

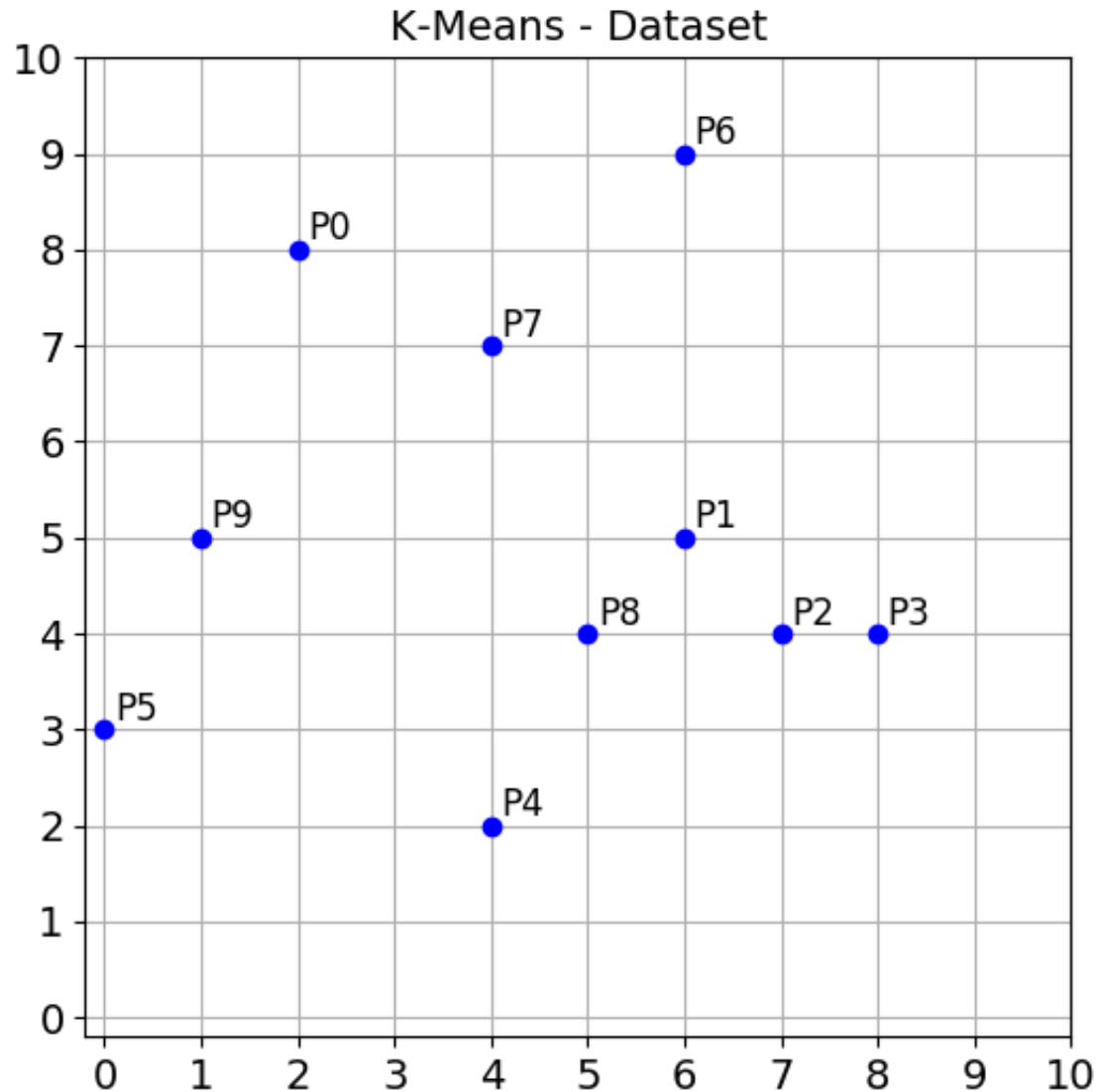
Ex. - Clustering

K-means simulation

Initial centroids:

$C1 = P2 = (7,4)$

$C2 = P8 = (5,4)$



Solution: Identify the **Bisecting** lines dividing the plane between pairs of centroids

Cluster1

P0,P7,P9,P8,P5,P4,P1,P6

Cluster2

P2,P3

Centrod1:

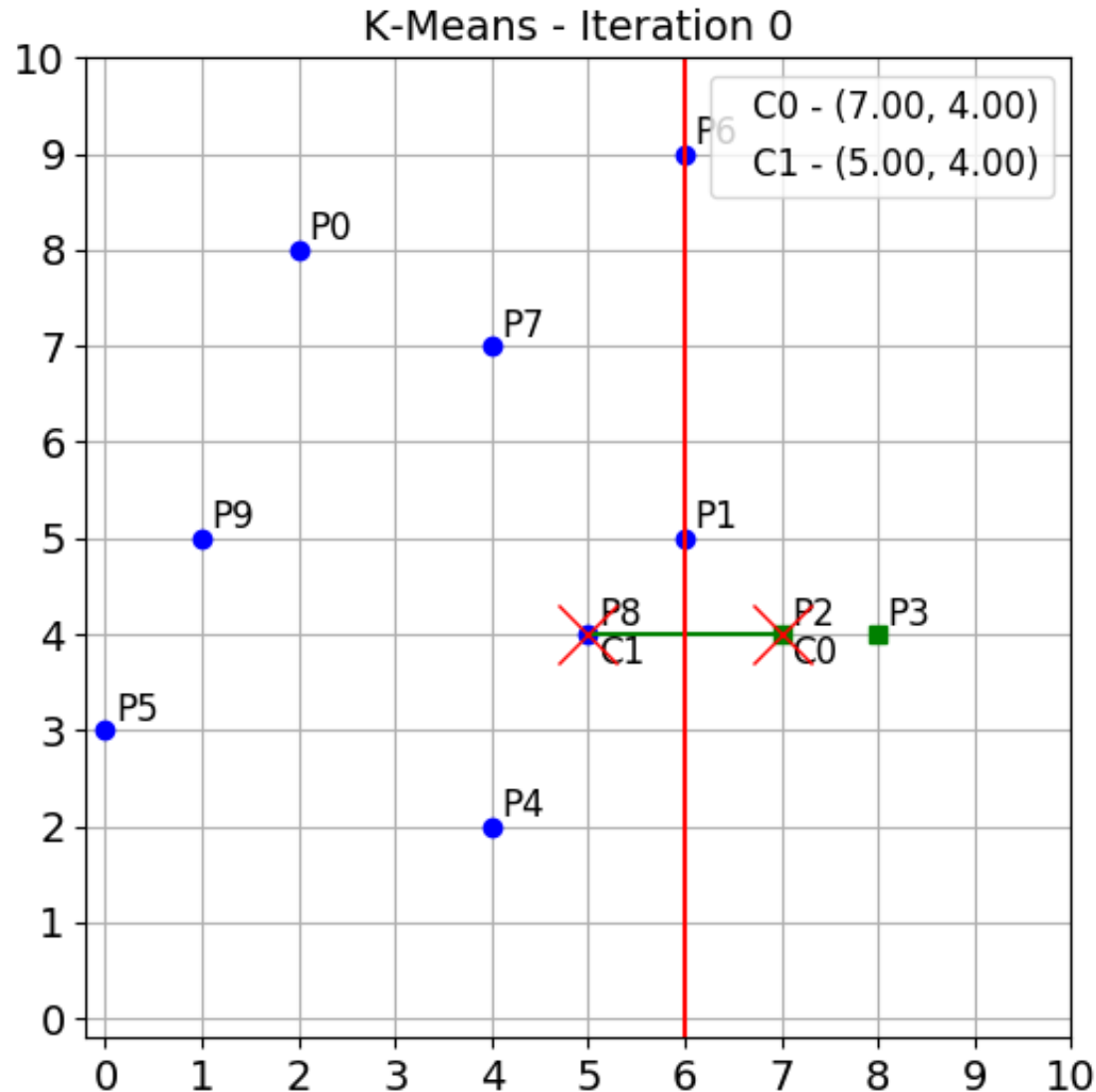
$$X1 = (0+1+2+4+4+5+6+6)/8 = 3.5$$

$$Y1 = (2+3+4+5+5+7+8+9)/8 = 5.38$$

Centrod2:

$$X2 = (7+8)/2 = 7.5$$

$$Y2 = (4+4)/2 = 4$$



Solution: Identify the **Bisecting** lines dividing the plane between pairs of centroids

Cluster1

P0,P7,P9,P8,P5,P4,P6

Cluster2

P1,P2,P3

Centrod1:

