Finite state transducers Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III

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* A finite state transducer (PST) is a finite state machine where transitions are conditioned on pairs of symbols

The machine moves between the states based on an input symbol, while it outputs the corresponding output symbol

• An FST encodes a relation, a mapping from a set to another

The relation defined by an PST is called a regular (or rational) relation

aba -- abb

Where do we use FSTs? Morphological analysis

Finite state transducers

- Spelling correction
- Transliteration
- Speech recognition
- Grapheme-to-phone

Where do we use FSTs?

- * POS tagging (not typical, but done) partial parsing / chunking

Where do we use FSTs?

Formal definition

 Σ_L is the input alphabet

Σ₀ is the output alphabet

Q a finite set of states

 $q_0^{}$ is the start state, $q_0^{} \in Q$ $F\,$ is the set of accepting states, $F\subseteq Q$ Δ is a relation $(\Delta\colon Q\times \Sigma_1\to Q\times \Sigma_o)$

A finite state transducer is a tuple $(\Sigma_t, \Sigma_o, Q, q_0, F, \Delta)$



In this lecture, we treat an PSA as a simple PST that outputs its input the edge label 'a' is a shorthand for 'aca'.

Closure properties of FSTs

Like PSA, PSTs are c

- Concatenation . Kleene star
- Complon
- . Reversal
- . Union
- Intersec . Impreine

Composition

FST inversion Since an FST enc

- $\star\,$ Inverse of an PST swaps the input symbols with output symbols We indicate inverse of an PST M with M⁻¹



Note: (1) It is important to express the ambiguity. (2) This gets interesting if we can 'compose' these automata.

FST composition

M₁ bb м, M₁ ∅

M₁ baab М2 . Can we compose two PSTs without running them sequentially?

FST composition









FST compositi





FST composition



FST composition





Projection

output language





PST determinization

- A deterministic PST has unambiguou transitions from every state on any input symbol . We can extend the subset construction to
- · Determinization of PSTs means cor a subsequential PST
- · However, not all FSTs can be determiniz



Sequential FSTs

- A sequential PST has a single transit each state on every input symbol
- . Output symbols can be strings, as well as a The recognition is linear in the length of
- input
- However, sequential PSTs do not allow ambiguity

Subsequential FSTs

- • A k -subsequential PST is a sequential PST which can output up to k strings at an accepting state
- Subsequential t
- Recognition time is still lin



The ... e.g., - baa → bba - baa → bbb

An exercise

Convert the follo



Determinizing PSTs

Can you convert the following PST to a sul ential PST?



Note that we cannot 'determine' the output on first input until reaching the final input

FSA vs FST

- + PSA are acceptors, PSTs are transducers
 - FSA accept or reject their input, FSTs produce output(s) for the inputs they FSA define sets, FSTs define relat

 - FSA define sets, FSIs define relations between sets
 FSTs share many properties of FSAs. However,
 FSTs are not closed under intersection and complen
 We can compose (and invert) the FSTs
 Determinizing FSTs is not always possible
 - Both PSA and PSTs can be weighted (not covered in this course)
 - Next:

- Parsing

References / additional reading material

- Jurafsky and Martin (2009, Ch. 3)
 - · Additional references include
 - Roche and Schabes (1996) and Roche and Schabes (1997): FSTs and their use in NLP
 - Mohri (2009): weighted PSTs

FSA and regular languages

References / additional reading material (cont.)

- ☐ Jurafsky, Daniel and James H. Martin (2009). Speech and Language Processing: As Introduction to Natural Language Processing. Computational Linguistics, and Speech Recognition. second edition. Processor Proentice 4-Hill. sace 579-6.33-604196-3.
 ☐ Mohri, Mehryar (2009). "Weighted automata algorithms". In: Handbook of
- pp. 213–254.

 Roche, Emmanuel and Yves Schabes (1996). Introduction to Finite-State Devices
 in Natural Language Processing Technical Report. Tech. rep. TR96–13. Mitsubishi
 Electric Research Laboratories. usa:
- http://www.merl.com/publications/docs/TR96-13.pdf.
 (1997). Finite-state Language Processing. A Bradford book. MIT Press. as

