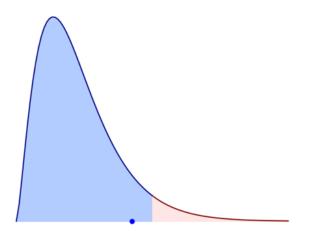
Basics of Machine Learning

Dmitry Ryabokon, github.com/dryabokon





Lesson 06 Statistical ML



Statistical ML

Summary

- P- Value and null hypothesis significance testing
- Chi-squared test
- T-test
- Feature importance
- Feature correlation
- Hashing
- Variance Inflation Factor

Statistical ML

Tutorials

- ex_06a_test_chi2.py
- ex_06a_test_normality.py
- ex_06a_test_student_one_var.py
- ex_06a_test_student_two_vars.py
- ex_06b_feature_correlation.py
- ex_06b_feature_importance.py

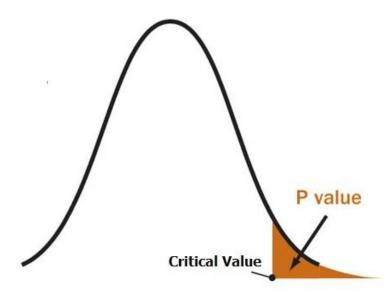
Statistical significance

- The result/value has **statistical significance** if it is unlikely to occur under hypothesis H
- significance level α is probability of false rejecting the hypothesis H (while it was true)

P-Value: probability value or asymptotic significance

how likely your data/experiment is occurred under hypothesis H

A p-value is an area in the tail of a distribution that tells you the probability of a result happening by chance



P-Value: probability value or asymptotic significance

how likely your data/experiment is occurred under hypothesis H

The p-value gives us the probability of observing what we observed, given a hypothesis is true

Small p-value has significance, it tells that hypothesis does not explain the experiment

```
If (p_value <= α)
    reject H
    data is statistically significant.
else:
    accept H</pre>
```

P-Value: probability value or asymptotic significance

how likely your data/experiment is occurred under hypothesis H

Example: p-value == 0.05 => the experiment has 5% or lower chance of occurring under hypothesis H

p-value significance		How likely experiment data is occurred under hypothesis H		
[0 0.01]	High significance	Highly unlikely to occur		
[0.01 0.05]	Strong significance			
[0.05 0.10]	Marginal significance			
[0.10	Low significance	Very likely to occur		

P-Value: probability value or asymptotic significance

p-value depends on the statistical test you are using to test your hypothesis

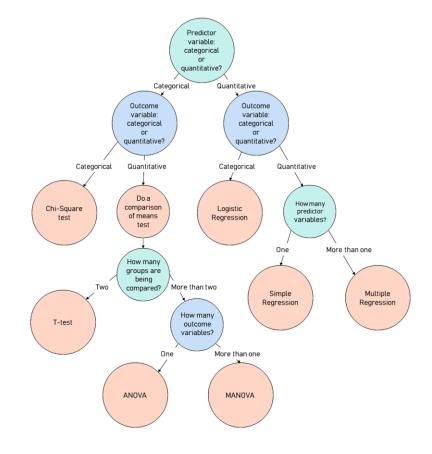
There are four main test statistics you can use in a hypothesis test.

Z-Test

T-Test

ANOVA

Chi-Square Test



Chi2 test

Chi-Square Test

Pearson's Chi-Square test for independence between categorical variables Goal: conclude if two variables are related to each other

 $X^2 = \sum [(observed-expected)^2 / expected]$

Chi-Square Test

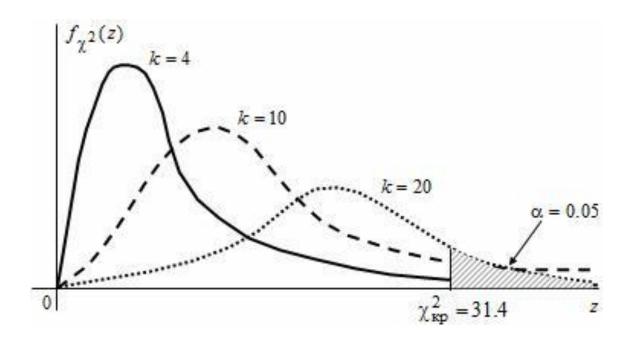
Если гипотеза о согласии наблюдаемых и ожидаемых частот верна, то, при большом количестве наблюдений, выражение

(observed-expected) / sqrt(expected)

имеет стандартное нормальное распределение

нормальность будет проявляться только при достаточно больших частотах. В статистике принято считать, что общее количество наблюдений (сумма частот) должна быть не менее 50 и ожидаемая частота в каждой группе должна быть не менее 5. Только в этом случае величина, показанная выше, имеет стандартное нормальное распределение.

