

# Gini Index and Inequality

ID, Last Name, First Name

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## Short Abstract

In this note, we study GINI index using WDI and compare with other index. In an OECD report, ‘OECD Regions and Cities at a Glance 2022’ Link, S80/S20 ratios are used. We consider a question if the ratio is related to GINI index.

**Definition S80/S20 ratio:** The total income received by the 20% of people with the highest income in a region divided by the total income received by the 20% of people with the lowest income in the same region.

## Information of data

### Poverty and Inequality

#### Distribution of income or consumption

Gini Index: SI.POV.GINI [Link]

Income share held by lowest 20%: SI.DST.FRST.20 [Link]

Income share held by second 20%: SI.DST.02ND.20 [Link]

Income share held by third 20%: SI.DST.03RD.20 [Link]

Income share held by fourth 20%: SI.DST.04TH.20 [Link]

Income share held by highest 20%: SI.DST.05TH.20 [Link]

## Setup

Install a package DescTools first.

```
library(tidyverse)
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr      1.1.4      v readr      2.1.5
## v forcats    1.0.0      v stringr   1.5.1
## v ggplot2    3.4.4      v tibble    3.2.1
## v lubridate  1.9.3      v tidyr     1.3.0
## v purrr      1.0.2
```

```
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
library(broom)
library(WDI)
library(DescTools)
```

## Importing Data

```
df_gini <- WDI(indicator = c(gini = "SI.POV.GINI",
                             `0-20` = "SI.DST.FRST.20",
                             `20-40` = "SI.DST.02ND.20",
                             `40-60` = "SI.DST.03RD.20",
                             `60-80` = "SI.DST.04TH.20",
                             `80-100` = "SI.DST.05TH.20"))

write_csv(df_gini, "data/gini.csv")

df_gini <- read_csv("data/gini.csv")

## Rows: 16758 Columns: 10
## -- Column specification -----
## Delimiter: ","
## chr (3): country, iso2c, iso3c
## dbl (7): year, gini, 0-20, 20-40, 40-60, 60-80, 80-100
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.

REGION <- c("1A", "1W", "4E", "6F", "6N", "6X", "7E", "8S", "A4", "A5",
            "A9", "B1", "B2", "B3", "B4", "B6", "B7", "B8", "C4", "C5", "C6",
            "C7", "C8", "C9", "D2", "D3", "D4", "D5", "D6", "D7", "EU", "F1",
            "F6", "M1", "M2", "N6", "OE", "R6", "S1", "S2", "S3", "S4", "T2",
            "T3", "T4", "T5", "T6", "T7", "V1", "V2", "V3", "V4", "XC", "XD",
            "XE", "XF", "XG", "XH", "XI", "XJ", "XL", "XM", "XN", "XO", "XP",
            "XQ", "XT", "XU", "XY", "Z4", "Z7", "ZB", "ZF", "ZG", "ZH", "ZI",
            "ZJ", "ZQ", "ZT")
```

## Viewing Data

```
df_gini

## # A tibble: 16,758 x 10
##   country    iso2c iso3c  year  gini `0-20` `20-40` `40-60` `60-80` `80-100`
##   <chr>      <chr> <chr> <dbl> <dbl> <dbl>   <dbl>   <dbl>   <dbl>
## 1 Afghanistan AF    AFG   1960    NA    NA     NA     NA     NA
## 2 Afghanistan AF    AFG   1961    NA    NA     NA     NA     NA
## 3 Afghanistan AF    AFG   1962    NA    NA     NA     NA     NA
## 4 Afghanistan AF    AFG   1963    NA    NA     NA     NA     NA
## 5 Afghanistan AF    AFG   1964    NA    NA     NA     NA     NA
## 6 Afghanistan AF    AFG   1965    NA    NA     NA     NA     NA
## 7 Afghanistan AF    AFG   1966    NA    NA     NA     NA     NA
## 8 Afghanistan AF    AFG   1967    NA    NA     NA     NA     NA
## 9 Afghanistan AF    AFG   1968    NA    NA     NA     NA     NA
## 10 Afghanistan AF    AFG   1969    NA    NA     NA     NA     NA
## # i 16,748 more rows
```

