```
In [1]: from sklearn.datasets import load boston
        import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        import seaborn as sns
        import warnings
        warnings.filterwarnings("ignore")
In [2]: boston = load boston()
In [3]: | type(boston)
Out[3]: sklearn.utils.Bunch
In [4]: boston.keys()
Out[4]: dict keys(['data', 'target', 'feature names', 'DESCR', 'filename'])
In [5]: boston.feature names
Out[5]: array(['CRIM', 'ZN', 'INDUS', 'CHAS', 'NOX', 'RM', 'AGE', 'DIS', 'RAD',
               'TAX', 'PTRATIO', 'B', 'LSTAT'], dtype='<U7')
In [6]: boston.data[0:2]
Out[6]: array([[6.3200e-03, 1.8000e+01, 2.3100e+00, 0.0000e+00, 5.3800e-01,
                6.5750e+00, 6.5200e+01, 4.0900e+00, 1.0000e+00, 2.9600e+02,
                1.5300e+01, 3.9690e+02, 4.9800e+00],
               [2.7310e-02, 0.0000e+00, 7.0700e+00, 0.0000e+00, 4.6900e-01,
                6.4210e+00, 7.8900e+01, 4.9671e+00, 2.0000e+00, 2.4200e+02,
                1.7800e+01, 3.9690e+02, 9.1400e+00]])
```

```
In [7]: df = pd.DataFrame(boston.data)
    df.head()
```

### Out[7]:

		0	1	2	3	4	5	6	7	8	9	10	11	12
_	0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98
	1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14
:	2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03
;	3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.94
	4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33

```
In [8]: boston.feature_names
```

In [9]: df.columns = boston.feature\_names
 df.head()

#### Out[9]:

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	В	LSTAT
 0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98
1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14
2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03
3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.94
4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33

```
In [10]: df['PRICE'] = boston.target
df.head()
```

### Out[10]:

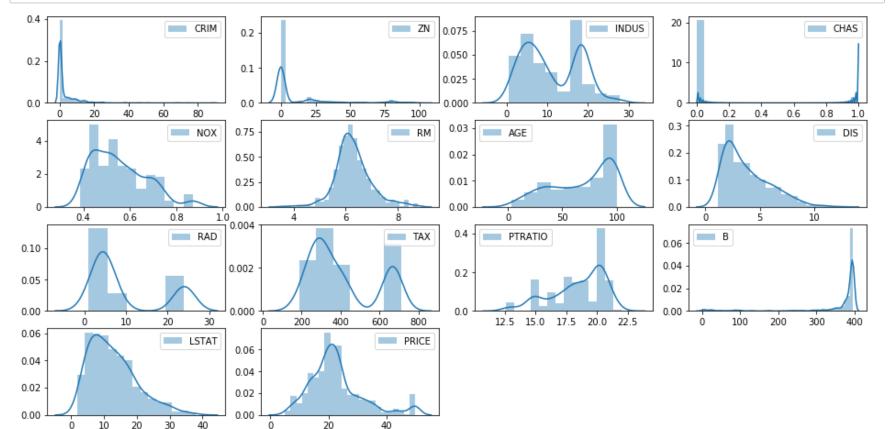
_		CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	В	LSTAT	PRICE
	0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98	24.0
	1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14	21.6
	2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03	34.7
	3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.94	33.4
	4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33	36.2

```
In [11]: df.columns[0]
```

Out[11]: 'CRIM'

# **Visualization**

```
In [12]: fig = plt.figure(figsize=(16,8))
for col in range(14):
    fig.add_subplot(4,4,col+1)
    sns.distplot(df.iloc[:,col], label=str(df.columns[col]))
    plt.xlabel(' ')
    plt.legend()
```



```
In []:
In [13]: corr_ = df.corr(method='pearson')
In [14]: np.shape(corr_)
Out[14]: (14, 14)
```

In [15]: plt.figure(figsize=(16,10))
sns.heatmap(corr\_, annot=True)

