Graph Traversal Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III

Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de

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Graph traversal · A graph traver

- itic way to visit all nodes in the graph Graph traversal is one of the basic tasks on a graph, answering many
- interesting questions
- Is there a path from one node to another?
 What is the shortest path (with minimum number of edges) between two
- What is the shorter
 nodes?
 Is the graph conne
 Is the graph cyclic?
- rsals are breadth-first and depth-first

DFS - intuition

- Depth first search follows the san idea as exploring a labyrinth with a string and a chalk
- Visit each intersection (node), while marking the path you took with the string
- Mark each visited node, backtrack (following the string) when hit a dead end



DFS - algorithm

- def dfs(start, visited=None):
 if visited is None:
 visited = {start: None}
 for node in start.neighbors():
 if node not in visited:
 visited[node] = start
 dfs(node, visited)
- . Depth-first search (DFS) is easy with · DFS starts from a start node
- · Marks each node it visits as visited (typically put it in a set data structure)
- . Then, take an arbitrary unvisited neighbor and continue visiting the nodes recursively
- Algorithm terminates when backtracking leads to the start node with no unvisited nodes left

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges
- . The discovery edges form the DFS tree
- · The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are
- The edges to a non-parent node in the DFS tree are called cross edges

DFS - demonstration

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Properties of DFS

- . DFS visits all nodes in the co * Discovery edges form a spanning tree of the connected component
- If a node v is connected to the start node, there is a path from the start node v in the DFS tree
- The DFS algorithm visits each node and check each edge once (twice for
- undirected graphs) * The complexity of the algorithm is O(n+m) for n nodes and m edges

BFS - intuition

in parallel

BFS - demonstration

Dangers of DFS

Company of the Compan

. In the maze, at every intersection

search (BPS) is to explore all options send out people in all directions

BPS divides the nodes into levels:

starting node at level 0
 nodes directly accessible from start at level 1

· A way to thing about breadth-first

BFS - algorithm

def bfs(start): lef bfs(start):
queue = [start]
visited = (start: None):
while queue:
current = queue.pop(o)
for mode in current.neighbors():
if mode not in visited:
 visited[node] = current
queue.append(node)

- · Typically implement BPS is implemented with a queue
- . If you replace the queue with a
- The algorithm visits nodes closest to the start node first stack, you get an iterative version of the DFS
- * Similar to DFS, the edges that we take to discover a new node are called the discovery edges
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BPS - demonstration



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Properties of BFS

= If a node ν is reachable from the start node, the BFS finds the shortest path from the start node to ν * The complexity of the algorithm is O(n+m) for n nodes and m edges

* DPS visits all nodes in the connected component from the start n

. The BFS algorithm visits each node and check each edge

* Discovery edges form a spanning tree of the connected component

Problems solved by graph traversals

- · Finding a path between two nodes (if one exists)
- Testing whether G is connected
- Computing connected components of G
- Detecting cycles

Finding a path between two nodes

- Traverse the graph from the source node, record the
- discovery edges . Start from the target node
- trace the path back to the source
- . With BPS, we get the
 - shortest path Running time is the length of the path: O(n)
- def find_path(source, target, visited):
 path = []
 if target in visited:
 path_append(target)
 current = target
- while current is not source parent = visited[current] path.append(parent) current = parent return path.reverse()

Some other problems solved by graph traversal

- · Is the graph connected?
- Yes if the 'visited' nodes have the same length as the nodes of the graph · Find the connected components Run traversal multiple times, until all nodes are visit
- · Is the graph cyclic?
- A graph is cyclic if there is a back edge during graph traversal

Summary

- · Traversal is one of the basic operations in graphs Graph traversals already solve some interesting prob
 Find a path (shortest with BFS)
 Tost connectivity, find connected components
- Find cycles * Reading on graphs: Goodrich, Tamassia, and Goldwasser (2013, chapter 14)
- More graph algorithms: special problems on directed graphs, shortest paths

Acknowledgments, credits, references

Goodrich, Michael T., Roberto Tamassia, and Michael H. Goldwasser (2013). Data Structures and Algorithms in Python. John Wiley & Sons, Incorporated. 1580