## Transforming Data

We add a new column with the value  $s_{80}/s_{20} = 80-100/0-20$ .

```
df_gini <- df_gini |> mutate(`s80/s20` = `80-100`/`0-20`)
df_gini
```

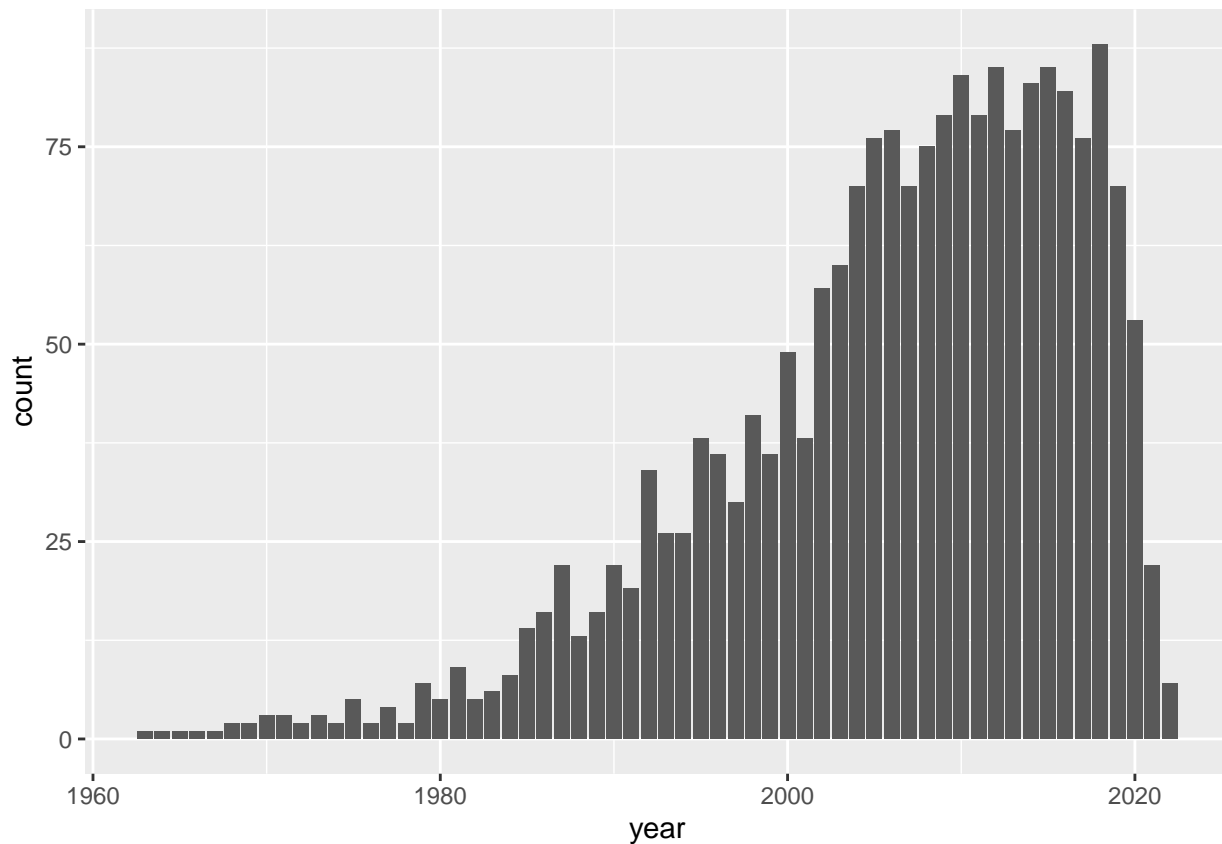
```
## # A tibble: 16,758 x 11
##   country    iso2c iso3c  year  gini `0-20` `20-40` `40-60` `60-80` `80-100`
##   <chr>      <chr> <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 Afghanistan AF    AFG  1960    NA    NA    NA    NA    NA    NA
## 2 Afghanistan AF    AFG  1961    NA    NA    NA    NA    NA    NA
## 3 Afghanistan AF    AFG  1962    NA    NA    NA    NA    NA    NA
## 4 Afghanistan AF    AFG  1963    NA    NA    NA    NA    NA    NA
## 5 Afghanistan AF    AFG  1964    NA    NA    NA    NA    NA    NA
## 6 Afghanistan AF    AFG  1965    NA    NA    NA    NA    NA    NA
## 7 Afghanistan AF    AFG  1966    NA    NA    NA    NA    NA    NA
## 8 Afghanistan AF    AFG  1967    NA    NA    NA    NA    NA    NA
## 9 Afghanistan AF    AFG  1968    NA    NA    NA    NA    NA    NA
## 10 Afghanistan AF    AFG  1969    NA    NA    NA    NA    NA    NA
## # i 16,748 more rows
## # i 1 more variable: `s80/s20` <dbl>
```

