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Exercise 3.1.2

MA(2)

$$X(t) = a(t) + 0.2a(t-1) - 0.48a(t-2)$$

$$P_k = \frac{-\theta_k + \sum_{j=1}^{q-k} \theta_j \theta_{j+k}}{1 + \sum_{j=1}^q \theta_j^2} \quad \begin{matrix} k=1, 2, \dots, q \\ k > q \end{matrix}$$

$$= 0,$$

$$\theta_1 = -0.2 \quad \theta_2 = 0.48$$

P_0 :

$$P_0 = 1 \text{ by definition}$$

$$P_1: \quad \frac{-(-0.2) + (-0.2)(0.48)}{1 + (-0.2)^2 + 0.48^2} = \frac{0.104}{1.2704} = \boxed{0.08186}$$

$k=1$

P_2 :

$$k=2$$

$$\frac{-0.48}{1 + (-0.2)^2 + 0.48^2} = \frac{-0.48}{1.2704} = \boxed{-0.377835}$$

P_3 :

$$k=3 \rightarrow 3 > 2 \rightarrow k > q \rightarrow \boxed{0 \text{ by definition}}$$