Algorithmic patterns Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de Winter Semester 2021/22 Recursion

the complete code the compete come

| def rl search(seq, val, i=0):
| if not seq:
| return None
| if val = seq[0]:
| return rl, search(seq[::], val, i=1)
| return rl, search(seq[::], val, i=1) if val -- meq[0]:
 return i
else:
 return rl_mearch(meq[::], val, i-:) Can we improve this?

Recursion: practical issues ration depth :

· Recursion is relatively easy:

. And we need a base case: if not meg: # onp

- Each function call requires some bookkeeping
 Compilers/interpreters allocate space on a stack for the bookkeeping for each function call
- Most environments limit the number of recursive calls: long chains of recursion are likely to cause errors

Your task from the first lecture: writing a recursive linear search

- * Tail recursion (e.g., our recursive search example) is easy to convert to iteration
- It is also easy to optimize, and optimized by many compilers (not by the Python interpreter)

Visualizing binary recursion

Brute force

- rate all possible cases (e.g., to find the best solution)
- Common in combinatorial problems
- · Often intractable, practical only for small input sizes
- It is also typically the beginning of finding a more efficient approach

Segmentation



. Can you think of a non-recursive soluti

Overview

- - Revisiting recursion
 Brute force
 Divide and conque
 Greedy algorithms

How does this recursion work



Another recursive example every algorithm course is required to

Fibonacci numbers are defined as Fo = 0

 $F_1 = 1$ $F_n = F_{n-1} + F_{n-2}$ for n > 1· Recursion is common in math, and maps well to the recursive algorithms

- : def fib(n): : if n <= 1: : return n : return fib(n-2) + fib(n-1)
- Note that we now have binary recursion, each function call creates two calls to self . We follow the math exactly, but is
- this code officiant?

Complexity of (naive) Fibonacci algorithm ursion tree for fib(7)



Brute force

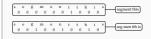
- · Segmentation is prevalent in CL
- eggmentation is prevaited in CL.

 Examples include finding words: tokenization (particularly for writing sy
 that do not use within space)

 Finding sub-rood units (e.g., morphemes, or more specialized applicatio
 compound splitting)

 Psycholinguistics: how do people extract words from continuous speech?
- We consider the following problem:
 Given a metric or score to determine the "best" segmentation
 We enumerate all possible ways to segment, pick the one with the best score
- How can we enumerate all possible segmentations of a string?

Enumerating segmentations



. '1' means there is a boundary at this pos-

- \star Problem is now enumerating all possible binary strings of length n-1
- (this is binary counting)

- · The general idea is dividing the problem into smaller parts until it becomes
- trivial to solve
- Once small parts are solved, the results are combined . Goes well with recursion
- We have already seen a particular flavor: binary search
- The algorithms like binary search are sometimes called d

Divide and conquer

· Task: find the closest two points

Divide and conquer

- Direct solution:
 20 × 20 = 400 comparisons²
- Divide
- 10 × 10 + 10 × 10 = 200 com
- Combine: pick the minimum of the individual solutions



Divide and conquer

- . This is probably the most common pattern
- Divide and conquer does not always yield good results, the cost of merging
- should be less than the gain from the division(s)

 Many of the important algorithms fall into this category

 - merge sort and quick sort (coming soon)
 integer multiplication

 - matrix multiplication
 fast Furrier transform (FFT)

Greedy algorithms

- . We want to produce minimum number of coins for a particular sum s Pick the largest coin c <= s
 - 2. set s = s c 3. repeat 1 & 2 until s = 0
- Is this algorithm correct?
- Think about coins of 10, 30, 40 and apply the algorithm for the sum value of 60
- . Is it correct if the coin values were limited Euro coins?

Dynamic programming

- : def memofib(n, memo = {0: 0, 1:1}): if n not in memo: nemo[n] = memofib(n-1) + memofib(n-2) return memo[n]
 - · We save the results calculated in a dictionary,
 - . if the result is already in the dictionary, we return without recursion
 - · Otherwise we calculate recursively as before
 - The difference is big, but there is also a 'neater' solution without (explicit) memoization

Summary

* We saw a few general approaches to (efficient) alg

- Designing algorithms is not a mechanical procedure: it requires on
 There are other common patterns, including
 Backtracking, Branch-and-bound

 - Randomized algorithms
 Distributed algorithms (sometime called swarm optimization)
- . Designing algorithms is difficult (possibly, not as difficult as analyzing them) Next:
- * Reading: Goodrich, Tamassia, and Goldwasser (2013, chapter 12)



Divide and conquer

- Task: find the closest two points
- Direct solution:
 20 × 20 = 400 comparisons¹ Divide
- 10 × 10 + 10 × 10 200 cc
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Greedy algorithms

- · An algorithm is greedy if it optimizes a local constrain For some problems, greedy algorithms result in correct
- . In others they may result in 'good enough' solutions
- . If they work, they are efficient
- An important class of graph algorithms fall into this category (e.g., finding shortest paths, scheduling)

Dynamic programming

- . Dynamic programming is a method to save earlier results to reduce computation
- It is sometimes called memoization (it is not a typo)
- * Again, a large number of algorithms we use fall into this category, including
- common parsing algorithms

Complexity of Fibonacci algorithm with dynamic pogramming O recu ion tree for fib(7)

Nearest neighbors

Define and implement a divide-and-conquer algorithm for nearest neighborhoblem, which divides the input into two until the solution becomes trivia

Analyze your algorithm and compare to the naive vers implementation was provided in the previous lecture)

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Segmentation without yield	Acknowledgments, credits, references
def segment_(seq): segs = (Some of the slides are based on the previous year's course by Cortna Dima. Goodends, Michael T., Roberto Tamassia, and Michael H. Colderassor (2013). Data Structures and Algorithms in Python. John Wiley & Sons, Incorporated, usac \$781115(20734.
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