Hypothesis Testing

Chaklam Silpasuwanchai

Analysis c variance

One-way with 2 levels
One-way with 4 levels
Between-subjects
Two-way

Normality check

Nonparametric tests

Hypothesis Testing

Chaklam Silpasuwanchai

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Overview

Hypothesis Testing

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Analysis variance

One-way with 2 leve One-way with 4 leve Between-subjects Two-way

Normality check

Nonparametri tests

- Analysis of variance
 - One-way with 2 levels
 - One-way with 4 levels
 - Between-subjects
 - Two-way
- 2 Normality check
- Non-parametric tests

Sources

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One-way with 2 levels
One-way with 4 levels
Between-subjects

Normality check

Nonparametrion tests

- Mackenzie, Chapter 6, Hypothesis Testing, Human Computer Interaction: An Empirical Research Perspective, 1st ed. (2013)
- Yatani, Advanced Topics in Human-Computer Interaction, http://yatani.jp/teaching/doku.php?id=2016hci: start

Reminders

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One-way with 2 lev
One-way with 4 lev

One-way with 4 level Between-subjects Two-way

Normality check

Nonparametrio tests

- Next week project proposal presentation. Hard copy and soft copy as usual.
- Next next week, please bring your pc, and install JASP.
 We shall together do "Analysis of Variance" workshops for two weeks.

Analysis of Variance

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Analysis of variance One-way with 2 lev

One-way with 2 level One-way with 4 level Between-subjects Two-way

Normality check

Nonparametri tests

- ANOVA, or F-test, is the main statistical test for factorial experiment
- T test is similar but only two levels
- The main motivation to use statistical test is if we see a difference in mean, is that difference occur by chance or is significant?
- Some definition: Null hypothesis is an assumption of no difference in mean

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Nonparametrio tests

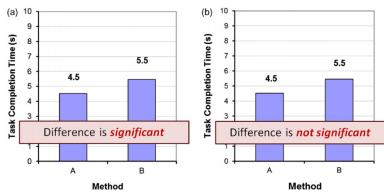


FIGURE 6.2

Difference in task completion time (in seconds) across two test conditions, Method A and Method B. Two hypothetical outcomes are shown: (a) The difference is statistically significant. (b) The difference is not statistically significant.

Figure: Source: Fg. 6.2 (Mackenzie)

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Two-way

Normality check

Nonparametrio

a) [Participant	Met	hod
	Participant	Α	В
	1	5.3	5.7
ſ	2	3.6	4.8
	3	5.2	5.1
	4	3.6	4.5
ſ	5	4.6	6.0
ſ	6	4.1	6.8
	7	4.0	6.0
	8	4.8	4.6
	9	5.2	5.5
	10	5.1	5.6
ĺ	Mean	4.5	5.5
	SD	0.68	0.72

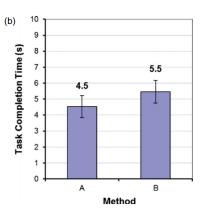


FIGURE 6.3

(a) Data for simulation in Figure 6.2a. (b) Bar chart with error bars showing ±1 standard deviation.

Figure: Source: Fg. 6.3 (Mackenzie)

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One-way with 4 levels
Between-subjects
Two-way

Normality check

Nonparametri

ANOVA Table for Task Completion Time (s)

	DF	Sum of Squares	Mean Square	F-Value	P-Value	Lambda	Pow er
Subject	9	5.080	.564				
Method	1	4.232	4.232	9.796	.0121	9.796	.804
Method * Subject	9	3.888	.432				

FIGURE 6.4

Analysis of variance table for data in Figure 6.3a.

Figure: Source: Fg. 6.4 (Mackenzie): P-value of 0.0121 means that there is less than 2% that the difference occurs by chance. By convention requires less than 0.05 to reject null hypothesis

The mean task completion time for Method A was 4.5 s. This was 20.1% less than the mean of 5.5 s observed for Method B. The difference was statistically significant ($F_{1,9}$ = 9.80, p < .05).