- 0.9

- 0.6

- -0.3

- -0.6

Out[15]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7fe9756cd710>

CRIM -	- 1	-0.2	0.41	-0.056	0.42	-0.22	0.35	-0.38	0.63	0.58	0.29	-0.39	0.46	-0.39
ZN -	-0.2	1	-0.53	-0.043	-0.52	0.31	-0.57	0.66	-0.31	-0.31	-0.39	0.18	-0.41	0.36
INDUS -	0.41	-0.53	1	0.063	0.76	-0.39	0.64	-0.71	0.6	0.72	0.38	-0.36	0.6	-0.48
CHAS -	-0.056	-0.043	0.063	1	0.091	0.091	0.087	-0.099	-0.0074	-0.036	-0.12	0.049	-0.054	0.18
NOX -	0.42	-0.52	0.76	0.091	1	-0.3	0.73	-0.77	0.61	0.67	0.19	-0.38	0.59	-0.43
RM -	-0.22	0.31	-0.39	0.091	-0.3	1	-0.24	0.21	-0.21	-0.29	-0.36	0.13	-0.61	0.7
AGE ·	0.35	-0.57	0.64	0.087	0.73	-0.24	1	-0.75	0.46	0.51	0.26	-0.27	0.6	-0.38
DIS -	-0.38	0.66	-0.71	-0.099	-0.77	0.21	-0.75	1	-0.49	-0.53	-0.23	0.29	-0.5	0.25
RAD -	- 0.63	-0.31	0.6	-0.0074	0.61	-0.21	0.46	-0.49	1	0.91	0.46	-0.44	0.49	-0.38
TAX -	0.58	-0.31	0.72	-0.036	0.67	-0.29	0.51	-0.53	0.91	1	0.46	-0.44	0.54	-0.47
PTRATIO -	0.29	-0.39	0.38	-0.12	0.19	-0.36	0.26	-0.23	0.46	0.46	1	-0.18	0.37	-0.51
В-	-0.39	0.18	-0.36	0.049	-0.38	0.13	-0.27	0.29	-0.44	-0.44	-0.18	1	-0.37	0.33
LSTAT -	0.46	-0.41	0.6	-0.054	0.59	-0.61	0.6	-0.5	0.49	0.54	0.37	-0.37	1	-0.74
PRICE -	-0.39	0.36	-0.48	0.18	-0.43	0.7	-0.38	0.25	-0.38	-0.47	-0.51	0.33	-0.74	1
	CRIM	ΖŃ	INDUS	CHAS	NÓX	RM	AĠE	DİS	RÁD	TÁX	PTRATIO	В́	LSTAT	PRICE

```
In [16]: corr_['PRICE']
Out[16]: CRIM
                   -0.388305
         zn
                    0.360445
         INDUS
                   -0.483725
         CHAS
                    0.175260
         NOX
                   -0.427321
         RM
                    0.695360
         AGE
                   -0.376955
         DIS
                    0.249929
         RAD
                   -0.381626
         TAX
                   -0.468536
         PTRATIO
                   -0.507787
         В
                    0.333461
         LSTAT
                   -0.737663
                    1.000000
         PRICE
         Name: PRICE, dtype: float64
```

```
In [17]: | 11 = corr ['PRICE'].values.tolist()
         11.remove(11[-1])
         11[0:3]
Out[17]: [-0.3883046085868114, 0.3604453424505447, -0.483725160028373]
In [18]: | 1 = 11
         ls = np.sort(l).tolist()
         ls1 = ls[-1::-1]
         ls1[0:3]
Out[18]: [0.6953599470715389, 0.3604453424505447, 0.33346081965706653]
In [19]: | idx = np.argsort(l).tolist()
         idx
Out[19]: [12, 10, 2, 9, 4, 0, 8, 6, 3, 7, 11, 1, 5]
In [20]: label = corr ['PRICE'].index.tolist()
         label[0:2]
Out[20]: ['CRIM', 'ZN']
In [21]: type(label)
Out[21]: list
In [22]: label1 = []
In [23]: for itm in idx:
             label1.append(label[itm])
```

```
In [24]: label1[-1::-1]
Out[24]: ['RM',
          'ZN',
          'В',
          'DIS',
          'CHAS',
          'AGE',
          'RAD',
          'CRIM',
          'NOX',
          'TAX',
          'INDUS',
          'PTRATIO',
          'LSTAT']
In [25]: label1s = label1[-1::-1]
         label1s[0:2]
Out[25]: ['RM', 'ZN']
```

```
In [26]: df_corr = pd.DataFrame({'itm':label1s, 'corr':ls1})
    df_corr
```

