NOPT042 Constraint programming: Tutorial 9 - Implicit constraints

```
In [1]: %load_ext ipicat
```

Picat version 3.7

Example: Seesaw

Adam, Boris, and Cecil want to sit on a 10-feet long seesaw such that they are at least 2 feet apart and the seesaw is balanced. Adam weighs 36 lbs, Boris 32 lbs, and Cecil 16 lbs. Write a general model. You can assume that the length is even, the distance is integer, and that they can only sit at integer points.

(Problem from Marriott & Stuckey "Programming with Constraints", page 257. Instance from R. Barták's tutorial.)

```
In [2]: !cat seesaw/instance1.pi
% sample instance
instance(NumPeople, Length, Distance, Weights) =>
    NumPeople = 3,
    Length = 10,
    Distance = 2,
    Weights = [36, 32, 16].
```

Possible decision variables?

- · Position on the seesaw for each person.
- Distances between persons, position of the first person, and order of persons.
- Person or empty for each position on the seesaw.

Global constraints? Symmetry breaking? Multiple modeling? Search strategies?

```
instance1.pi instance3.pi instance5.pi seesaw2.pi seesaw4.pi
instance2.pi instance4.pi seesaw1.pi seesaw3.pi

In [4]: !time picat seesaw/seesaw1.pi instance4.pi
!time picat seesaw/seesaw2.pi instance4.pi
!time picat seesaw/seesaw3.pi instance4.pi
!time picat seesaw/seesaw4.pi instance4.pi
!time picat seesaw/seesaw4.pi instance4.pi
```

```
[-16, -15, -14, -13, -12, -11, -10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 6, 8, 7, 9, 14, 15,
10,16,11,12,13]
         0m39.806s
real
user
         0m39.819s
sys
         0m0.011s
[-16, -15, -14, -13, -12, -11, -10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 6, 8, 7, 9, 14, 15,
10,16,11,12,13]
real
         0m31.246s
user
         0m31.199s
         0m0.031s
SYS
[-16, -15, -14, -13, -12, -11, -10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 6, 8, 7, 9, 14, 15,
10,16,11,12,13]
real
         0m48.420s
user
         0m48.440s
SYS
         0m0.001s
[-8,0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,-7,-6,-5,-4,-3,-9,-10,-13,-12,-
11, -16, -14]
real
         0m0.046s
user
         0m0.018s
         0m0.026s
sys
```

Example: Golomb's ruler

A Golomb's ruler is an imaginary ruler with n marks such that the distance between every two marks is different. Find the shortest possible ruler for a given n.

(The solution for N=28 was announced on Nov 23, 2022! The length is 585.)

- What length are you able to solve in reasonable time?
- Add suitable implicit constraints. (We will discuss this in class.)

Redundant (implicit) constraints

Redundant constraints do not restrict the solution set but rather express properties of a solution from a different viewpoint. This can lead to

- · faster domain reduction.
- a significant boost in propagation,
- improved communication between variables.

We have already seen one example last week in the Magic sequence problem: adding the scalar_product constraint.

Implicit constraints based on the following:

$$dist[i,j] = dist[i,i+1] + dist[i+1,i+2] + \ldots + dist[j-1,j]$$

Now estimate distances by 1, sum from i to j:

```
foreach(I in 1..N-1, J in I+1..N)
    Distances[I,J-I] #>= (J-I)*(J-I+1) div 2,
    Distances[I,J-I] #<= Length - (N-J+I-1)*(N-J+I) div 2
end</pre>
```

In [5]: !picat golomb/golomb.pi 10

CPU time 142.58 seconds. Backtracks: 14554575

length = 55 [0,1,6,10,23,26,34,41,53,55]

In [6]: !picat golomb/golomb-improved 11

CPU time 29.931 seconds. Backtracks: 1224484

length = 72 [0,1,4,13,28,33,47,54,64,70,72]

In [7]: !picat golomb/golomb-improved 11

CPU time 26.573 seconds. Backtracks: 1224484

length = 72 [0,1,4,13,28,33,47,54,64,70,72]