

# Announcements

- Homework 5 Deadline **extended to Friday (March 28, 11:59pm)**.
- No TA hours tomorrow, normal TA hours resume next week.
- Your Full Proposal + Lit Review are due April 4<sup>th</sup>!

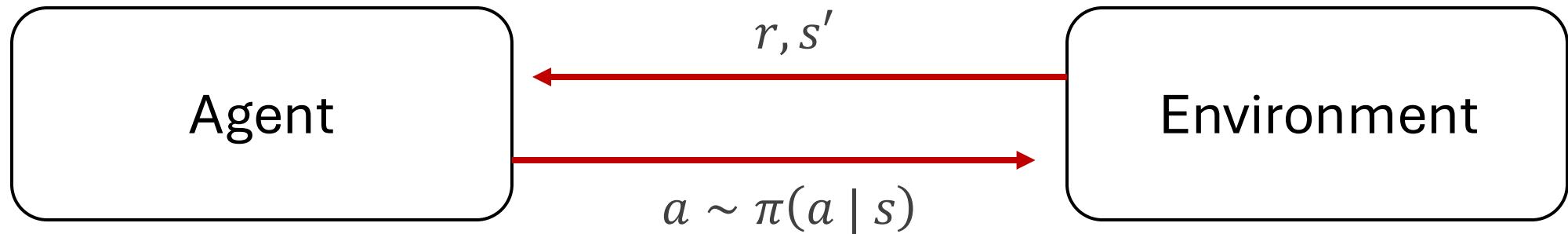


# Multi-Agent Reinforcement Learning

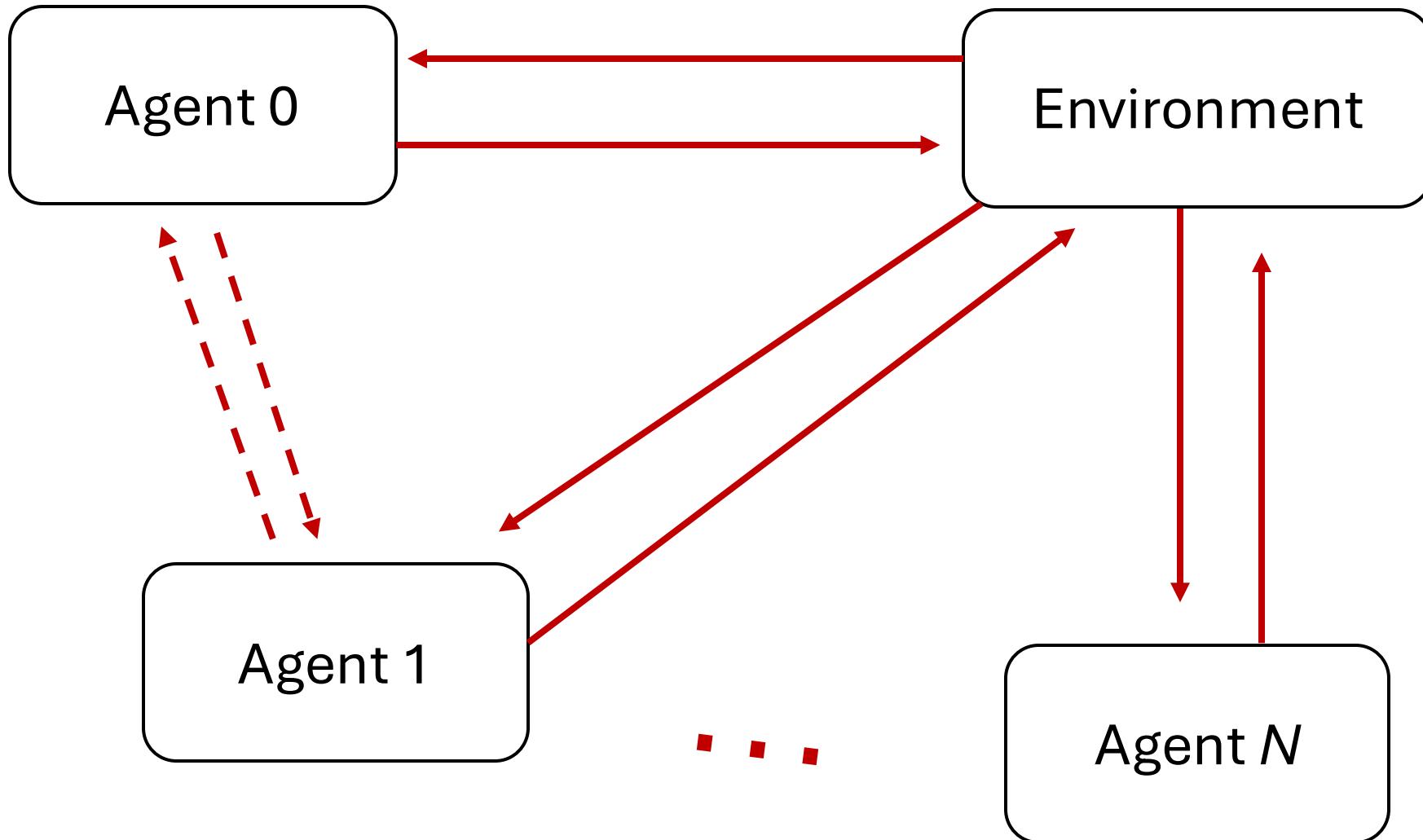
*Guest Lecturer: Connor Mattson*

# What are Multi-Agent Systems?

Recall our simple single-agent interaction loop!