## Out[26]:

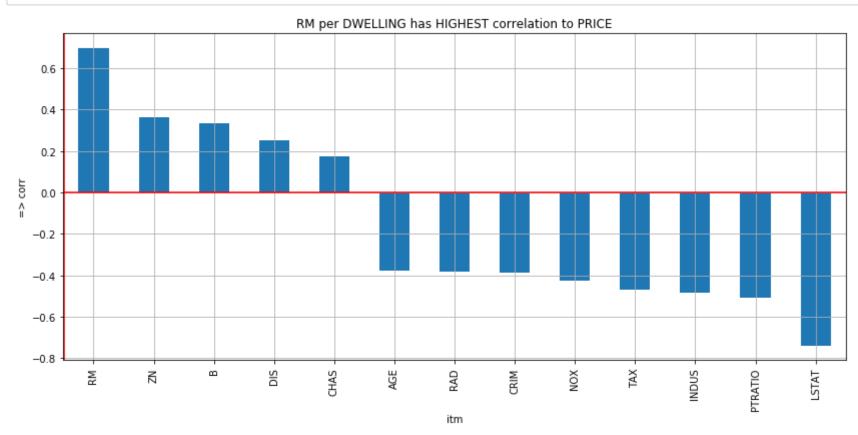
	itm	corr
0	RM	0.695360
1	ZN	0.360445
2	В	0.333461
3	DIS	0.249929
4	CHAS	0.175260
5	AGE	-0.376955
6	RAD	-0.381626
7	CRIM	-0.388305
8	NOX	-0.427321
9	TAX	-0.468536
10	INDUS	-0.483725
11	PTRATIO	-0.507787
12	LSTAT	-0.737663

```
In [27]: df_corr_1 = df_corr.set_index(df_corr['itm'])
    df_corr_1.head()
```

### Out[27]:

	itm	corr
itm		
RM	RM	0.695360
ZN	ZN	0.360445
В	В	0.333461
DIS	DIS	0.249929
CHAS	CHAS	0 175260

```
In [28]: df_corr_1['corr'].plot(kind='bar', figsize=(14,6))
    plt.axvline(-0.49, color='red', linestyle='-')
    plt.axhline(0, color='red', linestyle='-')
    plt.title('RM per DWELLING has HIGHEST correlation to PRICE')
    plt.ylabel('=> corr')
    plt.grid()
    plt.show()
```



```
In [29]: print(boston.DESCR)
         .. boston dataset:
         Boston house prices dataset
         **Data Set Characteristics:**
             :Number of Instances: 506
             :Number of Attributes: 13 numeric/categorical predictive. Median Value (attribute 14) is usually t
         he target.
             :Attribute Information (in order):
                 - CRIM
                            per capita crime rate by town
                            proportion of residential land zoned for lots over 25,000 sq.ft.
                 - ZN
                 - INDUS
                            proportion of non-retail business acres per town
                            Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)
                  - CHAS
                            nitric oxides concentration (parts per 10 million)
                 - NOX
                 - RM
                            average number of rooms per dwelling
                 - AGE
                            proportion of owner-occupied units built prior to 1940
                 - DIS
                            weighted distances to five Boston employment centres
                 - RAD
                            index of accessibility to radial highways
                 - TAX
                            full-value property-tax rate per $10,000
                 - PTRATIO pupil-teacher ratio by town
                            1000(Bk - 0.63)<sup>2</sup> where Bk is the proportion of blacks by town
                  B
                  - LSTAT
                            % lower status of the population
                  MEDV
                            Median value of owner-occupied homes in $1000's
             :Missing Attribute Values: None
             :Creator: Harrison, D. and Rubinfeld, D.L.
         This is a copy of UCI ML housing dataset.
         https://archive.ics.uci.edu/ml/machine-learning-databases/housing/ (https://archive.ics.uci.edu/ml/mac
         hine-learning-databases/housing/)
         This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.
         The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic
         prices and the demand for clean air', J. Environ. Economics & Management,
```

vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics ...', Wiley, 1980. N.B. Various transformations are used in the table on pages 244-261 of the latter.

The Boston house-price data has been used in many machine learning papers that address regression problems.