## Visualization and Analysis

### Number of Data in Each Year

Check the number of data available in year year.

```
df_gini |> drop_na(gini, `0-20`, `80-100`) |>
  ggplot(aes(year)) + geom_bar()
```



## Correlation of Three Indicators

We calculate the correlations among three indicators, GINI, top 20% and s80/s20 ratio.

1. Correlation using all available values.
2. Correlation using all available values of countries.
3. Correlation using all available values of countries in 2018.

```
df_gini |> drop_na(gini, `0-20`, `80-100`) |> select(gini, `80-100`, `s80/s20`) |>
cor() |> as.data.frame()
```

```
##           gini    80-100   s80/s20
## gini      1.0000000 0.9943488 0.8663291
## 80-100    0.9943488 1.0000000 0.8592673
## s80/s20   0.8663291 0.8592673 1.0000000
```

```
df_gini |> drop_na(gini, `0-20`, `80-100`) |>
  filter(!(iso2c %in% REGION)) |> select(gini, `80-100`, `s80/s20`) |>
  cor() |> as.data.frame()
```

```
##           gini    80-100   s80/s20
## gini      1.0000000 0.9943488 0.8663291
## 80-100    0.9943488 1.0000000 0.8592673
## s80/s20   0.8663291 0.8592673 1.0000000
```

```
df_gini |> drop_na(gini, `0-20`, `80-100`) |> filter(year == 2018) |>
  filter(!(iso2c %in% REGION)) |> select(gini, `80-100`, `s80/s20`) |>
  cor() |> as.data.frame()
```

