Data Structures and Algor nal Linguistics III (IGCL-RA-07)

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Winter Semester 2020/21

Definitions

A tree is a set of nodes organize hierarchically with the following properties:

- If a tree is non-empty, it has a
- If a tree is non-empty, it has a special node root
   Except the root node, every node in the tree has a unique parent (al nodes except the root are children of another node)

Ordered trees

- Alternatively, we can define a tree recursively:
   The empty set of nodes is a tree
   Otherwise a tree contains a root with sub-trees as its children

A tree is ordered if there is an ordering between siblings. Typical examples include:

- A tree representing a document (e.g., HTML) structure
   Parse trees
   (maybe) a family tree
- · In many cases order is not important Class hierarchy in a object-oriented prog
   The tree representing files in a computer

Some properties of binary trees

For a binary tree with  $n_g$  leaf,  $n_1$  internal, n

- nodes and with height h  $h + 1 \le n \le 2^{h+1} 1$ •  $1 \leqslant n_{\ell} \leqslant 2^h$ 
  - $\bullet \ h \leqslant n_i \leqslant 2^h 1$

•  $log(n+1)-1 \leqslant h \leqslant n-1$ • For any proper binary tree,  $n_c = n_s + 1$ 

Implementation of trees





Breadth first traversal



queue.append(root)
while queue:
node = queue.pop(0)
# process the mode fe = queue por process the node int(node data) r child in node children: ~~ append(child) Why study trees

- . A tree is a, hierarchical, non-linear data stri We have already resorted to descriptions using trees
- . A tree is a graph with certain properties, and part of many of the graph
- . It is also very common in (computational) linguistics

- Farse trees: we often represent
   Language trees: trees that trace the relation between languages
   Decision trees: a well-known algorithm for machine learning, also used for
- many NLP problems

More definitions

- The nodes with the same parent are called siblings The nodes with children are called internal nodes
- . The nodes without children are the leaf nodes · A path is a sequence of connected nodes
- Any node in the path from the root to a particular node is its ancestors . A node is the descendant of its ancestor
- \* A subtree is a tree rooted by a non-root node
- A depth of a node is the number of edges from root
   A height of a node is the number of edges from the deepest descendant
- . The height of a tree is the height of its root

# Binary trees

- . Binary trees, where nodes can have at most two children, have many applications Binary trees have a natural order, each child is either
- a left child or a right child A binary tree is proper, or full if every node has either
- two children or none In a complete binary tree, every level except possibly the last, is completely filled, and all nodes at the last level is at the left
- A perfect binary tree is is a full binary tree whose leaf nodes have the same depth



Binary tree example: expression trees

### Implementation of trees

- . Binary trees can also be implemented with arrays many trees can also be implemented wit - the root node is stored at index 0 - the left child of the node at index i is stor-the right child of the node at index i is stor-2i + 2

  - the parent of the node at index i is at index  $\lfloor i/2 \rfloor$
- . If the binary tree is complete, this representation does not waste (much)





## Pre-order traversal



def pre\_order(node)

print(node.data) for child in node.children: pre\_order(child)

