Algorithmic patterns Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de Winter Semester 2020/21

ome common approa - Revisiting recursion - Brute force - Divide and conquer - Greedy algorithms

Recursion - again

Your task from the last lecture: writing a recursive linear search Recursion is relatively easy:

if val == seq[0]:
 return i
else:
 return rl\_search(seq[1:], val, i=1) . And we need a base case: if not seq: # ony return lose

the compete come

| def rl search(seq, val, i=0):
| if not seq:
| return None
| if val = seq[0]:
| return rl, search(seq[::], val, i=1)
| return rl, search(seq[::], val, i=1) Can we improve this?

the complete code

How does this recursion work



: def fib(n): : if n <= 1

Recursion: practical issues oton depth :

> Each function call requires some bookkeeping Compilers/interpreters allocate space on a stack for the bookkeeping for each function call

- . Most environments limit the number of recursive calls: long chains of recursion is likely to be errors
- \* Tail recursion (e.g., our recursive search example) is easy to convert to
- iteration It is also easy to optimize, and optimized by many compilers (not by the
- Python interpreter)

Another recursive example an algorithm course is required to in Fibonacci numbers are defined as

Fo = 0  $F_1 = 1$  $F_n = F_{n-1} + F_{n-2}$  for n > 1

· Recursion is common in math, and maps well to the recursive algorithms

recursion, each function call creates two calls to self

: if n <= 1:
: return n
: return fib(n-2) + fib(n-1)</pre>

. We follow the math exactly, but is this code officiant?

Visualizing binary recursion



Brute force

In some cases, we may need to enumerate all possible cases (e.g., to find the best solution)

· Common in combinatorial problems . Often intractable, practical only for small input sizes

It is also typically the beginning of finding a more efficient approach

Brute force

· Segmentation is prevalent in CI egmentation is prevalent in CL

— Examples include finding words: tokenization (particularly for writing sy
that do not use white space)

— Finding sub-vord units (e.g., morphemes, or more specialized applicatio
compound splitting)

— Psycholingsistics: how do people extract words from continuous speech?

We consider the following problem:
 Given a metric or score to determine the "best" segmentation
 We enumerate all possible ways to segment, pick the one with the best score

. How can we enumerate all possible segmentations of a string?

Enumerating segmentations

s e g m e n t t h i s 0 0 0 0 0 0 0 1 0 0 0 s e g m e n t t h i s 0 0 1 0 0 1 0 0 1 0 seg men tth is

- . '1' means there is a boundary at this po - Problem is now enumerating all possible binary strings of length  $\pi - 1\,$

(this is binary counting)

Segmentation

: def segment\_r(seq): : if len(seq) == : yield [seq] #:
for seg in segment\_r(seq[i:]):
 yield [seq[0]] + seg
 yield [seq[0] + seg[0]] + seg[i:]

. Can you think of a non-recursive solution?

Divide and conquer

- trivial to solve . Once small parts are solved, the results are combined
- Goes very well with recursion
  - We have already seen a particular flavor: binary sea
  - . The algorithms like binary search are sometimes called dec

The general idea is dividing the problem into smaller parts until it becomes

Divide and conquer Big problem

# Divide and conquer

- Task: find the closest two points
  - Direct solution:  $20 \times 20 = 400 \text{ comparisons}^3$
  - . Divide
  - 10 × 10 + 10 × 10 = 200 comp Combine: pick the minimum of the individual solutions
    - . Gain is higher when n is larger, and we divide further

## Greedy algorithms

- . An algorithm is greedy if it optimizes a local constraint
- . For some problems, greedy algorithms result in correct sol
- . In others they may result in 'good enough' solutions
- . If they work, they are efficient
- An important class of graph algorithms fall into this category (e.g., finding shortest paths, scheduling)

# Dynamic programming

- ning is a method to save earlier results to red
- . It is sometimes called memoization (it is not a typo) \* Again, a large number of algorithms we use fall into this category, including common parsing algorithms

## Summary

- \* We saw a few general approaches to (efficient) algorithm design Designing algorithms is not a mechanical pro
- . There are other common patterns, including
- Backtracking, Branch-and-bound
  - Randomized algorithms
     Distributed algorithms (sometime called swarm optimization)

Better solutions for Fibonacci numbers

- Transform
- Designing algorithms is difficult but analyzing them is even more difficult (next topic)

· Analysis of algorithms Reading: textbook (Goodrich, Tamassia, and Goldwasser 2013) chapter 3

# memoization Linear search

a little bit of oots

Dynamic programming mple: Fibo

Divide and conquer

Greedy algorithms

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set s = s - c
 repeat 1 & 2 until s = 0

Is this algorithm correct?

. This is probably the most common example

Divide and conquer does not always yield good re-should be less than the gain from division

merge sort and quick sort (coming soon)
 integer multiplication
 matrix multiplication
 fast Furrier transform (FFT)

Many of the important algorithms fall into this category:

• We want to produce minimum number of coins for a particular sum s

· Is it correct if the coin values were limited Euro coins?

. We save the results calculated in a dictionary,

· if the result is already in the dictionary, we ret . Otherwise we calculate recursively as before The difference is big, but there is also a 'neater' solution without (explicit)

Think about coins of 10, 30, 40 and apply the algorithm for the sum value of

```
def rl_search(seq, val, i=0)
   if not seq:
       return None
   if val == seq[0]:
      return i
                    return rl_se

-- i+1)
```

Which one is faster, and why?

Which one is faster/better?

Segmentation

```
segment_r(seq):
segs = []
segs = []
if len(seq) == 1:
    return [seq]
for seg in segment_r(seq[1:]):
    segs.append([seq[0]] + seg)
    segs.append([seq[0]] + seg[0]] + seg[1:])
 return segr
```

# Acknowledgments, credits, references

\* Some of the slides are based on the previous year's course by Corina Dima.

Goodrich, Michael T., Roberto Tamassia, and Michael H. Goldwasser (2013).

Data Structures and Algorithms in Python. John Wiley & Sons, Incorporated. 1841

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