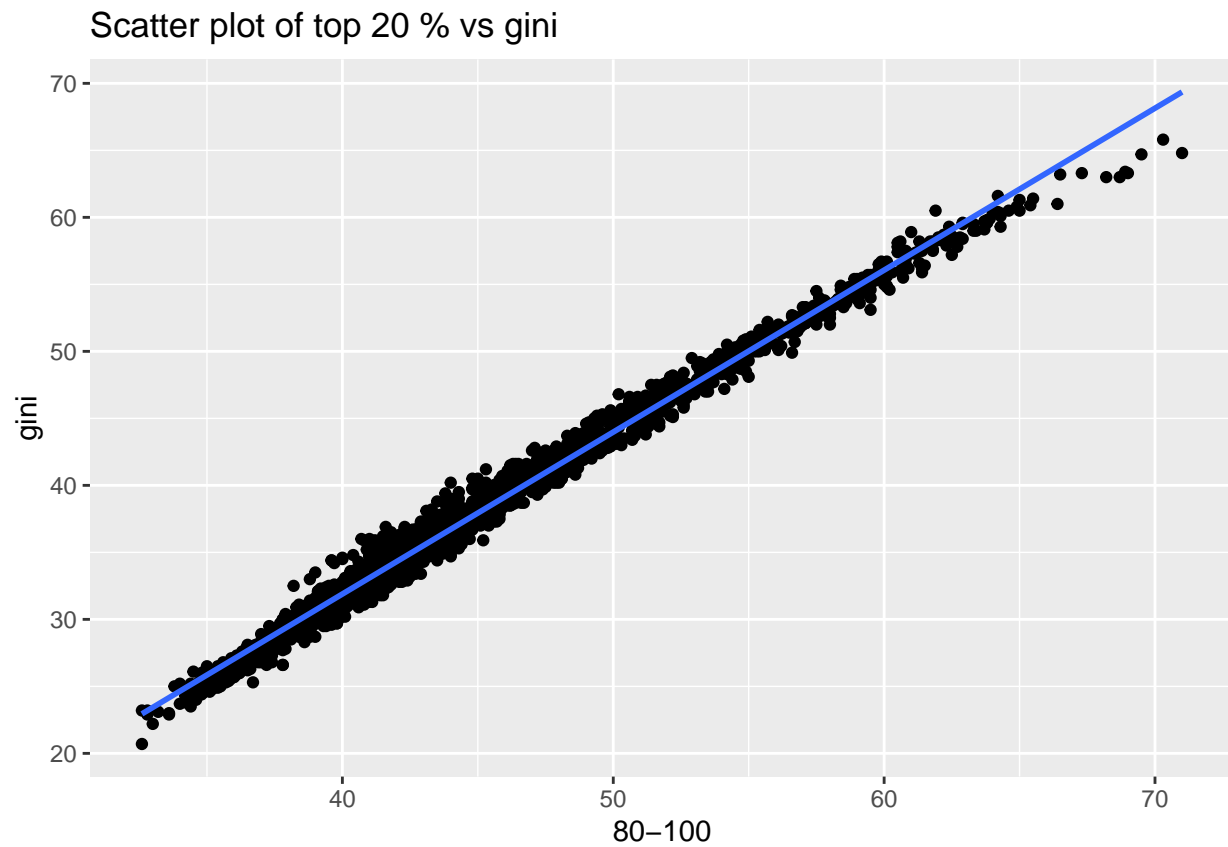
```
##           gini    80-100   s80/s20
## gini      1.0000000 0.9894834 0.9343159
## 80-100    0.9894834 1.0000000 0.9074783
## s80/s20   0.9343159 0.9074783 1.0000000
```

### Observations:

- The correlation between GINI index and the top 20% share of income is very close to 1.
- We chose 2018 as it is the year we have the most available values.
- There are no regional values of these three indices. So the values of the first two coincide.

