NFA determinization Data Structures and Algorithms for Computational Linguistics III (ISCL-BA-07)

Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de

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NFA recognition (again)

- 1. Start at q 2. Take the next input, mark all possible next
 - states If an accepting state is marked at the end of the input, accept

2. Take the next input, mark all possible next 3. If an accepting state is marked at the end of

Recap

- "Bible Stable automata CORRE" in New Javes

 Deterministic (DEA): linear recognition time

 Deterministic (NFA): sometimes more intuitive, easy to define, but expor
 - The DFA and NFA are equivalent: for any language recognized by an NFA
 - there is also a DFA recognizing the same language
 - Then, the question is: how can we determinize an NFA to obtain an equivalent DFS

1. Start at qo

NFA recognition (again)



- 2. Take the next input, mark all possible next states 3. If an accepting state is marked at the end of
 - the input, accept

Input a b a b



tabab

- $\begin{array}{l} 1. \ \ Start \ at \ q_0 \\ 2. \ \ Take \ the \ next \ input, \ mark \ all \ possible \ next \end{array}$
- 3. If an accepting state is marked at the end of the input, accept

NFA recognition (again)



1. Start at qo 2. Take the next input, mark all possible next

1. Start at qo

the input, accept

- If an accepting state is marked at the end the input, accept



Input a b a b

NFA recognition (again)

1. Start at qo 2. Take the next input, mark all possible next

- If an accepting state is marked at the end of the input, accept
- The process is deterministic, and finite-state

Determinization

Intuition: remember the parallel NFA recognition. We can consider an NFA being a deterministic machine which is at a set of states at any given time.

- Subset construction (sometimes called power set construction) uses this intuition to convert an NFA to a DFA

The algorithm can be modified to handle c-transitions (or we can eliminate)

c's as a preprocessing step)

The subset construction NEA

transition table with subsets a {0,1} {0,1} (0, 2) (0) (0, 1, 2) (0, 1) {0, 1} (0,1,2) (0,1) * {1,2} (0,1,2) * {0,1,2} {0,1,2} 60 13

The subset construction

transition table without useless/inaccessible sta

· What language do they recognize?

Yet another exercise The subset construction ${\bf *}$ In worst case, resulting DFA has 2^n nodes Determinize the following automaton Worst case is rather rare, number of nodes in an NFA and the converted DFA In practice, we do not need to enumerate all 2ⁿ subsets We've already seen a typical problematic case: -0 a,b 2 a,b 3 a,b 4 Summary Acknowledgments, credits, references + PSA are efficient tools with many applications * FSA have two flavors: DFA, NFA (or maybe three: ε-NFA) B. Hopeneth, John E. and Jeffrey D. Ullmans (1899). Introduction to Automate Theory, Languages, and Computation. Addison Worley Service to Compute Science and Information Processing, Addison-Worley-ruse 970020102998.

Juraficky, Daniel and James H. Martin (2009). Speech and Language Processing, Can Introduction to Natural Language Processing. Computational Linguistics, and Speech Introduction to Natural Language Processing. Computational Linguistics, and Speech Recognitions, second edition. Pleasant Prefix I feld. Introduction to Vision II Supress of Profits (1997). . DFA recognition is linear, recognition with NFA may require Reading suggestion: Hopcroft and Ullman (1979, Ch. 263), Jurafsky and Martin (2009, Ch. 2) • Minis