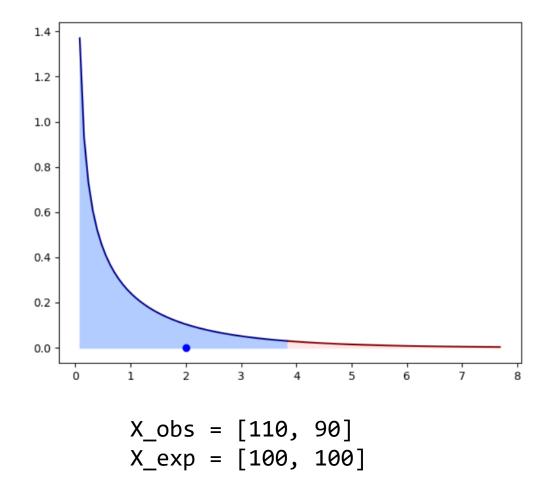
Chi-Square Test



Число степеней свободы к	Уровень значимости сс						
	0,01	0,025	0,05	0,95	0,975	0,89	
1	6,6	5,0	3,8	0.0039	0,00098	0,00016	
2 3 4 5 6 7	9,2	7,4	6,0	0,103	0.051	0,020	
3	11.3	9,4	7,8	0.352	0,216	0,115	
4	13,3	11,1	9,5	0,711	0,484	0,297	
5	15,1	12,8	11,1	1,15	0,831	0,554	
6	16,8	14,4	12,6	1,64	1,24	0,872	
7	18,5	16,0	14,1	2,17	1,69	1,24	
8	20,1	17,5	15,5	2,73	2,18	1,65	
8 9	21,7	19,0	16,9	3,33	2,70	2,09	
10	23,2	20,5	18,3	3,94	3,25	2,56	
11	24,7	21,9	19,7	4,57	3,82	3,05	
12	26,2	23,3	21,0	5,23	4,40	3,57	
13	27,7	24,7	22,4	5,89	5,01	4,11	
14	29,1	26,1	23,7	6,57	5,63	4,66	
15	30,6	27.5	25,0	7,26	6,26	5,23	
16	32,0	28,8	26,3	7,96	6,91	5,81	
17	33,4	30,2	27,6	8,67	7,56	6,41	
18	34,8	31,5	28,9	9,39	8,23	7,01	
19	36,2	32,9	30,1	10,1	8,91	7,63	
20	37,6	34,2	31,4	10,9	9,59	8,26	
21	38,9	35,5	32,7	11,6	10,3	8,90	
22	40,3	36,8	33,9	12,3	11,0	9,54	
23	41,6	38.1	35,2	13,1	11,7	10,2	
24	43,0	39,4	36.4	13,8	12,4	10,9	
25	44,3	40,6	37,7	14,6	13,1	11,5	
26	45,6	41,9	38,9	15,4	13,8	12,2	
27	47,0	43,2	40,1	16,2	14,6	12,9	
28	48,3	44,5	41,3	16,9	15,3	13,6	
29	49,6	45,7	42,6	17,7	16,0	14,3	
30	50,9	47,0	43,8	18,5	16.8	15,0	

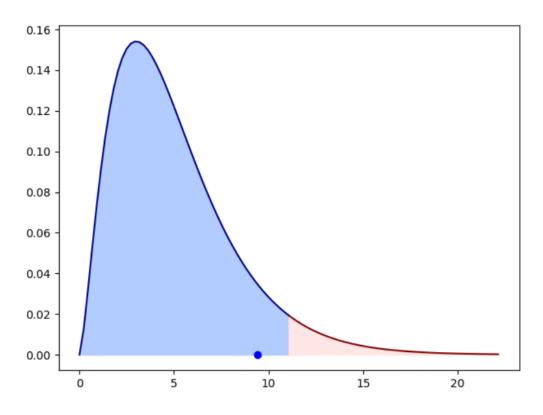
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Chi-Square Test





Chi-Square Test





T-test

T-Test

Статистический метод, который позволяет сравнивать средние значения двух выборок и на основе результатов теста делать заключение о том, различаются ли они друг от друга статистически или нет.

Для проведения теста, необходимо, чтобы данные выборок имели распределение близкое к нормальному.