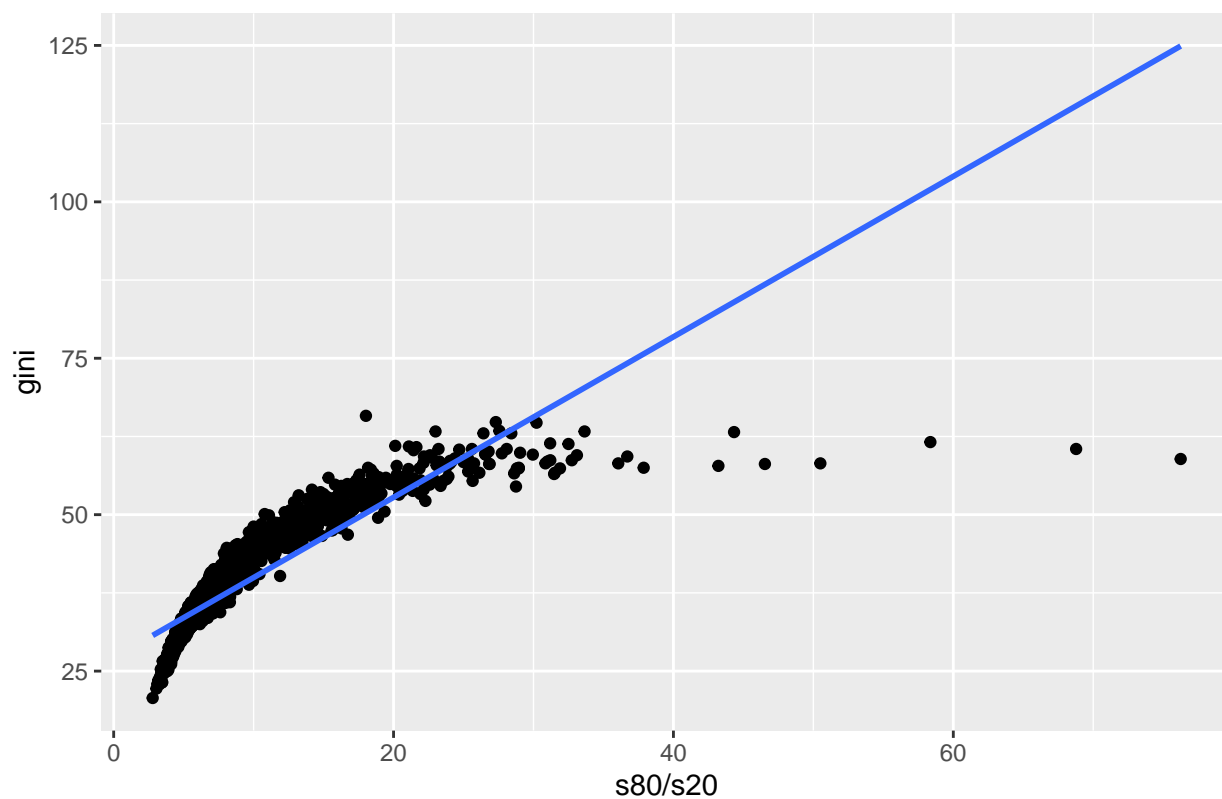
## Scatter Plots

```
df_gini |> drop_na(gini, `0-20`, `80-100`) |>
  ggplot(aes(`80-100`, gini)) + geom_point() +
  geom_smooth(formula = 'y~x', method = "lm", se = FALSE) +
  labs(title = "Scatter plot of top 20 % vs gini")
```



