Data Science Toolbox Question Sheet

08.1 Algorithms

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Block 8

1. Why do we distinguish between average case and worst case in algorithmic complexity? Describe (with reasons) a situation in which each would be appropriate.
2. What is the name for an algorithm satisfying $x \in \mathcal{X} \rightarrow u \in \mathcal{U}\,[0, r)$?
3. Consider that we are working with a hash function. Under which circumstances would it be useful to consider a) predictability, b) locality, c) collisions, d) compute, and e) families of hash functions?
4. What is a hash table?
5. The error rate of a bloom filter is $(1 - \exp(-kn/r))^k$. Given fixed n and r, differentiate this with respect to k. Show that the error rate is minimised when $k = (r/n)\ln(2)$.
6. Explain what Jaccard Similarity means. Why is this slow to compute naively when the feature space is large, and how does hashing help?
7. is $f(n) = 4n\log(3n) \in \mathcal{O}(n^2)$?
8. is $2n + 5 \in \Theta(n^2)$?
9. Consider the following pseudo-code. What is its time complexity as a function of `a`?

```
input a
algorithm:
    b=0
    while a>1
        a=a/2
        b=b+1
    end
    return b
```