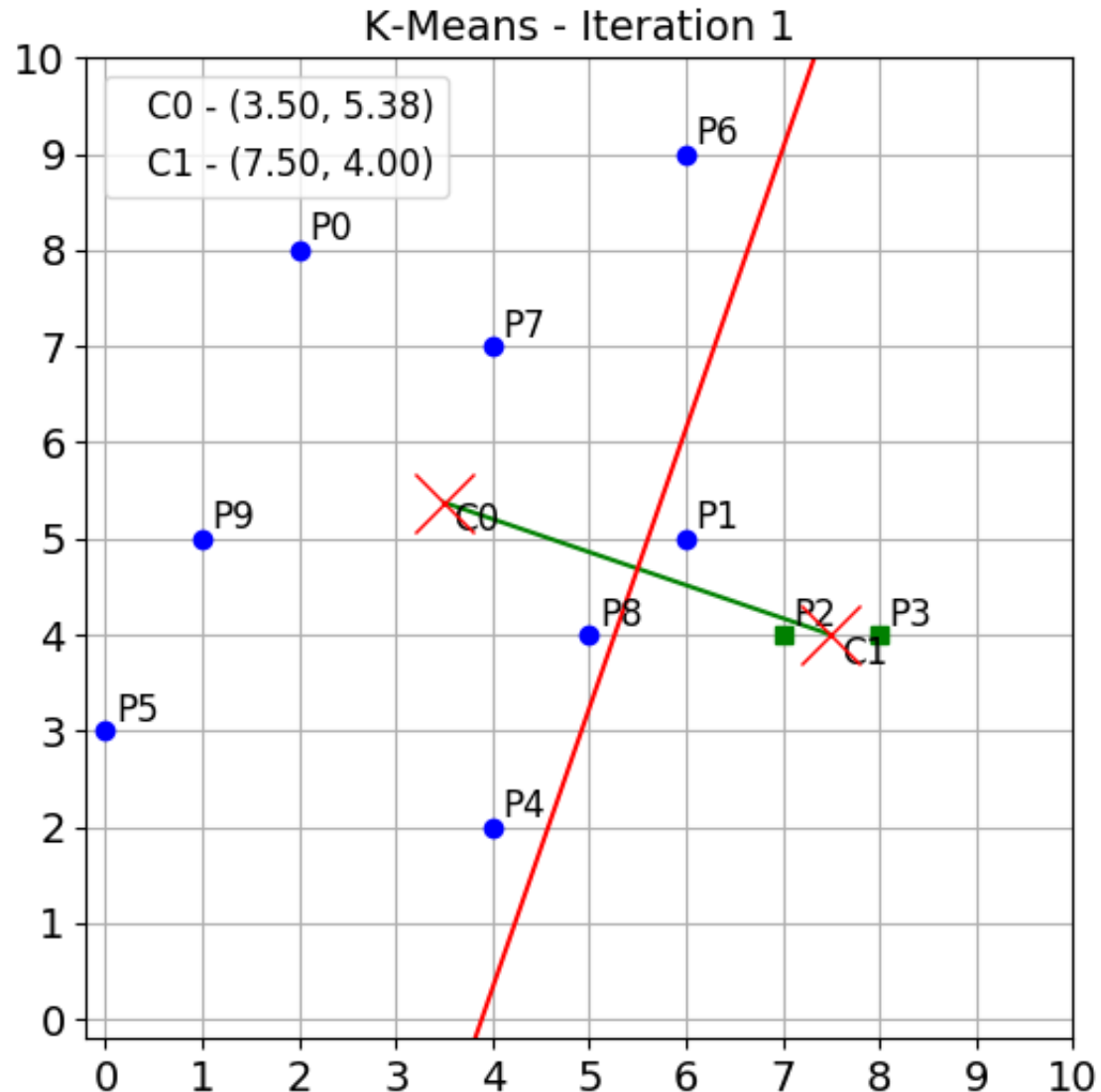
$$X1 = (0+1+2+4+4+5+6)/7 = 3.14$$

$$Y1 = (2+3+4+5+7+8+9)/7 = 5.43$$

Centrod2:

$$X2 = (6+7+8)/3 = 7$$

$$Y2 = (5+4+4)/3 = 4.33$$



Solution: Identify the **Bisecting** lines dividing the plane between pairs of centroids

Cluster1

P0,P7,P9,P5,P4,P6

Cluster2

P1,P2,P3,P8

Centrod1:

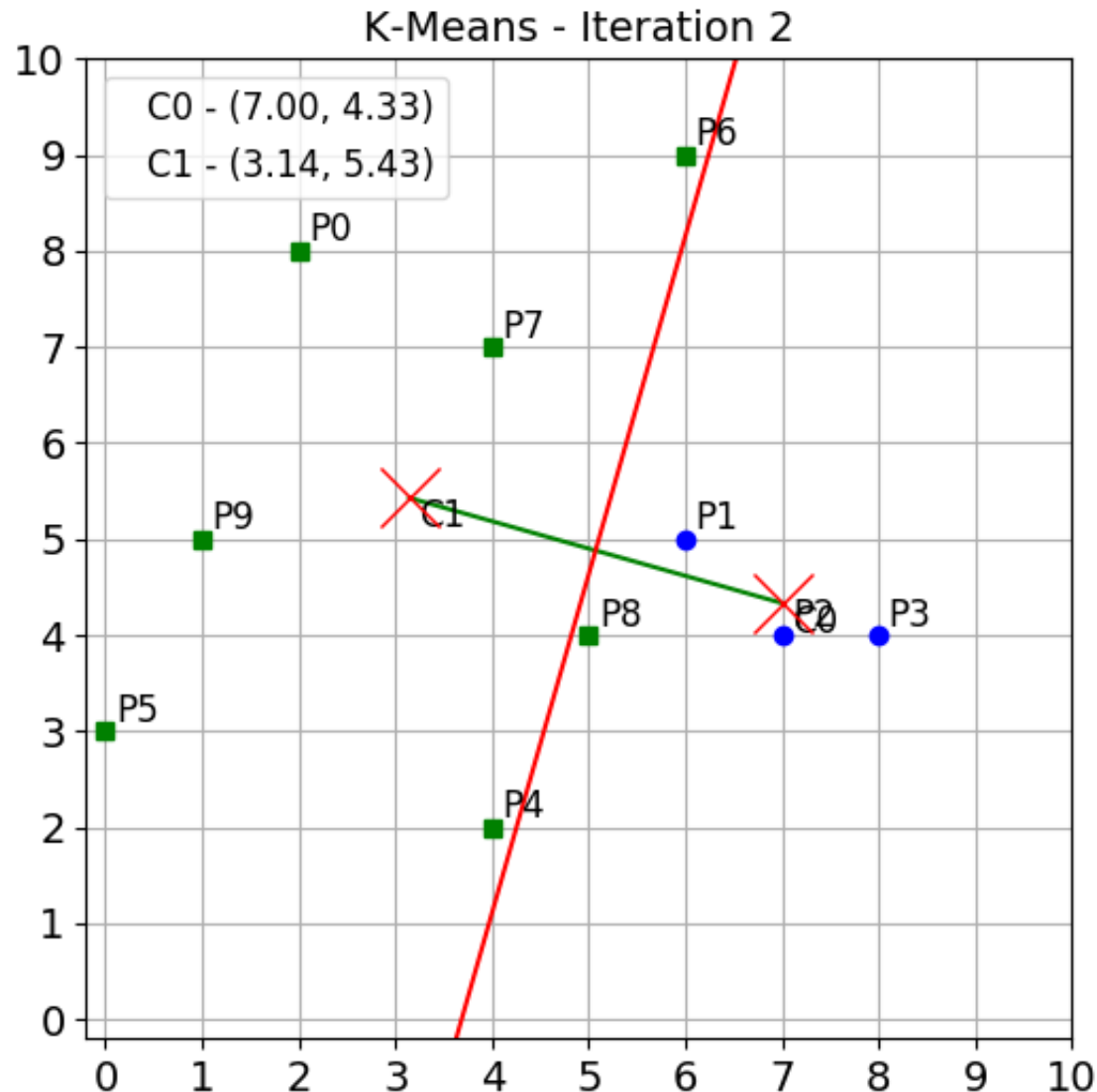
$$X1 = (0+1+2+4+4+6)/6 = 2.83$$

$$Y1 = (2+3+5+7+8+9)/6 = 5.67$$

Centrod2:

$$X2 = (6+7+8+5)/4 = 6.5$$

$$Y2 = (5+4+4+4)/4 = 4.25$$



Solution: Identify the **Bisecting** lines dividing the plane between pairs of centroids

Cluster1

P0,P7,P9,P5,P6

Cluster2

P1,P2,P3,P8,P4

Centrod1:

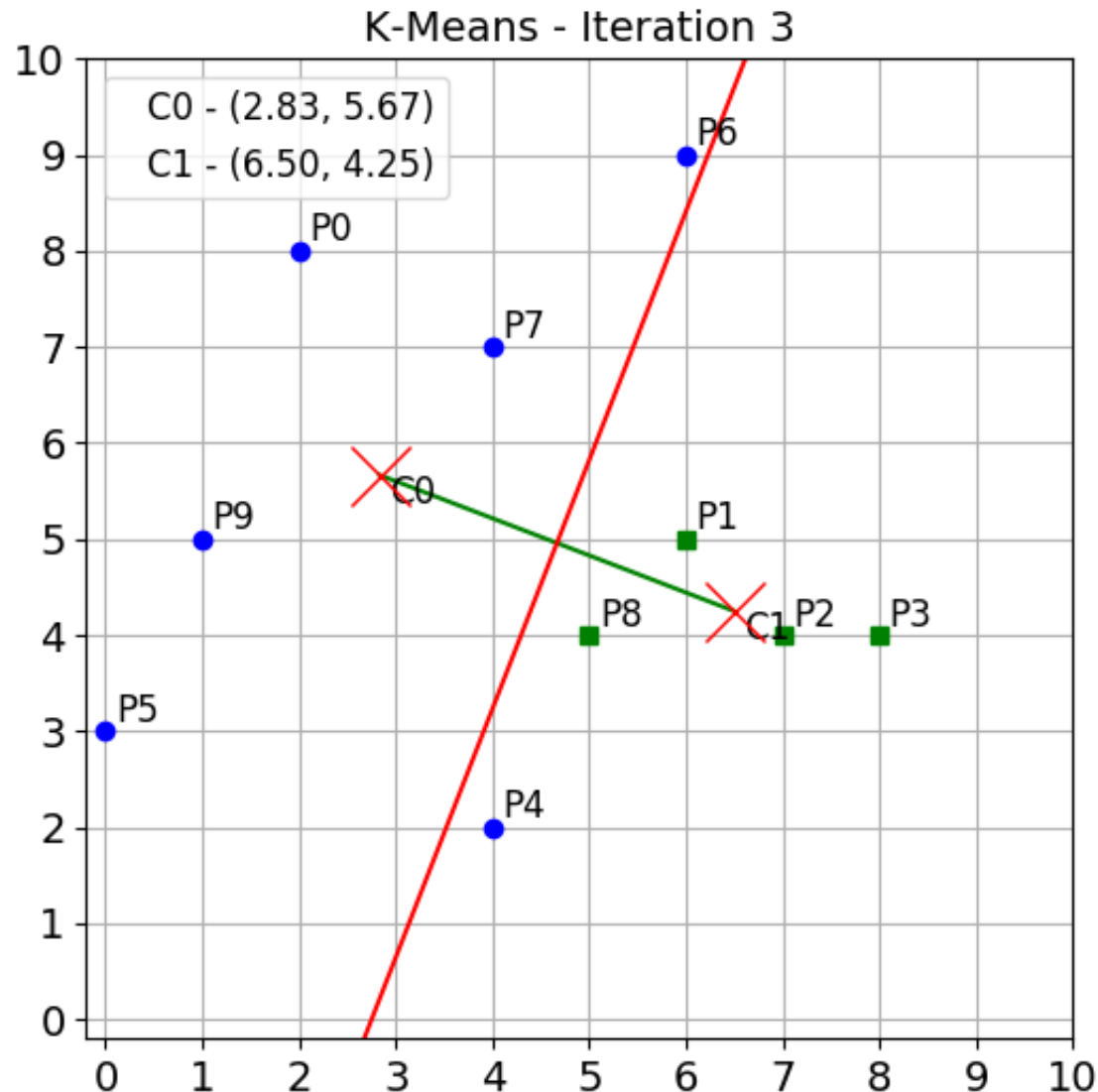
$$X1 = (0+1+2+4+6)/5 = 2.6$$

$$Y1 = (3+5+7+8+9)/5 = 6.4$$

Centrod2:

$$X2 = (6+7+8+5+4)/5 = 6$$

$$Y2 = (5+4+4+4+2)/5 = 3.8$$



Solution: Identify the **Bisecting** lines dividing the plane between pairs of centroids