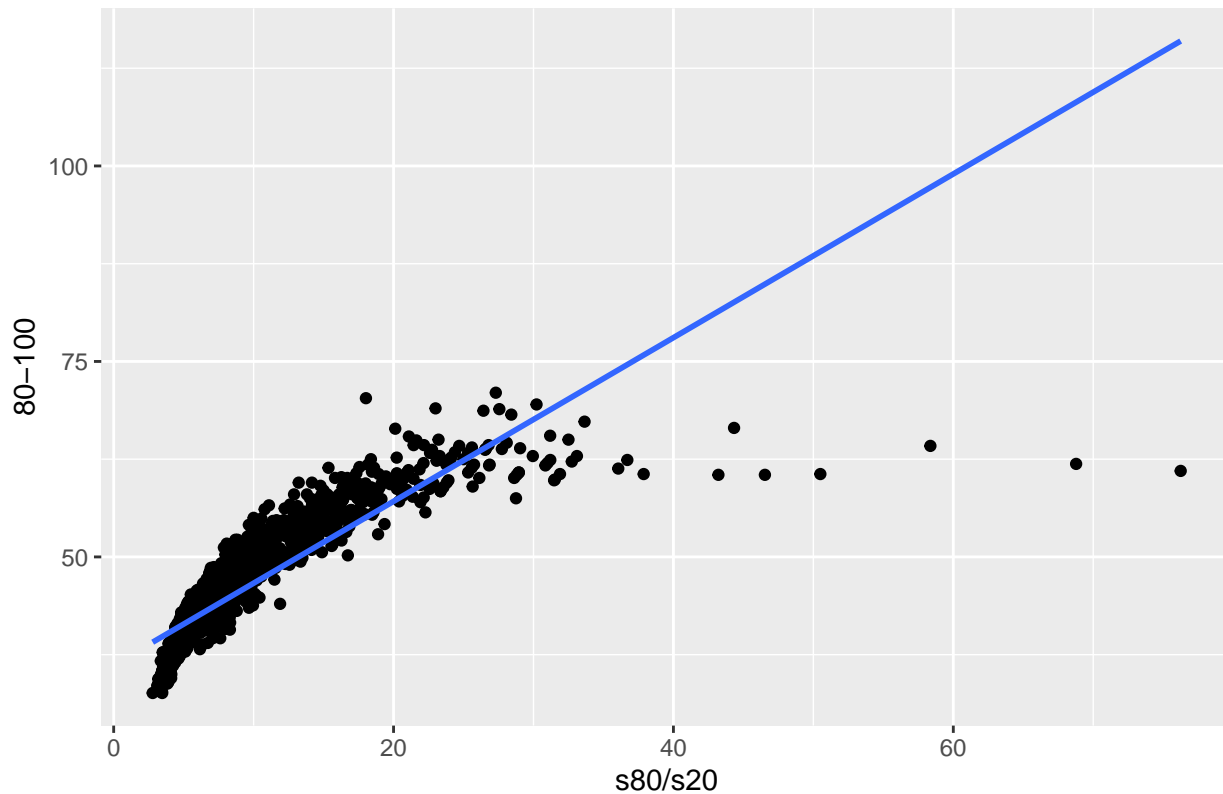
```
df_gini |> drop_na(gini, `0-20`, `80-100`) |>  
  ggplot(aes(`s80/s20`, gini)) + geom_point() +  
  geom_smooth(formula = 'y~x', method = "lm", se = FALSE) +  
  labs(title = "Scatter plot of s80/s20 ratio vs gini")
```

Scatter plot of s80/s20 ratio vs gini



```
df_gini |> drop_na(gini, `0-20`, `80-100`) |>  
  ggplot(aes(`s80/s20`, `80-100`)) + geom_point() +  
  geom_smooth(formula = 'y~x', method = "lm", se = FALSE) +  
  labs(title = "Scatter plot of s80/s20 ratio vs top 20 %")
```

Scatter plot of s80/s20 ratio vs top 20 %



## Models

We set three models.

```
model_gini_top20 <- df_gini |> lm(gini ~ `80-100`, data = _)
model_gini_8020 <- df_gini |> lm(gini ~ `s80/s20`, data = _)
model_8020_top20 <- df_gini |> lm(`s80/s20` ~ `80-100`, data = _)
```

### Summary of the model $\text{gini} \sim \text{top 20\%}$

```
model_gini_top20 |> summary()

##
## Call:
## lm(formula = gini ~ `80-100`, data = df_gini)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.5592 -0.6513 -0.0618  0.5784  3.4748
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -16.456298   0.131171  -125.5   <2e-16 ***
## `80-100`      1.208670   0.002879   419.8   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 0.9416 on 2005 degrees of freedom
## (14751 observations deleted due to missingness)
## Multiple R-squared: 0.9887, Adjusted R-squared: 0.9887
## F-statistic: 1.762e+05 on 1 and 2005 DF, p-value: < 2.2e-16
```

#### Summary of the model `gini ~ s80/s20`

```
model_gini_8020 |> summary()
```

```
##
## Call:
## lm(formula = gini ~ `s80/s20`, data = df_gini)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -66.009  -2.487   0.140   2.871  15.560
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  27.12397    0.17022  159.35  <2e-16 ***
## `s80/s20`    1.28242    0.01652   77.65  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.429 on 2004 degrees of freedom
## (14752 observations deleted due to missingness)
## Multiple R-squared: 0.7505, Adjusted R-squared: 0.7504
## F-statistic: 6029 on 1 and 2004 DF, p-value: < 2.2e-16
```

