MATH1220: Midterm 2 Practice Problems

The following are practice problems for the second exam.

1. Evaluate the following integrals:

(a)
$$\int xe^{3x} dx = \frac{e^{3x}}{3} \left(x - \frac{1}{3}\right) + C$$

(b)
$$\int x^2 \cos x \, dx = (x^2 - 2) \sin x + 2x \cos x + C$$

(c)
$$\int \cos^3 x \, dx = \sin x - \frac{1}{3} \sin^3 x + C$$

(d)
$$\int \tan^4(2x) \, dx = \frac{1}{6} \tan^3(2x) - \frac{1}{2} \tan(2x) + x + C$$

(e)
$$\int \sin(3x)\sin(9x) dx = \frac{-1}{24}(\sin(12x) + 2\sin(-6x)) + C$$

(f)
$$\int \frac{x^2 dx}{\sqrt{16 - x^2}} = 8\sin^{-1}(x/4) - 4\sin(2\sin^{-1}(x/4)) + C = 8\sin^{-1}(x/4) - \frac{1}{2}x\sqrt{16 - x^2} + C$$

(g)
$$\int \frac{dx}{\sqrt{x^2 + 4x + 5}} = \ln|\sqrt{x^2 + 4x + 5} + x + 2| + C = \sinh^{-1}(x + 2) + C$$

(h)
$$\int \frac{x}{4x - x^2} dx = \ln|4 - x| + C$$

(i)
$$\int \frac{5x}{2x^3 + 6x^2} dx = \frac{5}{6} (\ln|x| - \ln|2x + 6|) + C$$

(j)
$$\int \frac{x^3 + x^2}{x^2 + 5x + 6} = \frac{x^2}{2} - 4x - 4\ln|x + 2| + 18\ln|x + 3| + C$$

(k)
$$\int \frac{3x+13}{x^2+4x+3} dx = 5 \ln|x+1| - 2 \ln|x+3| + C$$

2. Compute the following limits:

(a)
$$\lim_{x \to 1} \frac{x^2 - 2x + 1}{\sin(\pi x)} = 0$$

(b)
$$\lim_{x\to 0} \frac{e^x - e^{-x}}{2\sin x} = 1$$

3. Find an algebraic expression for $\tan(\sin^{-1}(x/3))$. Answer: $\frac{x}{\sqrt{9-x^2}}$

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