

NOPT042 Constraint programming:

Tutorial 9 - Implicit constraints

```
In [1]: %load_ext ipicat
```

Picat version 3.7

Example: Seesaw

Adam, Boris, and Cecil want to sit on a 10-feet long seesaw such that they are at least 2 feet apart and the seesaw is balanced. Adam weighs 36 lbs, Boris 32 lbs, and Cecil 16 lbs. Write a general model. You can assume that the length is even, the distance is integer, and that they can only sit at integer points.

(Problem from Marriott & Stuckey "Programming with Constraints", page 257.
Instance from R. Barták's tutorial.)

```
In [2]: !cat seesaw/instance1.pi
```

```
% sample instance
instance(NumPeople, Length, Distance, Weights) =>
    NumPeople = 3,
    Length = 10,
    Distance = 2,
    Weights = [36, 32, 16].
```

Possible decision variables?

- Position on the seesaw for each person.
- Distances between persons, position of the first person, and order of persons.
- Person or empty for each position on the seesaw.

Global constraints? Symmetry breaking? Multiple modeling? Search strategies?

```
In [3]: !ls seesaw/
```

```
instance1.pi  instance3.pi  instance5.pi  seesaw2.pi  seesaw4.pi
instance2.pi  instance4.pi  seesaw1.pi    seesaw3.pi
```

```
In [4]: !time picat seesaw/seesaw1.pi instance4.pi
!time picat seesaw/seesaw2.pi instance4.pi
!time picat seesaw/seesaw3.pi instance4.pi
!time picat seesaw/seesaw4.pi instance4.pi
```

```
[-16,-15,-14,-13,-12,-11,-10,-9,-8,-7,-6,-5,-4,-3,-2,-1,0,1,2,6,8,7,9,14,15,10,16,1
1,12,13]
```

```

real    0m25.497s
user    0m25.452s
sys     0m0.008s
[-16,-15,-14,-13,-12,-11,-10,-9,-8,-7,-6,-5,-4,-3,-2,-1,0,1,2,6,8,7,9,14,15,10,16,1
1,12,13]

real    0m25.505s
user    0m25.481s
sys     0m0.016s
[-16,-15,-14,-13,-12,-11,-10,-9,-8,-7,-6,-5,-4,-3,-2,-1,0,1,2,6,8,7,9,14,15,10,16,1
1,12,13]

real    0m40.777s
user    0m40.758s
sys     0m0.012s
[-8,0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,-7,-6,-5,-4,-3,-9,-10,-13,-12,-11,-16,-
14]

real    0m0.022s
user    0m0.013s
sys     0m0.004s

```

Example: Golomb's ruler

A [Golomb's ruler](#) is an imaginary ruler with n marks such that the distance between every two marks is different. Find the shortest possible ruler for a given n .

(The solution for $N=28$ was announced on Nov 23, 2022! The length is 585.)

- What length are you able to solve in reasonable time?
- Add suitable implicit constraints. (We will discuss this in class.)

Redundant (implicit) constraints

Redundant constraints do not restrict the solution set but rather express properties of a solution from a different viewpoint. This can lead to

- faster domain reduction,
- a significant boost in propagation,
- improved communication between variables.

We have already seen one example last week in the Magic sequence problem: adding the `scalar_product` constraint.

Implicit constraints based on the following:

$$dist[i, j] = dist[i, i + 1] + dist[i + 1, i + 2] + \dots + dist[j - 1, j]$$

Now estimate distances by 1, sum from i to j :

```

foreach(I in 1..N-1, J in I+1..N)
  Distances[I,J-I] #>= (J-I)*(J-I+1) div 2,
  Distances[I,J-I] #<= Length - (N-J+I-1)*(N-J+I) div 2
end

```

In [5]: `!picat golomb/golomb.pi 10`

CPU time 112.032 seconds. Backtracks: 14554575

```

length = 55
[0,1,6,10,23,26,34,41,53,55]

```

In [6]: `!picat golomb/golomb-improved 11`

CPU time 24.83 seconds. Backtracks: 1224484

```

length = 72
[0,1,4,13,28,33,47,54,64,70,72]

```

In [7]: `!picat golomb/golomb-improved 11`

CPU time 25.994 seconds. Backtracks: 1224484

```

length = 72
[0,1,4,13,28,33,47,54,64,70,72]

```