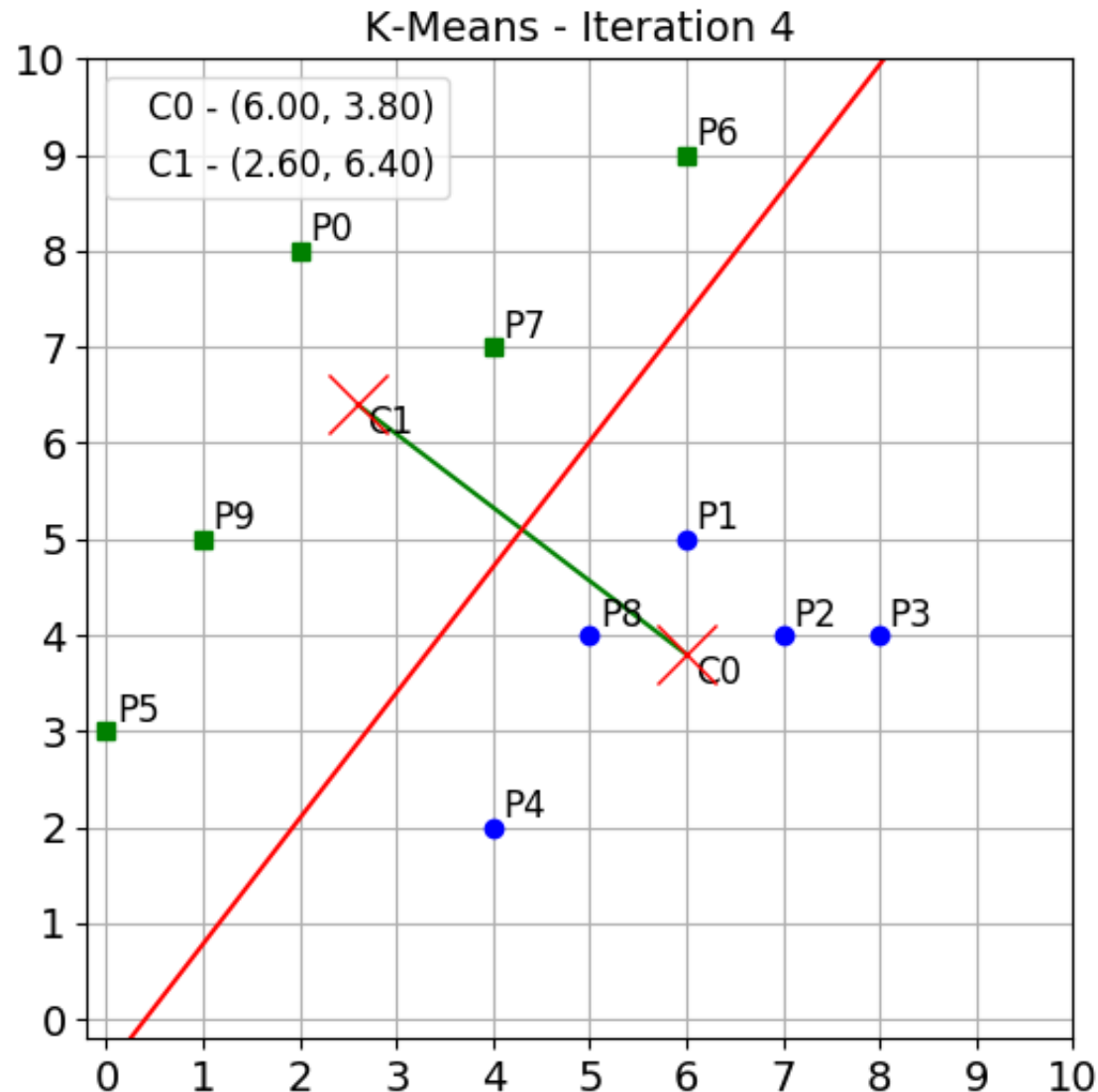
Cluster1

P0,P7,P9,P5,P6

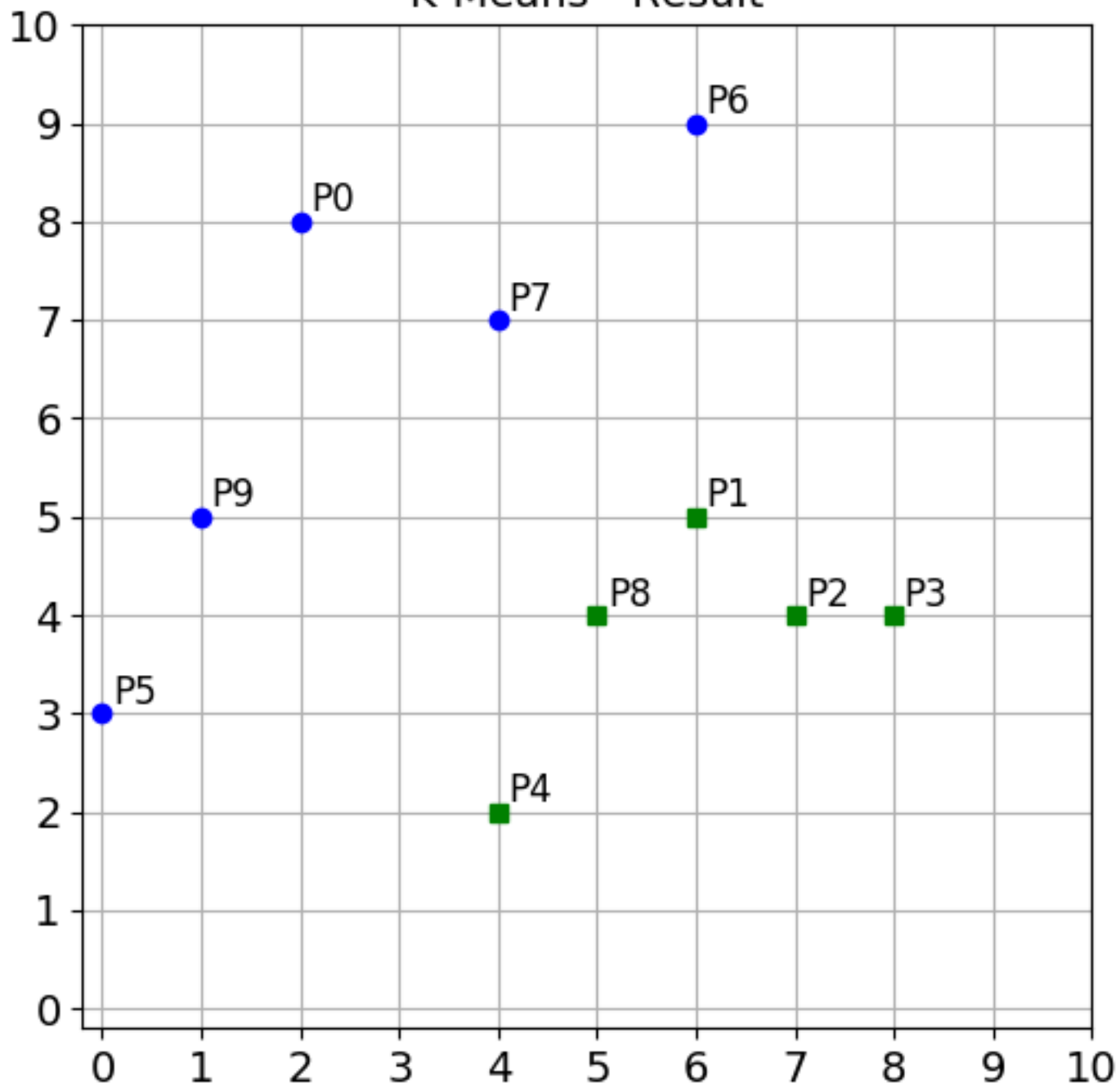
Cluster2

P1,P2,P3,P8,P4

The cluster composition does not change, so K-means stops

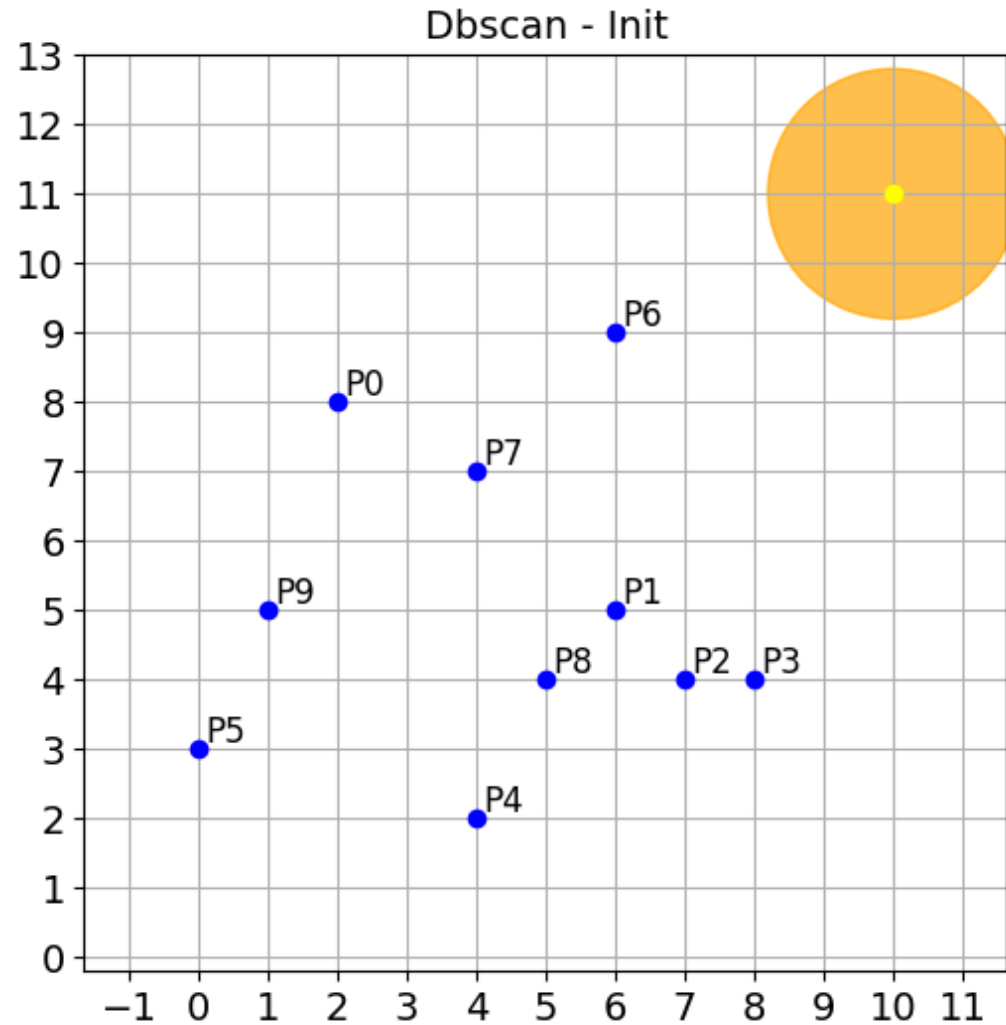


K-Means - Result



DBSCAN - Simulation

- Eps = 1.8
- MinPoints=3
 - (included the point)



DBSCAN

- Eps = 1.8
- MinPoints=3
 - (included the point)

CORE POINTS:

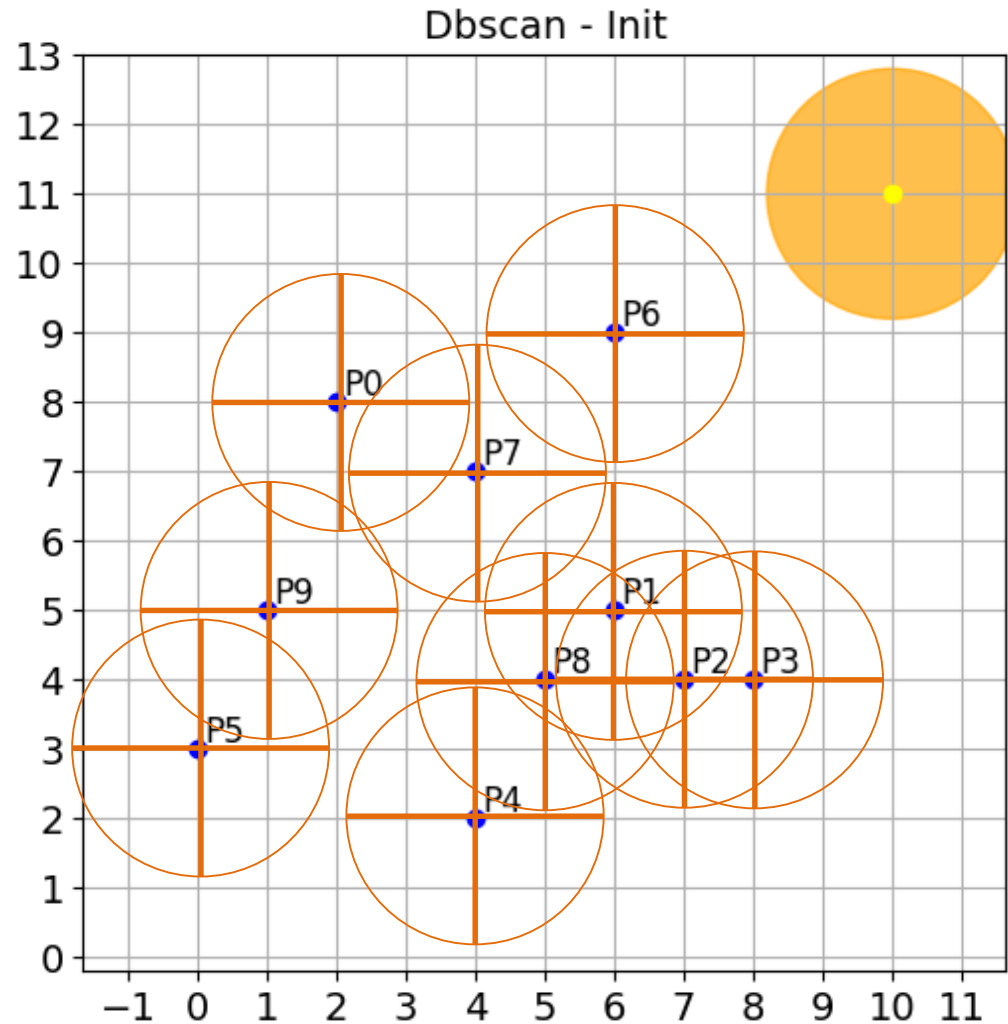
- P1
- P2

BORDER POINTS

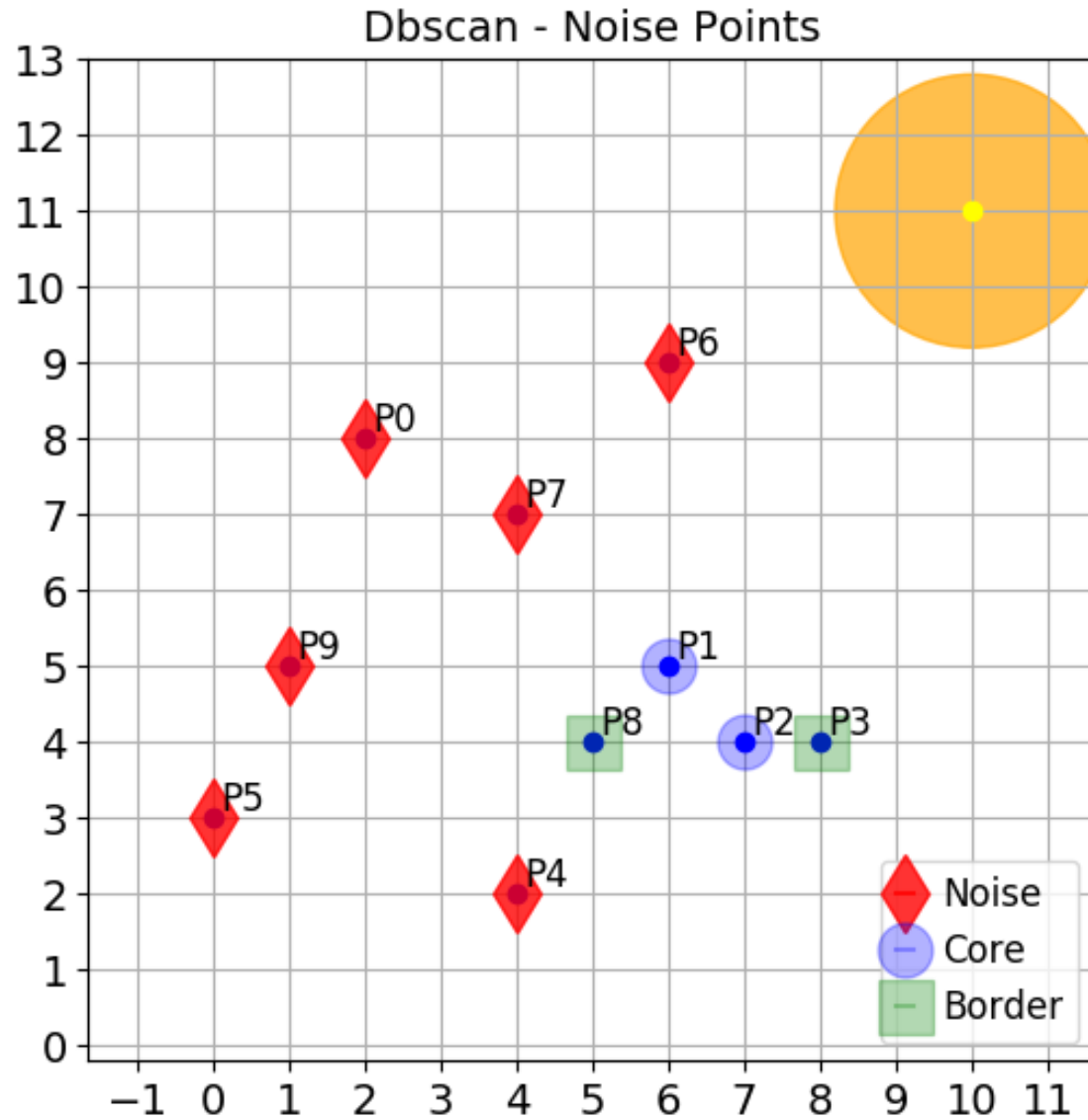
- P3
- P8

NOISE POINTS

- P4, P5, P9, P0, P6, P7

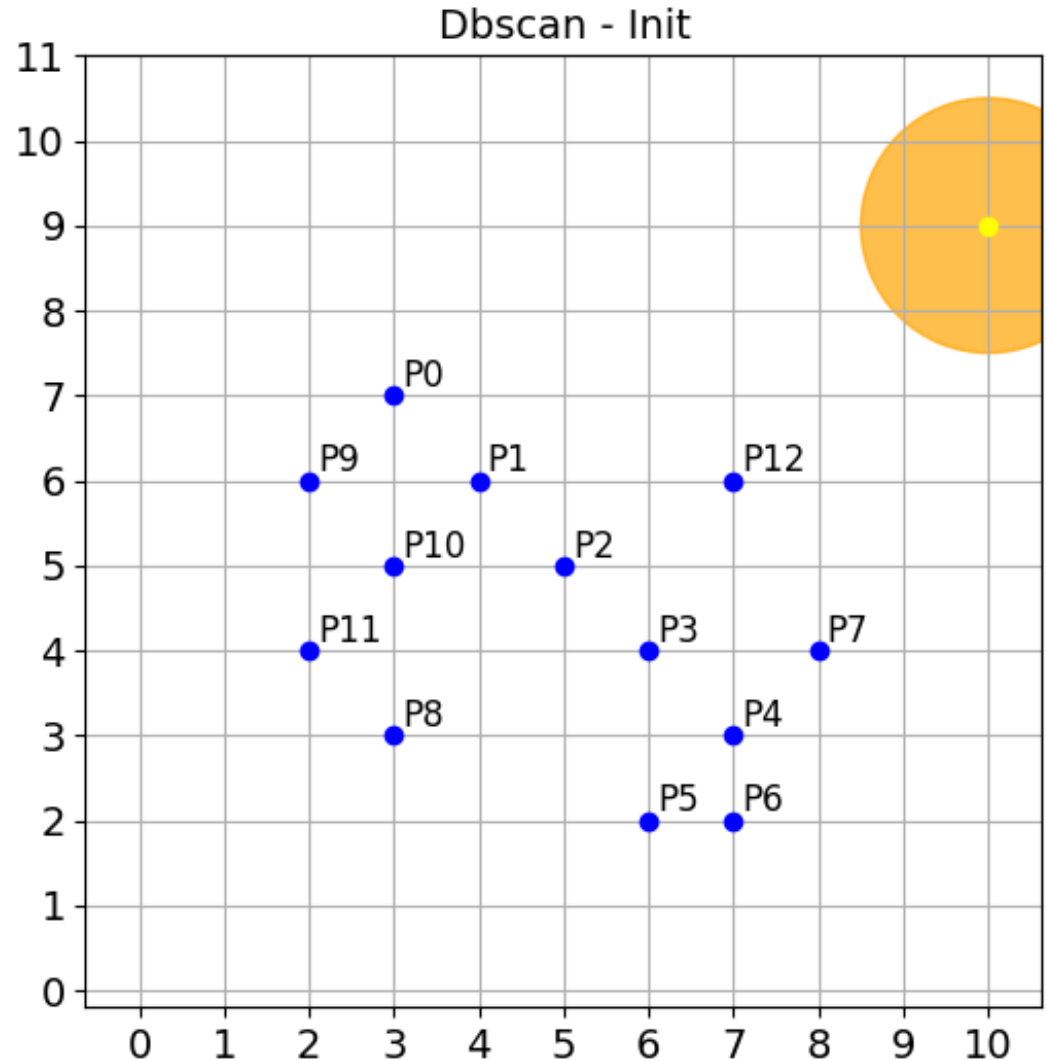


DBSCAN



DBSCAN EX. 2

- Eps = 1.5
- MinPoints=3
 - (included the point)