FIGURE 6.5

Example of how to report the results of an analysis of variance in a research paper.

Figure: Source: Fg. 6.5 (Mackenzie): F-value is calculated = between-group variances / within-group variances = 4.232 / .432

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One-way with 2 levels
One-way with 4 levels

Two-way

Normality check

Nonparametri tests

Reporting format (APA):

- If significant, use threshold set .05, .01, .005, .001, .0005, .0001. p is cited as p < .05 instead of p = .0121.
- If **not significant though**, don't report p-value.
- If very close to significant, report exact value.
- Plot with standard error bars
- Report mean and std
- Common nowadays to report effect size
 - **Effect size** measures how "strong" is the significance. SPSS reports **Partial Eta Squared** (η_p^2) .02 means that the factor X by itself accounted for only 2% of the overall (effect + error) variance. Usually around > 0.09 is considered moderate, while > 0.25 is large.

Hypothesis Testing

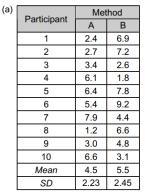
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One-way with 4 levels
Between-subjects

Normality check

Nonparametric



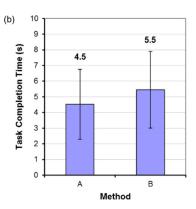


FIGURE 6.6

(a) Data for simulation in Figure 6.2b. (b) Bar chart with error bars showing ±1 standard deviation.

Figure: Source: Fg. 6.6 (Mackenzie)

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Analysis of variance

One-way with 2 levels One-way with 4 levels Between-subjects

Normality check

Nonparametri

ANOVA Table for	Task (Completion Time	(s)				
	DF	Sum of Squares	Mean Square	F-Value	P-Value	Lambda	Pow er
Subject	9	37.372	4.152				
Method	1	4.324	4.324	.626	.4491	.626	.107
Method * Subject	9	62.140	6.904				
FIGURE 6.7							

Analysis of variance for data in Figure 6.3b.

Figure: Source: Fg. 6.7 (Mackenzie). F = 4.324/6.904 = .626. Given p-value of .4491, there is around 45% that the difference occurs by chance.

The mean task completion times were 4.5 s for Method A and 5.5 s for Method B. As there was substantial variation in the observations across participants, the difference was not statistically significant as revealed in an analysis of variances $(F_{7.0} = 0.626, ns)$.

FIGURE 6.8

Reporting a non-significant ANOVA result.

Figure: Source: Fg. 6.8 (Mackenzie). It means that we have not enough evidence to reject null hypothesis, but it **does not mean** that null hypothesis is true either.

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Analysis of variance
One-way with 2 level

One-way with 4
Between-subject

Normality check

Nonparametric

Participant	Test Condition							
Farticipant	Α	В	С	D				
1	11	11	21	16				
2	18	11	22	15				
3	17	10	18	13				
4	19	15	21	20				
5	13	17	23	10				
6	10	15	15	20				
7	14	14	15	13				
8	13	14	19	18				
9	19	18	16	12				
10	10	17	21	18				
11	10	19	22	13				
12	16	14	18	20				
13	10	20	17	19				
14	10	13	21	18				
15	20	17	14	18				
16	18	17	17	14				
Mean	14.25	15.13	18.75	16.06				
SD	3.84	2.94	2.89	3.23				

Figure: Source: Fg. 6.9a (Mackenzie)

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One-way with 4 levels
Between-subjects

Normality check

Nonparametric

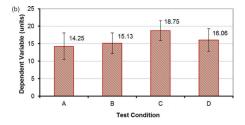


Figure: Source: Fg. 6.9b (Mackenzie)

ANOVA Table for Dependent Variable (units)

	DF	Sum of Squares	Mean Square	F-Value	P-Value	Lambda	Pow er
Subject	15	81.109	5.407				
Test Condition	3	182.172	60.724	4.954	.0047	14.862	.896
Test Condition * Subject	45	551.578	12.257				

