Bottom-up Chart Parsing: the CKY algorithm Data Structures and Algorithms for Computat (ISCL-BA-07) Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de Winter Semester 2021/22

Parsing so far * Parsing is the task of automatic syntactic analysis

- For most practical purposes, context-free grammars are the most useful formalism for parsing
 We can formulate parsing as
- e can occurrence passing as

 Top-down: begin with the start symbol, try to produce the input string to be
 parsed

 Bottom up: begin with the input, and try to refuce it to the start symbol · Both strategies can be cast as search with backtracking

Backtracking parsers are inefficient: they recompute sub-tree



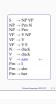


I saw her duck















→ NP VP

 $NP \rightarrow Pm N$

 $NP \rightarrow Prn$? $NP \rightarrow Prn$ $VP \rightarrow V$ NF $VP \rightarrow V$ $VP \rightarrow V$ $V \rightarrow duck$ $V \rightarrow duck$ $V \rightarrow saw$



Dealing with ambiguity



Dealing with ambiguity









Dealing with ambiguity



Dealing with ambiguity





 $S \rightarrow NP VI$ $NP \rightarrow Prn N$



$S \rightarrow NPVP$	
$NP \rightarrow Pm N$	
$NP \rightarrow Pm$	
$VP \rightarrow V NP$	
$VP \rightarrow V$	
$VP \rightarrow VS$	6
$N \rightarrow duck$	
V → duck	
$V \longrightarrow saw$	
$Pm \rightarrow I$	
$Prn \rightarrow she$	
$Prn \rightarrow her$	

Dealing with ambiguity

 \rightarrow NP VI \rightarrow Prn N NE $NP \rightarrow Prn$ $NP \rightarrow Prn$ $VP \rightarrow V$ NE $VP \rightarrow V$ $VP \rightarrow V$ N → duck V → duck V → saw $\operatorname{Prn} \to \operatorname{I}$ $\operatorname{Prn} \to \operatorname{she}$

Prn → he

Dealing with ambiguity



→ NP VI → Pm N NP $NP \rightarrow Pm N$ $NP \rightarrow Pm$ $VP \rightarrow V NP$ $VP \rightarrow V$ $VP \rightarrow V S$ N V V → duck → duck → saw Pm → I Prn → she

Dealing with ambiguity







Dealing with ambiguity



Dealing with ambiguity

Dealing with ambiguity





 \rightarrow NP VP NP → Prn N

 $NP \rightarrow Prn$ $NP \rightarrow Prn$ $VP \rightarrow V$ $VP \rightarrow V$ $VP \rightarrow V$

N V V → duck

 $Prn \to I$ Prn → sh Prn -- be



Dealing with ambiguity



How to represent multiple parses





Chomsky normal form (CNF) . A CFG is in CNF, if the rewrite rules are in one of the following forms

CKY algorithm

- The CKY (Cocke-Kasami-Younger) parsing algorithm is a dyr programming algorithm
- Space complexity is O(n²)
- relaxed, but not common)
- . It processes the input bottom up, and saves the intermediate results on a chart Time complexity for recognition is O(n⁵)
- It requires the CFG to be in Chomsky normal form (CNF) (can somewhat be

- A → BC
- where A, B, C are non-ter
- · Any CFG can be converted to CNF
- Resulting grammar is weakly equivalent to the original gran
 it generates/accepts the same language
 but the derivations are different

1. Eliminate the ϵ rules: if $A \rightarrow \epsilon$ is in the grammar – replace any rule $B \rightarrow \alpha A \beta$ with two rules

Converting to CNF: example

\rightarrow NP VI

- $VP \rightarrow V NP$ $VP \rightarrow V$ $N \rightarrow cat$ VP N N V → dog → bites
- VP → bites
- Remove the rule A → B
 Repeat the percoss until no unit rules remain
 Binarize all the non-binary rules with non-terminal on the RHS: for a rule A → X₁ X₂ ... X₆;
 Replace the rule with A → A₁ X₂... X₆, and add A₁ → X₁ X₂.
 Repeat the process until all near rules are binary to the process until all representations.

 $\begin{array}{c} B \to \alpha \, \beta \\ B \to \alpha \, A' \, \beta \end{array}$

Converting to CNF

