Shortest path algorithms Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III

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Shortest path

- Finding shortest paths on a weighted (directed) graph is one of the most common problems in many fields
 Applications include
- Navigation

Shortest paths on weighted graphs

- · Different versions of the problem:
- Single source shortest path: find shortest path from a source node to all others single target (sometimes called sink) shortest path: find shortest path from all nodes to a target node. Source to target: from a particular source node to a particular target node
 All pairs: shortest paths between all pairs of nodes
 Restrictions on weights:

 - Euclidean weights
 Non-negative weights
 Arbitrary weights

Dijkstra's algorithm

Shortest paths on unweighted graphs

 A BFS search tree gives the shortes path from the source node to all other nodes

. The BFS is not enough on weighted graphs Shortest-cost path may be longer in

- · Dijkstra's algorithm is a 'weighted' version of the BFS
- The algorithm finds shortest path from a single source node to all connected nodes
- Weights has to be non-negative

Dijkstra's algorithm

- . It is a greedy algorithm that grows a 'cloud' of nodes for which we know the
- shortest paths from the source node The new nodes are included in the cloud in order of their shortest paths from
- the source node
- The algorithm is also similar to Prim-Jarník algorithm used for finding MST

Dijkstra's algorithm

- We maintain a list D of mi know distances to each node
- At each step
- Can be more efficient if Q is implemented using a (adaptable) priority queue
- 4: Q ← nodes
 5: while Q is not empty do
 6: Find the node v with min D[v]
 7: for each edge (v, w) do
 8: if D[v] + w[(v, w)] < D[w] then
 9: D[v] ← D[v] + w[(v, w)]

 $Q \leftarrow nodes$

1: D[s] ← 0

for each node $v \neq s$ do $D[v] \leftarrow \infty$

10: D contains the shortest distances from s

Dijkstra's algorithm

2

Dijkstra's algorithm

Dijkstra's algorithm



Dijkstra's algorithm 2