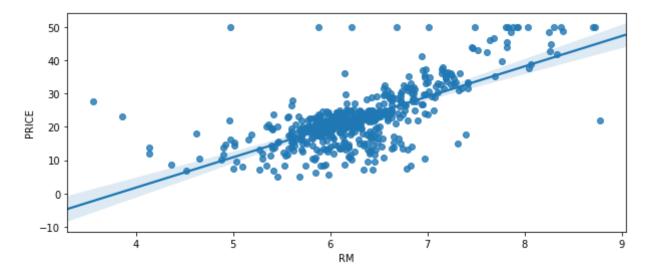
- .. topic:: References
- Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influential Data and Sources of Colli nearity', Wiley, 1980. 244-261.
- Quinlan, R. (1993). Combining Instance-Based and Model-Based Learning. In Proceedings on the Tenth International Conference of Machine Learning, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.

# Regression

**RM vs PRICE** 

```
In [30]: plt.figure(figsize=(10,4))
sns.regplot(x="RM", y="PRICE", data=df)
```

Out[30]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7fe97575f898>



In [31]: import statsmodels.api as sm
from statsmodels.formula.api import ols

```
In [32]: ols pr rm = ols('PRICE ~ RM', df).fit()
         ols pr rm.summary()
```

#### Out[32]:

**OLS Regression Results** 

Dep. Variable: PRICE R-squared: 0.484 Model: OLS Adj. R-squared: 0.483 Method: Least Squares 471.8 F-statistic: Mon, 16 Nov 2020 Prob (F-statistic): 2.49e-74 Date: Time: 00:42:17 Log-Likelihood: -1673.1 506 3350. No. Observations: AIC: 504 3359. **Df Residuals:** BIC: **Df Model:** 1 nonrobust **Covariance Type:** coef std err P>|t| [0.025 0.975] 2.650 -13.084 0.000 -39.877 -29.465

Intercept -34.6706 RM9.1021 0.419 21.722 0.000 8.279 9.925

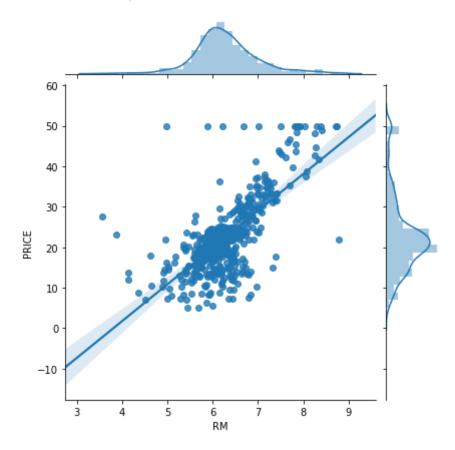
0.684 **Omnibus:** 102.585 **Durbin-Watson:** Prob(Omnibus): Jarque-Bera (JB): 0.000 612.449 Skew: 0.726 **Prob(JB):** 1.02e-133 **Kurtosis:** 8.190 Cond. No. 58.4

## Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [33]:
sns.jointplot(x="RM", y="PRICE", data=df, kind="reg")
```

Out[33]: <seaborn.axisgrid.JointGrid at 0x7fe976ba8550>



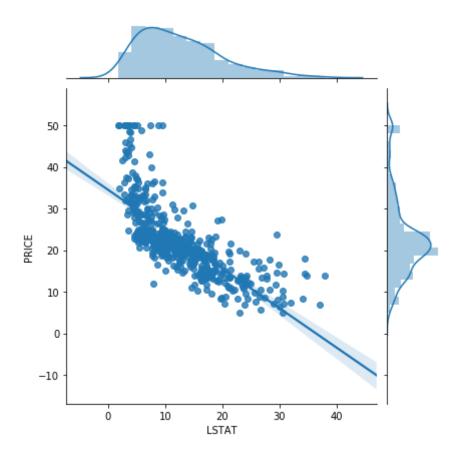
```
In [34]: 66.6/7.3
```

Out[34]: 9.123287671232877

## **LSTAT vs PRICE**

```
In [35]: sns.jointplot(x='LSTAT', y='PRICE', data=df, kind='reg')
```

Out[35]: <seaborn.axisgrid.JointGrid at 0x7fe976d68be0>