DBSCAN 2

- $Eps = 1.8$
- $MinPoints = 3$
 - (included the point)

CORE POINTS:

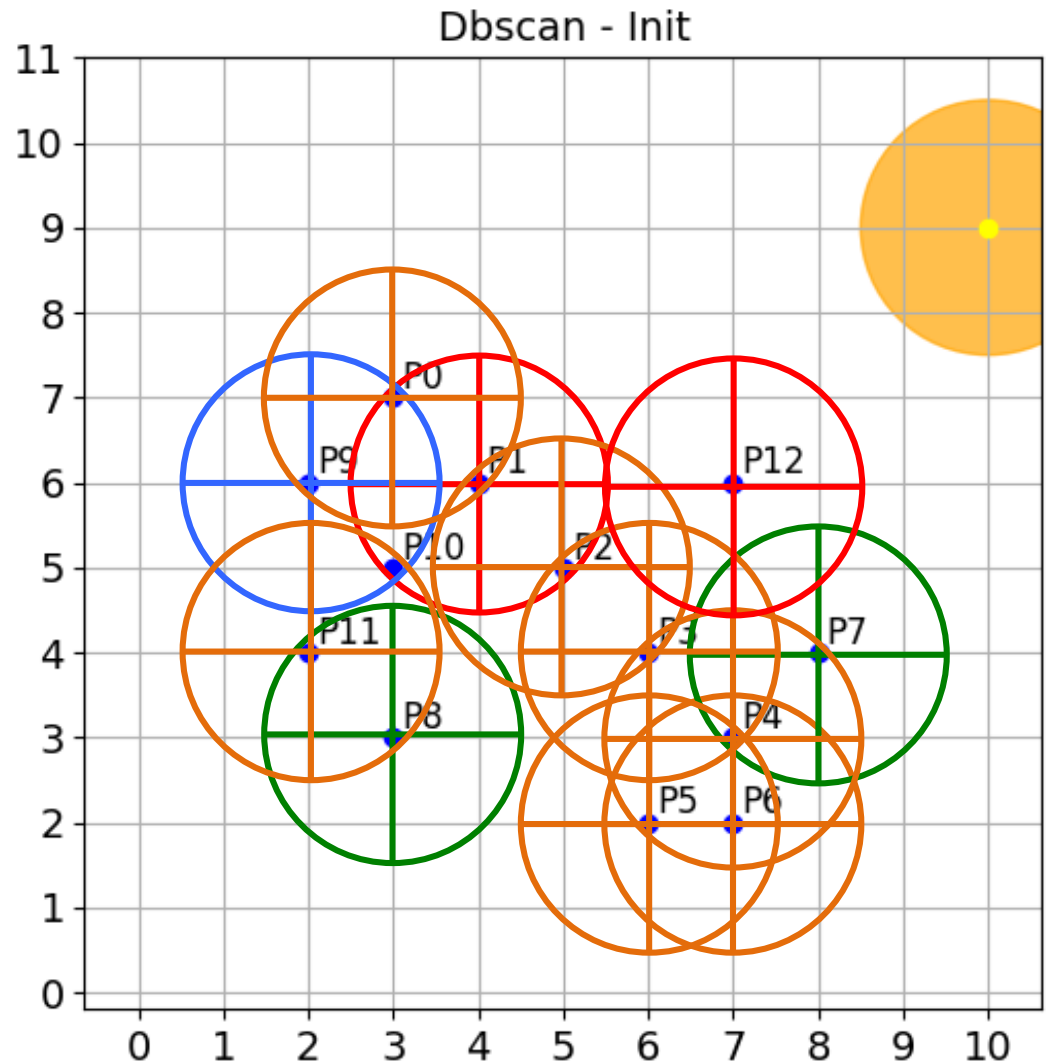
- P5
- P6
- P4
- P3
- P2
- P1
- P0
- P9
- P11

