Data Structures and Algor nal Linguistics III (IGCL-RA-07)

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A tree is a set of nodes organize hierarchically with the following properties:

Definitions

Ordered trees

 If a tree is non-empty, it has a If a tree is non-empty, it has a special node root
 Except the root node, every node in the tree has a unique parent (al nodes except the root are children of another node)

Alternatively, we can define a tree recursively:
 The empty set of nodes is a tree
 Otherwise a tree contains a root with sub-trees as its children



 A tree is ordered if there is an ordering between siblings. Typical examples include: A tree representing a document (e.g., HTML) structure
 Parse trees
 (maybe) a family tree

· In many cases order is not important Class hierarchy in a object-oriented prog
 The tree representing files in a computer

Some properties of binary trees

For a binary tree with n_g leaf, n_1 internal, n

nodes and with height h • $h + 1 \le n \le 2^{h+1} - 1$

• $1 \leqslant n_{\ell} \leqslant 2^h$ $\bullet \ h \leqslant n_i \leqslant 2^h - 1$

• $log(n+1)-1 \leqslant h \leqslant n-1$

• For any proper binary tree, $n_c = n_s + 1$



Implementation of trees





Breadth first traversal



queue.append(root)
while queue:
node = queue.pop(0)
process the mode fe = queue por process the node int(node data) r child in node children: ~~ append(child) Why study trees

. A tree is a, hierarchical, non-linear data stri

· We have already resorted to descriptions using trees . A tree is a graph with certain properties, and part of many of the graph

. It is also very common in (computational) linguistics

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Parse trees: we often represent

Language trees: trees that trace the relation between languages

Decision trees: a well-known algorithm for machine learning, also used for

many NLP problems

More definitions

 The nodes with the same parent are called siblings The nodes with children are called internal nodes

. The nodes without children are the leaf nodes · A path is a sequence of connected nodes Any node in the path from the root to a particular node is its ancestors

. A node is the descendant of its ancestor * A subtree is a tree rooted by a non-root node

A depth of a node is the number of edges from root
 A height of a node is the number of edges from the

deepest descendant . The height of a tree is the height of its root

Binary trees

. Binary trees, where nodes can have at most two children, have many applications

 Binary trees have a natural order, each child is either a left child or a right child A binary tree is proper, or full if every node has either

two children or none In a complete binary tree, every level except possibly the last, is completely filled, and all nodes at the last level is at the left

A perfect binary tree is is a full binary tree whose leaf nodes have the same depth

Binary tree example: expression trees



Implementation of trees

Binary trees can also be implemented with arrays:

 the root node is stored at index 0
 the left child of the node at index i is stored at Zi + 1
 the right child of the node at index i is stored at Zi + 2

 the parent of the node at index i is at index [(i-1)/2] . If the binary tree is complete, this re



Pre-order traversal

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def pre_order(node)

print(node.data) for child in node.children: pre_order(child)