#### Summary of the model `s80/s20 ~ top 20%`

```
model_8020_top20 |> summary()
```

```
##
## Call:
## lm(formula = `s80/s20` ~ `80-100`, data = df_gini)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -8.242  -1.450  -0.068   0.975  56.544
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -23.327946    0.427285  -54.6  <2e-16 ***
## `80-100`     0.705481    0.009382   75.2  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.064 on 2004 degrees of freedom
## (14752 observations deleted due to missingness)
## Multiple R-squared: 0.7383, Adjusted R-squared: 0.7382
## F-statistic: 5655 on 1 and 2004 DF, p-value: < 2.2e-16
```



## broom::tidy and broom::glance

```
tidy(model_gini_top20) |> rbind(tidy(model_gini_8020)) |> rbind(tidy(model_8020_top20))

## # A tibble: 6 x 5
##   term          estimate std.error statistic p.value
##   <chr>          <dbl>    <dbl>    <dbl>    <dbl>
## 1 (Intercept)  -16.5      0.131     -125.      0
## 2 `80-100`      1.21     0.00288    420.      0
## 3 (Intercept)   27.1      0.170     159.      0
## 4 `s80/s20`     1.28     0.0165     77.6      0
## 5 (Intercept)  -23.3      0.427     -54.6      0
## 6 `80-100`      0.705     0.00938    75.2      0

glance(model_gini_top20) |> rbind(glance(model_gini_8020)) |> rbind(glance(model_8020_top20))

## # A tibble: 3 x 12
##   r.squared adj.r.squared sigma statistic p.value    df logLik    AIC    BIC
##   <dbl>      <dbl> <dbl>    <dbl>    <dbl> <dbl> <dbl> <dbl> <dbl>
## 1  0.989      0.989 0.942  176193.      0      1 -2726.  5458.  5475.
## 2  0.751      0.750 4.43    6029.      0      1 -5831. 11667. 11684.
## 3  0.738      0.738 3.06    5655.      0      1 -5092. 10189. 10206.
## # i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```

## Conclusion

The GINI index and the income share held by highest 20% is strongly correlated. The relation is even stronger than the correlation between the GINI index and the `s80/s20` ratio.

## Calculation Model of Gini Index

```
df_gini_calc <- df_gini |>
  mutate(`0` = 0, `20` = `0-20`,
         `40` = `0-20` + `20-40`,
         `60` = `0-20` + `20-40` + `40-60`,
         `80` = `0-20` + `20-40` + `40-60` + `60-80`,
         `100` = 100) |>
  select(-c(`0-20`:`60-80`))
df_gini_calc %>% drop_na()

## # A tibble: 2,003 x 13
##   country iso2c iso3c year  gini `80-100` `s80/s20` `0` `20` `40` `60`
##   <chr>   <chr> <chr> <dbl> <dbl>    <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 Albania AL  ALB  1996  27    36.1     3.92    0  9.2  22.9  40.6
## 2 Albania AL  ALB  2002  31.7  40.4     4.81    0  8.4  21    37.5
## 3 Albania AL  ALB  2005  30.6  39.2     4.67    0  8.4  21.3  38.3
## 4 Albania AL  ALB  2008  30    39      4.38    0  8.9  22    38.8
## 5 Albania AL  ALB  2012  29    37.8     4.25    0  8.9  22.1  39.4
## 6 Albania AL  ALB  2014  34.6  41.7     5.96    0  7    18.5  34.9
## 7 Albania AL  ALB  2015  32.8  40.6     5.27    0  7.7  19.8  36.3
## 8 Albania AL  ALB  2016  33.7  41.2     5.64    0  7.3  19.1  35.5
## 9 Albania AL  ALB  2017  33.1  40.7     5.36    0  7.6  19.6  36.1
## 10 Albania AL  ALB  2018  30.1  38.2     4.84    0  7.9  20.9  38.4
## # i 1,993 more rows
## # i 2 more variables: `80` <dbl>, `100` <dbl>
```