```
In [36]: ols_pr_lstat = ols("PRICE ~ LSTAT", data=df).fit() # ols -> ordinary least square
    ols_pr_lstat.summary()
```

### Out[36]:

**OLS Regression Results** 

**Covariance Type:** 

Dep. Variable: **PRICE** 0.544 R-squared: Model: OLS Adj. R-squared: 0.543 Method: Least Squares 601.6 F-statistic: Mon, 16 Nov 2020 Prob (F-statistic): 5.08e-88 Date: Time: 00:42:21 Log-Likelihood: -1641.5 506 3287. No. Observations: AIC: 3295. **Df Residuals:** 504 BIC: 1 Df Model:

 coef
 std err
 t
 P>|t|
 [0.025
 0.975]

 Intercept
 34.5538
 0.563
 61.415
 0.000
 33.448
 35.659

 LSTAT
 -0.9500
 0.039
 -24.528
 0.000
 -1.026
 -0.874

nonrobust

 Omnibus:
 137.043
 Durbin-Watson:
 0.892

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 291.373

 Skew:
 1.453
 Prob(JB):
 5.36e-64

 Kurtosis:
 5.319
 Cond. No.
 29.7

## Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [37]: ols_pr_rm.params[1]
```

Out[37]: 9.102108981180306

```
In [38]: g = df_corr_1.index.tolist()
Out[38]: ['RM',
           'ZN',
           'В',
           'DIS',
          'CHAS',
          'AGE',
          'RAD',
          'CRIM',
          'NOX',
           'TAX',
          'INDUS',
          'PTRATIO',
          LSTAT']
In [49]: for itm in g:
             str1 = str(" PRICE ~ ") + str(itm)
             str2 = str(str1)
             ols_fit = ols(str2, data=df).fit()
             print(ols_fit.params[1])
         9.102108981180306
         0.1421399941553545
         0.03359306011501362
         1.0916130158411057
         6.3461571125265515
         -0.12316272123567987
         -0.40309539555252993
         -0.41519027791509056
         -33.9160550086611
         -0.025568099481987235
         -0.6484900536157133
         -2.157175296060963
         -0.9500493537579908
 In [ ]:
```

```
In [50]: df.columns
Out[50]: Index(['CRIM', 'ZN', 'INDUS', 'CHAS', 'NOX', 'RM', 'AGE', 'DIS', 'RAD', 'TAX',
                'PTRATIO', 'B', 'LSTAT', 'PRICE'],
               dtype='object')
In [51]: from sklearn.model_selection import train_test_split
         from sklearn.linear model import LinearRegression
         from sklearn import metrics
         from sklearn.metrics import r2_score, mean_squared_error
         from sklearn.metrics import classification report, accuracy score
In [52]: x tr, x t, y tr, y t = train_test_split(df[["RM"]].values, df[["PRICE"]].values, test_size=0.15, random
         np.shape(x_tr), np.shape(y_tr), np.shape(x_t), np.shape(y_t)
Out[52]: ((430, 1), (430, 1), (76, 1), (76, 1))
In [53]: lr = LinearRegression()
         lr.fit(x tr, y tr)
         y p = lr.predict(x t)
In [54]: y_p[0:5].tolist(), y_t[0:5].tolist()
Out[54]: ([[31.48770152144715],
           [25.052497893143745],
           [21.202071345460823],
           [20.774246173496053],
           [17.50316621284876]],
          [[34.6], [31.5], [20.6], [14.5], [16.2]])
In [55]: r2_score(y_t, y_p), mean squared error(y t, y_p)
Out[55]: (0.6254819615240168, 26.940868860063624)
 In [ ]:
```

```
In [56]: X=df[ ['CRIM', 'ZN', 'INDUS', 'CHAS', 'NOX', 'RM', 'AGE', 'DIS', 'RAD', 'TAX',
                'PTRATIO', 'B', 'LSTAT'] ].values
         np.shape(X)
Out[56]: (506, 13)
In [57]: y = df[['PRICE']].values
         np.shape(y)
Out[57]: (506, 1)
In [58]: x_tr, x_t, y_tr, y_t = train_test_split(X, y, test_size=0.15, random_state=100)
         lr.fit(x_tr, y_tr)
         y p = lr.predict(x_t)
         r2_score(y_t, y p), mean_squared error(y t, y p)
Out[58]: (0.8273125828534873, 12.422229588884392)
In [ ]:
 In [ ]:
 In [ ]:
 In [ ]:
```