BORDER POINTS

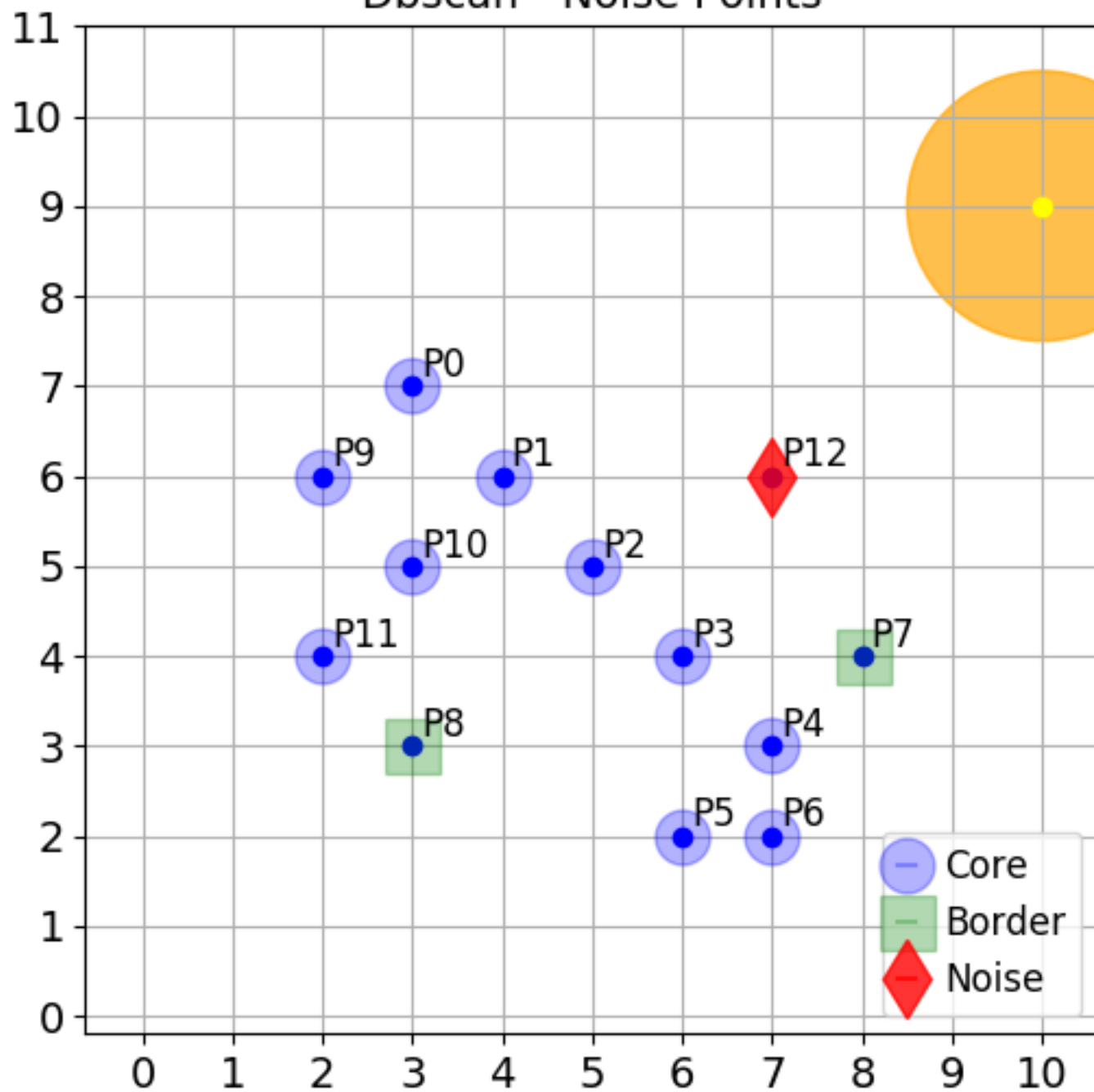
- P8
- P7

NOISE POINTS

- P12



Dbscan - Noise Points



Hierarchical

P0	X	1	Y	3
P1	X	5	Y	5
P2	X	4	Y	3
P3	X	4	Y	1
P4	X	3	Y	1
P5	X	3	Y	2

Euclidean Distance

$$\left((x_0 - x_1)^2 + (y_0 - y_1)^2 \right)^{1/2}$$

Distance Matrix

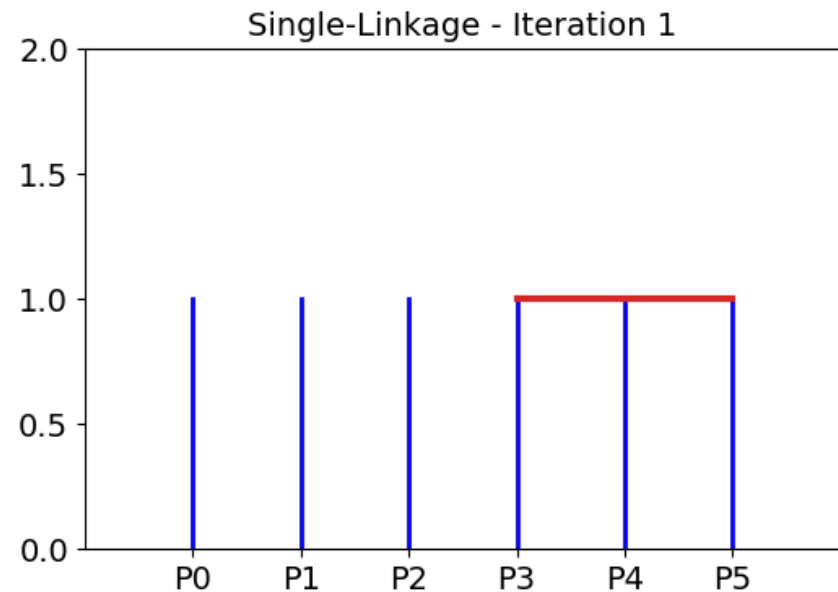
	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
P0	0.0	4.47	3.0	3.61	2.83	2.24
P1	4.47	0.0	2.24	4.12	4.47	3.61
P2	3.0	2.24	0.0	2.0	2.24	1.41
P3	3.61	4.12	2.0	0.0	1.0	1.41
P4	2.83	4.47	2.24	1.0	0.0	1.0
P5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Single-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

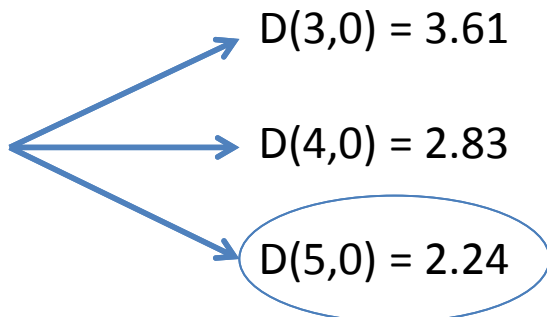
Minimum Distance



Hierarchical: Single-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	
1	4.47	0.0	2.24	
2	3.0	2.24	0.0	
(3,4,5)				0.0

$D([3,4,5], 0) =$


$D(3,0) = 3.61$
 $D(4,0) = 2.83$
 $D(5,0) = 2.24$

Min Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Single-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	2.24
1	4.47	0.0	2.24	
2	3.0	2.24	0.0	
(3,4,5)	2.24			0.0

$$D([3,4,5], 1) = \begin{cases} D(3,1) = 4.12 \\ D(4,1) = 4.47 \\ D(5,1) = 3.61 \end{cases}$$

Min Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Single-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	2.24
1	4.47	0.0	2.24	3.61
2	3.0	2.24	0.0	
(3,4,5)	2.24	3.61		0.0

$$D([3,4,5], 2) = \begin{cases} D(3,2) = 2 \\ D(4,2) = 2.24 \\ D(5,2) = 1.41 \end{cases}$$

Min Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

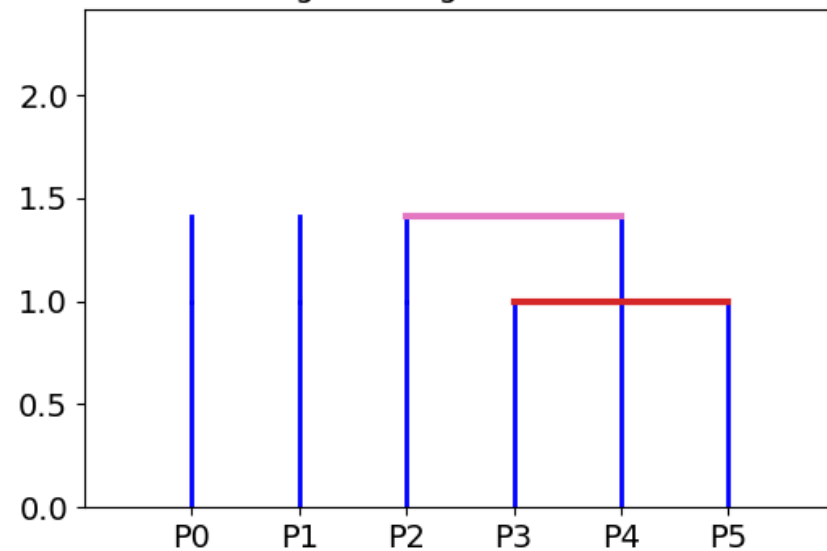
Hierarchical: Single-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	2.24
1	4.47	0.0	2.24	3.61
2	3.0	2.24	0.0	1.41
(3,4,5)	2.24	3.61	1.41	0.0

Minimum Distance

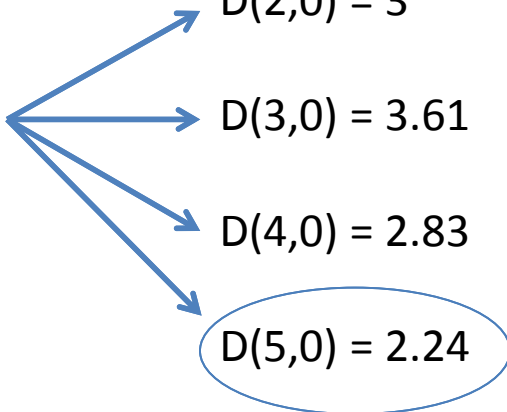
Single-Linkage - Iteration 2



Hierarchical: Single-LINK

Distance Matrix

	((0,),)	((1,),)	((2,), (3, 4, 5))
0	0.0	4.47	
1	4.47	0.0	
(2,3,4,5)			0.0

$D([2,3,4,5], 0) =$


 $D(2,0) = 3$

 $D(3,0) = 3.61$

 $D(4,0) = 2.83$

 $D(5,0) = 2.24$

Min Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Single-LINK

Distance Matrix

	((0,),)	((1,),)	((2,), (3, 4, 5))
0	0.0	4.47	2.24
1	4.47	0.0	
(2,3,4,5)	2.24		0.0

$$D([2,3,4,5], 1) = \begin{cases} D(2,1) = 2.24 \\ D(3,1) = 4.12 \\ D(4,1) = 4.47 \\ D(5,1) = 3.61 \end{cases}$$

Min Distance

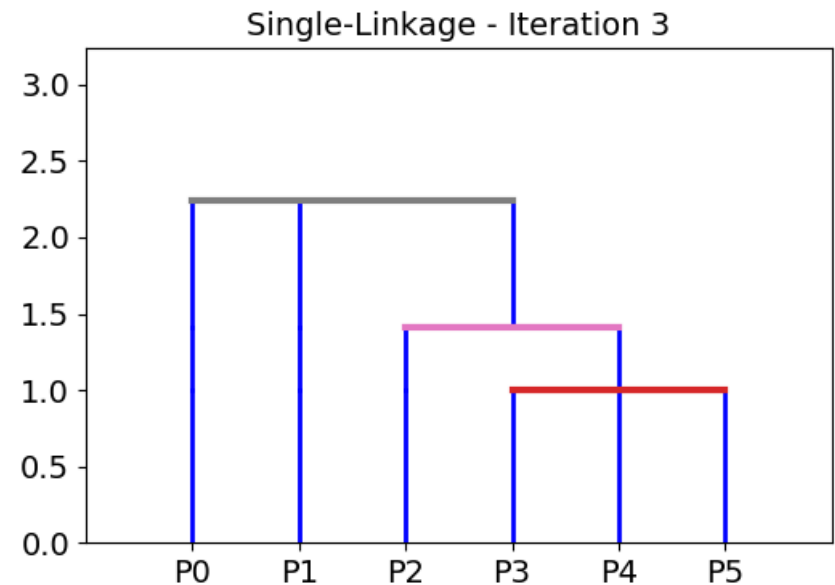
	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Single-LINK

Distance Matrix

	((0,),)	((1,),)	((2,), (3, 4, 5))
0	0.0	4.47	2.24
1	4.47	0.0	2.24
(2,3,4,5)	2.24	2.24	0.0

Minimum Distance



Hierarchical – Complete Link

P0	X	1	Y	3
P1	X	5	Y	5
P2	X	4	Y	3
P3	X	4	Y	1
P4	X	3	Y	1
P5	X	3	Y	2

Euclidean Distance

$$\left((x_0 - x_1)^2 + (y_0 - y_1)^2 \right)^{1/2}$$

Distance Matrix

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
P0	0.0	4.47	3.0	3.61	2.83	2.24
P1	4.47	0.0	2.24	4.12	4.47	3.61
P2	3.0	2.24	0.0	2.0	2.24	1.41
P3	3.61	4.12	2.0	0.0	1.0	1.41
P4	2.83	4.47	2.24	1.0	0.0	1.0
P5	2.24	3.61	1.41	1.41	1.0	0.0