Figure: Source: Fg. 6.9c (Mackenzie)

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One-way with 2 levels
One-way with 4 levels
Between-subjects

Normalit check

Nonparametrio tests After ANOVA, to determine exactly which condition is different with which condition, a posthoc analysis is required - either Tukey's test or pairwise comparison with the Bonferroni correction

Scheffe for Dependent Variable (units)

Effect: Test Condition Significance Level: 5 %

	Mean Diff.	Crit. Diff.	P-Value	
A, B	875	3.302	.9003	
A, C	-4.500	3.302	.0032	s
A, D	-1.813	3.302	.4822	
B, C	-3.625	3.302	.0256	s
B, D	938	3.302	.8806	
C, D	2.688	3.302	.1520	

Figure: Source: Fg. 6.11 (Mackenzie)

Example: Between-subjects designs

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One-way with 4 let

Between-subjects

Two-way

Normality check

Nonparametric tests To check whether handedness has a effect on task completion time.

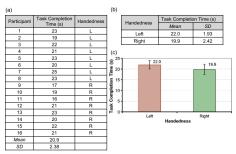


Figure: Source: Fg. 6.12 (Mackenzie)

ANOVA Table for Task Completion Time (s)

	DF	Sum of Squares	Mean Square	F-V alue	P-Value	Lambda	Pow er	
Handedness	1	18.063	18.063	3.781	.0722	3.781	.429	
Residual	14	66.875	4.777					

Figure: Source: Fg. 6.13 (Mackenzie)



Two-way analysis of variance

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One-way with 2 leve
One-way with 4 leve
Between-subjects

Two-way

Normality
check

Nonparametrio tests

- Experiments with two IVs (factors) is called a two-way design
- Analysis of variance of two-way design will give us main effects of each factor and interaction effect
- Interaction effect indicates a relational effect between the IV on the DV

Interaction effects

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Analysis of

One-way with 2 level One-way with 4 level Between-subjects

Normality check

Nonparametric tests

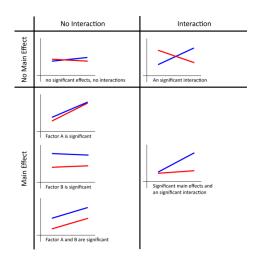


Figure: Source: Yatani's post-hoc tests

Example: 3 x 2 within-subjects design

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Variance
One-way with 2 leve

Two-way

Normality check

Nonparametric tests Let's take both factors as within-subjects, the first factor is device with 3 levels - mouse, trackball, and stylus, and second factor is task with 2 levels - point-select and drag-select. We called this a 3×2 within-subjects design.

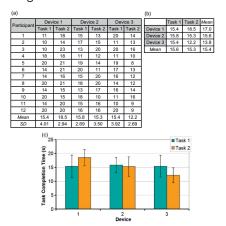


Figure: Source: Fg. 6.14 (Mackenzie)

Example: 3 x 2 within-subjects design

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Variance
One-way with 2 lev

Between-subje Two-way

Normality check

Nonparametric Three effects were observed - the main effect of device and task, and the interaction effect between device and task

ANOVA Table for Task Completion Time (s)

	DF	Sum of Squares	Mean Square	F-Value	P-Value	Lambda	Pow er
Subject	11	134.778	12.253				
Device	2	121.028	60.514	5.865	.0091	11.731	.831
Device * Subject	22	226.972	10.317				
Task	1	.889	.889	.076	.7875	.076	.057
Task * Subject	11	128.111	11.646				
Device * Task	2	121.028	60.514	5.435	.0121	10.869	.798
Device * Task * Subject	22	244.972	11.135				

Figure: Source: Fg. 6.15 (Mackenzie)

Example: 3 x 2 within-subjects design

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Normality check

Nonparametri tests

Reporting:

The grand mean for task completion time was 15.4 seconds. Device 3 was the fastest at 13.8 seconds, while device 1 was the slowest at 17.0 seconds. The main effect of device on task completion time was statistically significant ($F_{2,22} = 5.865$, p <.01). The task effect was modest, however. Task completion time was 15.6 seconds for task 1. Task 2 was slightly faster at 15.3 seconds; however, the difference was not statistically significant $(F_{1,11} = 0.076, \text{ ns})$. The results by device and task are shown in Figure x. There was a significant Device × Task interaction effect $(F_{2,22} = 5.435, p < .05)$, which was due solely to the difference between device 1 task 2 and device 3 task 2, as determined by a Scheffé post hoc analysis.

Figure: Source: Fg. 6.16 (Mackenzie)

Normality check

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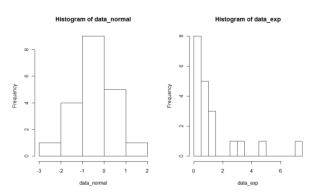
variance
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One-way with 2 level
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Normality check

Nonparametric tests To decide whether we can use ANOVA (also called parametric tests), we check the assumption of normality and homogenity of variances.

• First easy way is to use histogram to check skewness



Normality check

Hypothesis Testing

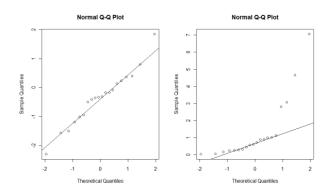
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Normality check

Nonparametric tests • Another way is to use **Q-Q plot**.



Normality check

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One-way with 2 leve
One-way with 4 leve

Normality check

Nonparametrio Two common tests for normality is Shapiro Wilk and Kolmogorov-Smirnov test

- Shapiro-Wilk is more appropriate for small sample sizes (<
 50)
- For example, the null hypothesis of Shapiro-Wilk is that samples are taken from a normal distribution. Here, the p-value is larger than .05, thus is safe to say it's normal. The null hypothesis is same for Kolmogorov-Smirnov

Tests of Normality

	Course	Kolm	Kolmogorov-Smirnov ^a			Shapiro-Wilk		
		Statistic	df	Sig.	Statistic	df	Sig.	
Time	Beginner	.177	10	.200*	.964	10	.827	
	Intermediate	.166	10	.200*	.969	10	.882	
	Advanced	.151	10	.200*	.965	10	.837	

a. Lilliefors Significance Correction



^{*.} This is a lower bound of the true significance.

Homogeneity of variances

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One-way with 2 leve
One-way with 4 leve
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Normality check

Nonparametric tests

- t-test and ANOVA can handle differences in variances up to 4 times between smallest and largest (Howell, 2007)
- Tests that can be use is Levene's test and Bartlett's test (p-value over 0.05 means that the variances are equal)
- In a repeated measures experiment, Sphericity test is used instead - p-value over .05 means that sphericity has not been violated.

Non-parametric tests for ordinal data

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One-way with 2 leve
One-way with 4 leve
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Normality check

Nonparametric tests

- Non-parametric tests make no assumptions for probability distribution
- Downsides of non-parametric tests are loss of information
- For example, 49, 81, 82 are transformed to 1, 2, 3
- In HCI, non-parametric tests are often used for questionnaires data (e.g., using Likert scale) since they are ordinal data.

Non-parametric tests for ordinal data

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variance

One-way with 2 level One-way with 4 level Between-subjects Two-way

Normality check

Nonparametric Four most common non-parametric procedures that work based on the number of conditions and design

Desire	Conditions		
Design	2	3 or more	
Between-subjects (independent samples)	Mann-Whitney U	Kruskal-Wallis	
Within-subjects (correlated samples)	Wilcoxon Signed-Rank	Friedman	

Figure: Source: Fg. 6.29 (Mackenzie)

Example: Mann-Whitney U

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Normality check

Nonparametric tests 10 Mac users and 10 PC users are interviewed about their political views on a 10-point linear scale (1 = very left, 2 = very right). Turns out PC users are a little more "right-leaning"!