```
df_gini_calc_long <- df_gini_calc |> pivot_longer(`0`:`100`, names_to = "classes", values_to = "cumulative_share")
df_gini_calc_long %>% drop_na()
```

```
## # A tibble: 12,018 x 9
##   country iso2c iso3c year  gini `80-100` `s80/s20` classes cumulative_share
##   <chr>   <chr> <chr> <dbl> <dbl>   <dbl>   <dbl>   <dbl>         <dbl>
## 1 Albania AL   ALB   1996  27     36.1     3.92     0             0
## 2 Albania AL   ALB   1996  27     36.1     3.92    20            9.2
## 3 Albania AL   ALB   1996  27     36.1     3.92    40           22.9
## 4 Albania AL   ALB   1996  27     36.1     3.92    60           40.6
## 5 Albania AL   ALB   1996  27     36.1     3.92    80           63.9
## 6 Albania AL   ALB   1996  27     36.1     3.92   100          100
## 7 Albania AL   ALB   2002  31.7    40.4     4.81     0             0
## 8 Albania AL   ALB   2002  31.7    40.4     4.81    20            8.4
## 9 Albania AL   ALB   2002  31.7    40.4     4.81    40            21
## 10 Albania AL   ALB   2002  31.7    40.4     4.81    60           37.5
## # i 12,008 more rows
```

```
df_gini_f <- df_gini_calc_long |> group_by(country, year) |>
  drop_na(gini) |>
  reframe(gini, gini_spline = round(100-AUC(classes, cumulative_share, method = "spline")/50, digits = 1),
  distinct(country, year, gini, gini_spline, gini_trapezoid, `80-100`, `s80/s20`)
df_gini_f
```

```
## # A tibble: 2,009 x 7
##   country year  gini gini_spline gini_trapezoid `80-100` `s80/s20`
##   <chr>   <dbl> <dbl>   <dbl>   <dbl>   <dbl>   <dbl>
## 1 Albania 1996  27     26.4     25.4     36.1     3.92
## 2 Albania 2002  31.7    30.6     29.4     40.4     4.81
## 3 Albania 2005  30.6    29.7     28.5     39.2     4.67
## 4 Albania 2008  30     28.9     27.7     39       4.38
## 5 Albania 2012  29     28.1     27       37.8     4.25
## 6 Albania 2014  34.6    33.9     32.6     41.7     5.96
## 7 Albania 2015  32.8    32       30.8     40.6     5.27
## 8 Albania 2016  33.7    33.1     31.8     41.2     5.64
## 9 Albania 2017  33.1    32.2     30.9     40.7     5.36
## 10 Albania 2018  30.1    29.6     28.4     38.2     4.84
## # i 1,999 more rows
```

```
df_gini_f |> drop_na(gini, gini_spline, gini_trapezoid, `80-100`, `s80/s20`) |> select(gini, gini_spline, gini_trapezoid, `80-100`, `s80/s20`)
```

```
##           gini gini_spline gini_trapezoid    80-100    s80/s20
## gini          1.0000000  0.9993752      0.9992505 0.9943488 0.8663291
## gini_spline    0.9993752  1.0000000      0.9999799 0.9913027 0.8666667
## gini_trapezoid 0.9992505  0.9999799      1.0000000 0.9908249 0.8665828
## 80-100         0.9943488  0.9913027      0.9908249 1.0000000 0.8592673
## s80/s20        0.8663291  0.8666667      0.8665828 0.8592673 1.0000000
```

#### Observation:

- Since gini\_spline and gini\_trapezoid are calculated using the definition of the gini index, they are strongly correlated, though they are not exactly equal.