Algorithmic patterns Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de Winter Semester 2020/21

- - ome common approa Revisiting recursion Brute force Divide and conquer Greedy algorithms

How does this recursion work

: def fib(n): : if n <= 1

. And we need a base case: if not seq: # ony return lose

oton depth :

Recursion - again

Recursion is relatively easy:

if val == seq[0]:
 return i
else:
 return rl_search(seq[1:], val, i=1)

Can we improve this?

the complete code

the compete come

| def rl search(seq, val, i=0):
| if not seq:
| return None
| if val = seq[0]:
| return rl, search(seq[::], val, i=1)
| return rl, search(seq[::], val, i=1)

Recursion: practical issues

Your task from the last lecture: writing a recursive linear search

Each function call requires some bookkeeping

- Compilers/interpreters allocate space on a stack for the bookkeeping for each function call
- . Most environments limit the number of recursive calls: long chains of recursion is likely to be errors
- * Tail recursion (e.g., our recursive search example) is easy to convert to iteration
- It is also easy to optimize, and optimized by many compilers (not by the
- Python interpreter)

Another recursive example an algorithm course is required to in Fibonacci numbers are defined as

Fo = 0

 $F_1 = 1$ $F_n = F_{n-1} + F_{n-2}$ for n > 1

- · Recursion is common in math, and maps well to the recursive algorithms
- : if n <= 1:
 : return n
 : return fib(n-2) + fib(n-1)</pre> recursion, each function call creates two calls to self
- . We follow the math exactly, but is this code officiant?



Brute force

- In some cases, we may need to enumerate all possible cases (e.g., to find the best solution) · Common in combinatorial problems
- . Often intractable, practical only for small input sizes

It is also typically the beginning of finding a more efficient approach

Brute force

- · Segmentation is prevalent in CI
 - egmentation is prevalent in CL

 Examples include finding words: tokenization (particularly for writing sy
 that do not use white space)

 Finding sub-vord units (e.g., morphemes, or more specialized applicatio
 compound splitting)

 Psycholingsistics: how do people extract words from continuous speech?
- We consider the following problem:
 Given a metric or score to determine the "best" segmentation
 We enumerate all possible ways to segment, pick the one with the best score
- . How can we enumerate all possible segmentations of a string?

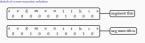
Segmentation

: def segment_r(seq): : if len(seq) == : yield [seq]

. Can you think of a non-recursive solution?

#:
for seg in segment_r(seq[i:]):
 yield [seq[0]] + seg
 yield [seq[0] + seg[0]] + seg[i:]

Enumerating segmentations



- . '1' means there is a boundary at this po
- Problem is now enumerating all possible binary strings of length $\pi 1\,$ (this is binary counting)

Divide and conquer

- The general idea is dividing the problem into smaller parts until it becomes trivial to solve
- . Once small parts are solved, the results are combined
- Goes very well with recursion
- We have already seen a particular flavor: binary sea
- . The algorithms like binary search are sometimes called dec

Divide and conquer Big problem

ŧ.

Divide and conquer

- · Task: find the closest two points
 - Direct solution:
 20 × 20 = 400 comparisons³
 - Divide

 - 10 × 10 + 10 × 10 = 200 comp
- Combine: pick the minimum of the individual solutions
 - Gain is higher when n is larger, and we divide further

Greedy algorithms

- · An algorithm is greedy if it optimizes a local constraint
- For some problems, greedy algorithms result in correct s
- . In others they may result in 'good enough' solutions
- · If they work, they are efficient
- An important class of graph algorithms fall into this category (e.g., finding shortest paths, scheduling)

Dynamic programming

- . Dynamic programming is a method to save earlier results to reduce computation
- It is sometimes called memoization (it is not a typo)
- · Again, a large number of algorithms we use fall into this category, including
- common parsing algorithms

- . We saw a few general approaches to (efficient) algorithm design Designing algorithms is not a mechanical procedure: it req
 - . There are other common patterns, including
- Backtracking, Branch-and-bound
 Randomized algorithms
 Distributed algorithms (sometime called swarm optimization)
 - Transformation
 - Designing algorithms is difficult but analyzing them is even more difficult
 - (next topic)
 - · Analysis of algorithms
 - - Reading: textbook (Goodrich, Tamassia, and Goldwasser 2013) chapter 3

Better solutions for Fibonacci numbers

def fibb(n):
 if n <= 1:
 recurs n
 a, b = 0, 1
 for i in range(0, n):
 a, b = b, a + b
 return a

Divide and conquer

- Task: find the closest two points Direct solution:
- $20 \times 20 400$ comparisons¹
- . Divide
- 10 × 10 + 10 × 10 = 200 comp Combine: pick the minimum of the individual solutions
 - . Gain is higher when n is larger, and we divide further

Divide and conquer

- . This is probably the most common example
- Divide and conquer does not always yield good res should be less than the gain from division Many of the important algorithms fall into this category:
 - merge cert and quick sort (coming soon)
 integer multiplication
 matrix multiplication
 fast Furrier transform (FFT)

Greedy algorithms

- · We want to produce minimum number of coins for a particular sum s
- Pick the largest coin c <= s 2. set s = s - s
- 3. repeat 1 & 2 until s = 0
- . Is this algorithm correct * Think about coins of 10, 30, 40 and apply the algorithm for the sum value of 60
- . Is it correct if the coin values were limited Euro coins?

Dynamic programming mole: Fibe

idef memofib(n, memo = {0: 0, 1:1}):
if n not in memo:
 memo[n] = memofib(n-1) + memofib(n-2)
return memo[n]

- . We save the results calculated in a dictionary,
- . if the result is already in the dictionary, we reti . Otherwise we calculate recursively as before The difference is big, but there is also a 'neater' solution without (explicit)
 - memoization

Linear search

a little bit of cotten

def rl_nearch(seq, val, i=0):
 if not seq:
 return None
 if val = seq[0]:
 return i return rl_m -- i-1)

Which one is faster, and why?

Segmentation

segment_r(seq):
segs = []
if len(seq) == i:
 return [seq]
for seg in segment_r(seq[i:]):
 segs.append([seq[i:] + seq[i:]) + seg[i:])
 segs.append([seq[i:] + req[i:]) + seg[i:])

return segi

binductor. More or recursion. Some common algorithm patients	Interduction. More on recording. Some constant algorithm patterns.
Acknowledgments, credits, references	
Some of the slides are based on the previous year's course by Corina Dima.	
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