Mac Users	PC Users
2	4
3	6
2	5
4	4
9	8
2	3
5	4
3	2
4	4
3	5

Figure: Source: Fg. 6.30 (Mackenzie)

Example: Mann-Whitney U

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One-way with 4 level Between-subjects Two-way

Normality check

Nonparametric tests Given 2 levels and between subject designs,
 Mann-Whitney U is suitable

• Here we found that p = .1418, thus we conclude that no differences were found.

(a)								
Mann-Whitney U for Response								
Grouping Variable: Category for Response								
U	31.000							
U Prime	69.000							
Z-Value	-1.436							
P-Value	.1509							
Tied Z-Value	-1.469							
Tied P-Value	.1418							
# Ties	4							

Figure: Source: Fg. 6.31 (Mackenzie)

Example: Wilcoxon Signed-Rank

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Normality check

Nonparametric tests 10 users rated the design of two media players on a 10-point linear scale (1 = not cool, 10 = really cool). Which test should we use?

Mac Users	PC Users	
2	4	
3	6	
2	5	
4	4	
9	8	
2	3	
5	4	
3	2	
4	4	
3	5	

Figure: Source: Fg. 6.32 (Mackenzie)

Example: Wilcoxon Signed-Rank

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Normality check

Nonparametric tests The Wilcoxon Signed-Rank test found that p = .0242, thus we conclude that no differences were found.

(a)

Wilcoxon Signed Rank Test for MPA, MPB

#0 Differences	2	
# Ties	2	
Z-Value	-2.240	
P-Value	.0251	
Tied Z-Value	-2.254	
Tied P-Value	.0242	

Figure: Source: Fg. 6.33 (Mackenzie)

Example: Kruskal-Wallis

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Normality check

Nonparametric tests

Is it significant?

A20-29	A30-39	A40-49	
9	7	4	
9	3	5	
4	5	5	
9	3	2	
6	2	2	
3	1	1	
8	4 2		
9	7	2	

Figure: Source: Fg. 6-34

(Mackenzie).

(a)

Kruskal-Wallis Test for Acceptability Grouping Variable: Category for Preference

DF 2
Groups 3
Ties 7
H 9.421
P-Value .0090
H corrected for ties 9.605
Tied P-Value .0082

Figure: Source: Fg. 6-35

(Mackenzie).

Example: Kruskal-Wallis

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Nonparametric tests Since there are three conditions, we can further run post-hoc tests to find out the differences in pair. Here, we found the difference between group 1 and 3.

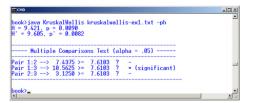


Figure: Source: Fg. 6.36 (Mackenzie)

Example: Friedman Test

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One-way with 2 leve One-way with 4 leve Between-subjects Two-way

Normality check

Nonparametric tests

So, what's the conclusion?

Participant	Α	В	С	D
1	66	80	67	73
2	79	64	61	66
3	67	58	61	67
4	71	73	54	75
5	72	66	59	78
6	68	67	57	69
7	71	68	59	64
8	74	69	69	66

Friedman Test for 4 Variables

DF	3
# Groups	4
# Ties	2
Chi Square	8.475
P-Value	.0372
Chi Square corrected for ties	8.692
Tied P-Value	.0337

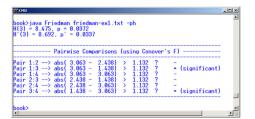


Figure: Source: Fg. 6-(37-39) (Mackenzie).

Reminders

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- Next next week, please bring your pc, and install JASP.
 We shall together do "Analysis of Variance" workshops for two weeks.

Readings For Next Week

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Nonparametric tests Mackenzie, Chapter 3, Interaction Elements, Human Computer Interaction: An Empirical Research Perspective, 1st ed. (2013)

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Questions