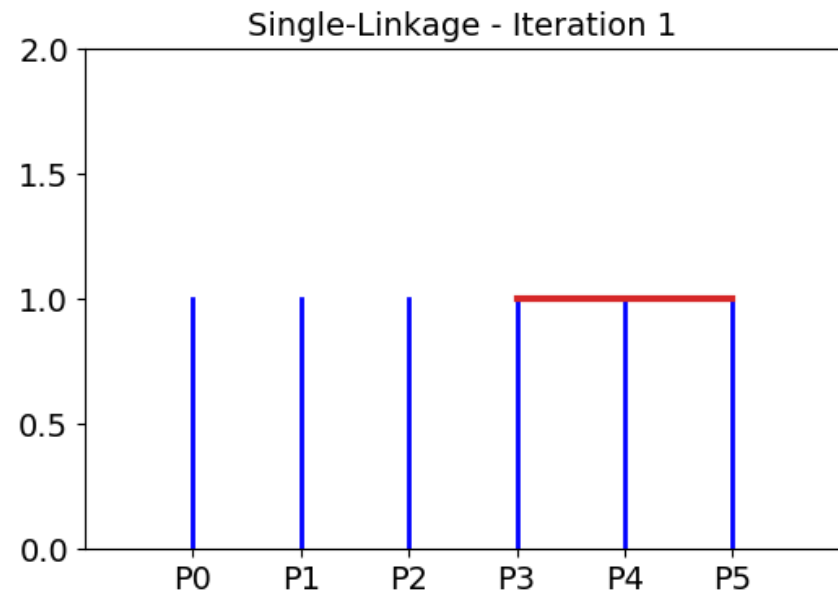
Hierarchical: Complete-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Minimum Distance

First Step **equal** to SINGLE LINK



Hierarchical: Complete-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	
1	4.47	0.0	2.24	
2	3.0	2.24	0.0	
(3,4,5)				0.0

$$D([3,4,5], 0) = \begin{cases} D(3,0) = 3.61 \\ D(4,0) = 2.83 \\ D(5,0) = 2.24 \end{cases}$$

Max Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Complete-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	3.61
1	4.47	0.0	2.24	
2	3.0	2.24	0.0	
(3,4,5)	3.61			0.0

$$D([3,4,5], 1) = \begin{cases} D(3,1) = 4.12 \\ D(4,1) = 4.47 \\ D(5,1) = 3.61 \end{cases}$$

Max Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Complete-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	3.61
1	4.47	0.0	2.24	
2	3.0	2.24	0.0	
(3,4,5)	3.61	4.47		0.0

$$D([3,4,5], 2) = \begin{cases} D(3,2) = 2 \\ D(4,2) = 2.24 \\ D(5,2) = 1.41 \end{cases}$$

Max Distance

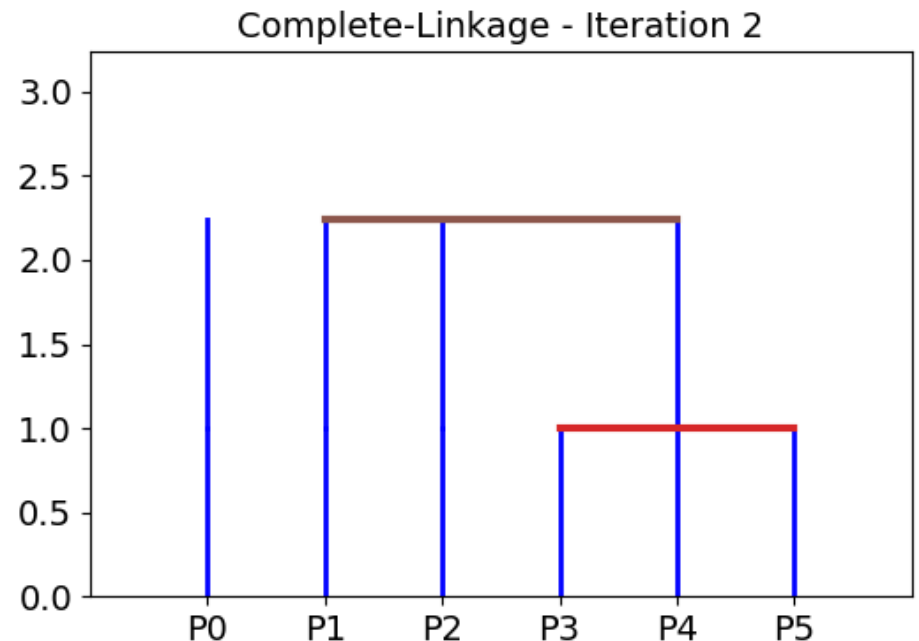
	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Complete-LINK

Distance Matrix

	(0,)	(1,)	(2,)	(3, 4, 5)
0	0.0	4.47	3.0	3.61
1	4.47	0.0	2.24	4.47
2	3.0	2.24	0.0	2.24
(3,4,5)	3.61	4.47	2.24	0.0

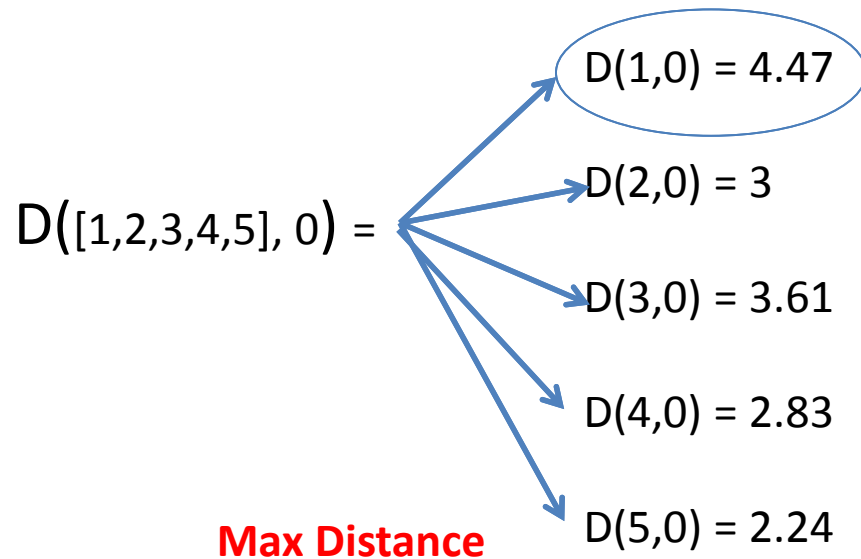
Minimum Distance



Hierarchical: Complete-LINK

Distance Matrix

	((0,))	((1,), (2,), (3, 4, 5))
0	0.0	
(1,2,3,4,5)		0.0

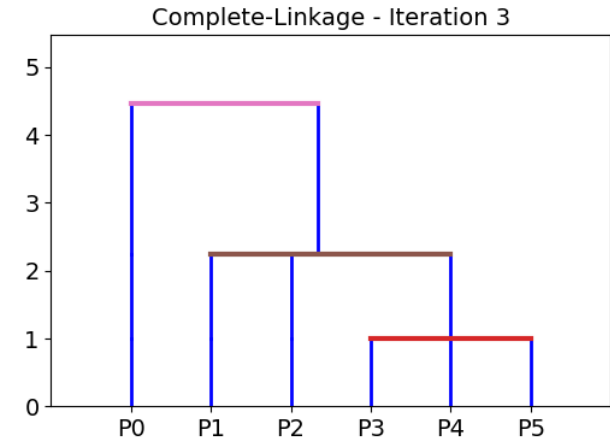


	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0

Hierarchical: Complete-LINK

Distance Matrix

	((0,))	((1,), (2,), (3, 4, 5))
0	0.0	4.47
(1,2,3,4,5)	4.47	0.0



$$D([1,2,3,4,5], 0) = \begin{cases} D(1,0) = 4.47 \\ D(2,0) = 3 \\ D(3,0) = 3.61 \\ D(4,0) = 2.83 \\ D(5,0) = 2.24 \end{cases}$$

Max Distance

	(0,)	(1,)	(2,)	(3,)	(4,)	(5,)
0	0.0	4.47	3.0	3.61	2.83	2.24
1	4.47	0.0	2.24	4.12	4.47	3.61
2	3.0	2.24	0.0	2.0	2.24	1.41
3	3.61	4.12	2.0	0.0	1.0	1.41
4	2.83	4.47	2.24	1.0	0.0	1.0
5	2.24	3.61	1.41	1.41	1.0	0.0