Для этого существуют методы оценки, которые позволяют сказать, допустимо ли в данном случае полагать, что данные распределены нормально или нет. Например *график квантилей (qqplot) или тест Шапиро-Уилка*

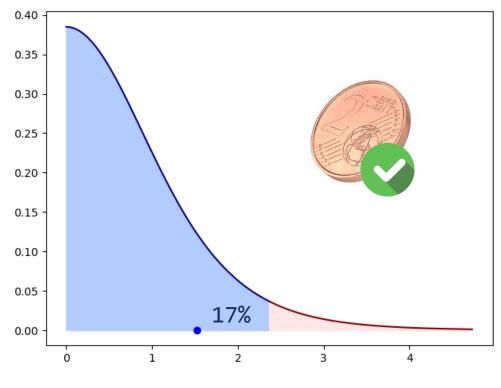
T-Test: one sample test

сравнение выборочного среднего с заданным значением

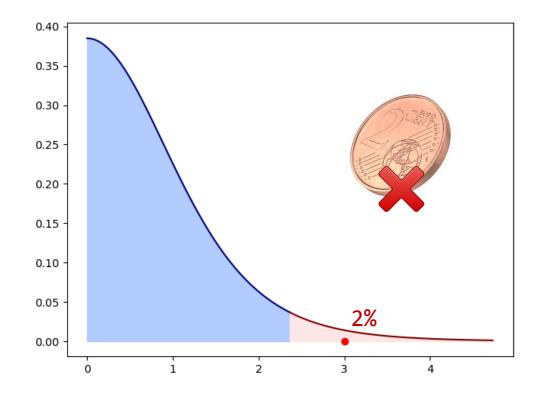
$$t=rac{(\overline{x}-\mu)\sqrt{m}}{s}$$
 имеет распределение Стьюдента с $m-1$ степенями свободы, где $\overline{x}=rac{1}{m}\sum_{i}^{m}x_{i}$ — выборочное среднее,

$$\overline{x} = \frac{1}{m} \sum_{i=1}^{m} x_i$$
 — выборочное среднее, $s^2 = \frac{1}{m-1} \sum_{i=1}^{m} (x_i - \overline{x})^2$ — выборочная дисперсия.

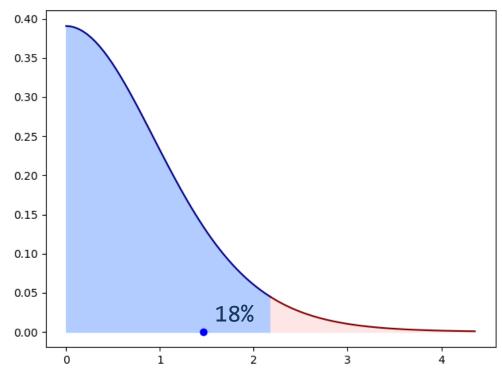
T-Test: one sample test

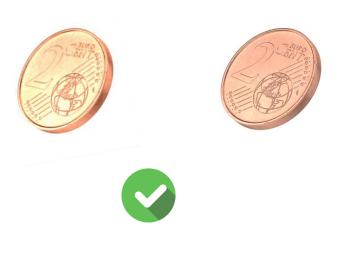


X_obs = [0, 1, 1, 1, 1, 1, 0]
mean_exp = 0.5



T-Test: two samples test

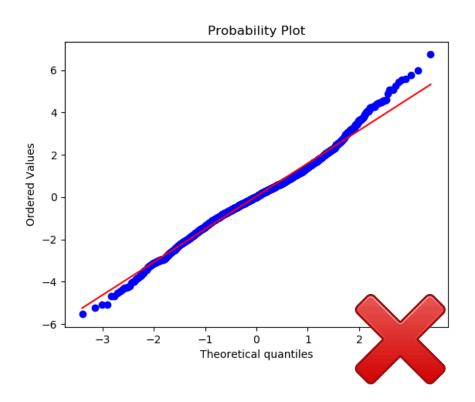


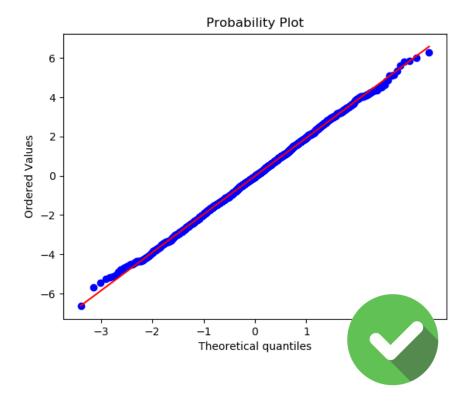


Normality test

- •Shapiro-Wilk W Test
- Anderson-Darling Test
- •Martinez-Iglewicz Test
- •Kolmogorov-Smirnov Test
- •D'Agostino Skewness Test

Normality test





F-test

F-Test does a hypothesis testing against models X and Y. It tells you if X is significantly better than Y, with respect to a p-value

- X is a model created by just a constant
- Y is the model created by a constant and a feature

The least square errors in both models are compared and checks if the difference in errors between model **X** and **Y** are significant or introduced by chance

The goal of the F-test is to provide significance level. If you want to make sure the features your are including are significant with respect to your pp-value, you use an F-test.

