F(x) \cdot 2sin(F(x))$
 $\cdot cos(F(x)) \cdot F'(x)$

59.
$$g'(x) = -\sin(f(x)) \cdot f'(x) \Rightarrow g'(0) = -\sin(1) \cdot 2 = -2\sin(1)$$