If you just want to include the kk best features, you can use the correlation only

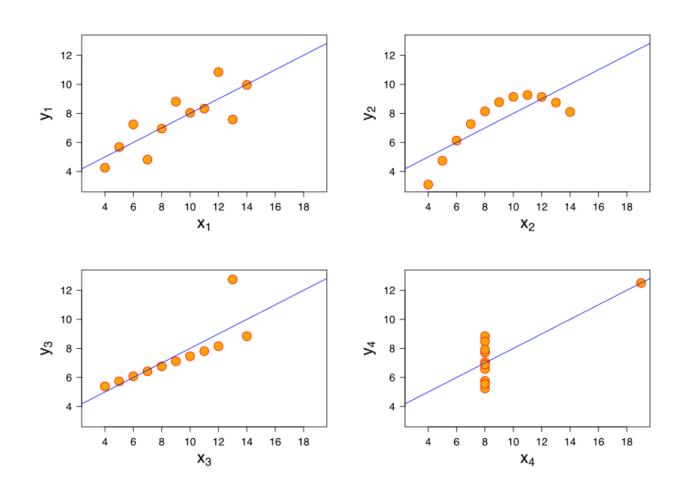
$$\rho_i = \frac{(X[:,i] - mean(X[:,i])) * (y - mean(y))}{std(X[:,i]) * std(y)}.$$

$$F_i=rac{
ho_i^2}{1-
ho_i^2}*(n-2)$$

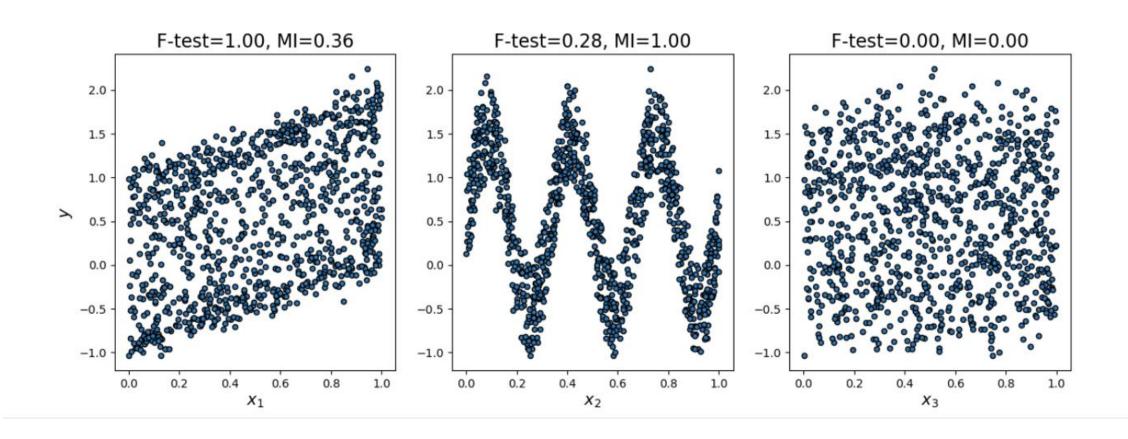
F-test: drawbacks

F-Test checks for and only captures <u>linear</u> relationships between features and labels.

A highly <u>correlated</u> feature is given higher score and less correlated features are given lower score.



Mutual information



Variance Inflation Factor

Variance Inflation Factor

Multicollinearity

Multicollinearity is problem that you can run into when you're fitting a regression model, or other linear model. It refers to predictors that are correlated with other predictors in the model. Unfortunately, the effects of multicollinearity can feel murky and intangible, which makes it unclear whether it's important to fix.

Moderate multicollinearity may not be problematic. However, severe multicollinearity is a problem because it can increase the variance of the coefficient estimates and make the estimates very sensitive to minor changes in the model. The result is that the coefficient estimates are unstable and difficult to interpret. Multicollinearity saps the statistical power of the analysis, can cause the coefficients to switch signs, and makes it more difficult to specify the correct model

Upon correlation matrix - remove high correlated variables (eg above 75%).

In addition, calculate **VIF** (variance inflation factor) to check the presence of multicollinearity. VIF value <= 4 suggests no multicollinearity whereas a value of >= 10 implies serious multicollinearity.