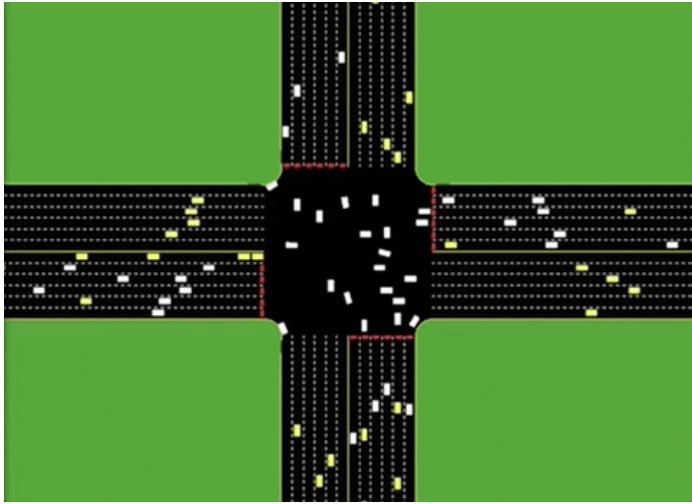


# What are Multi-Agent Systems?



**What information is being passed along the red arrows?**

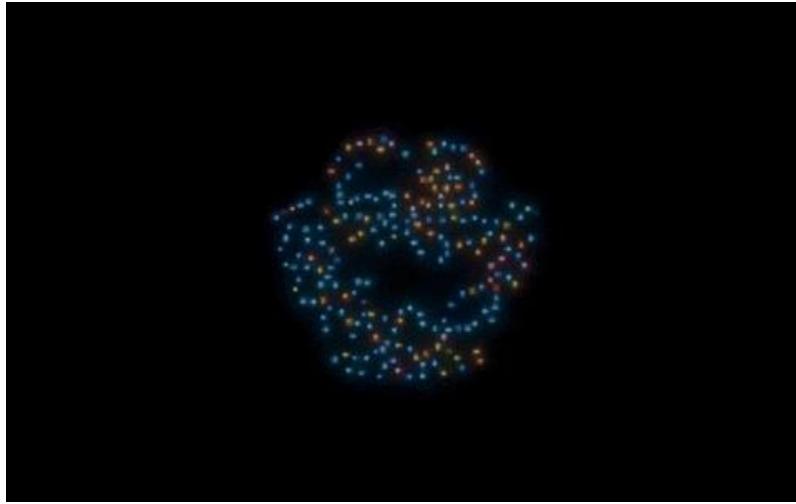
# Examples of Multi-Agent Applications



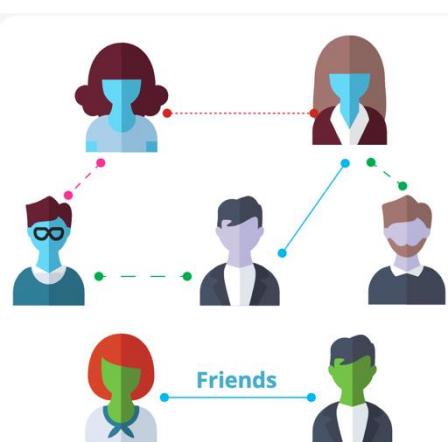
Autonomous Driving  
+ Traffic Control



n-Player Games



UAVs + Drones



Psychology + Sociology



Coordinated Robot Motion



Human Multi-Robot Interaction

# Amazon Robotics

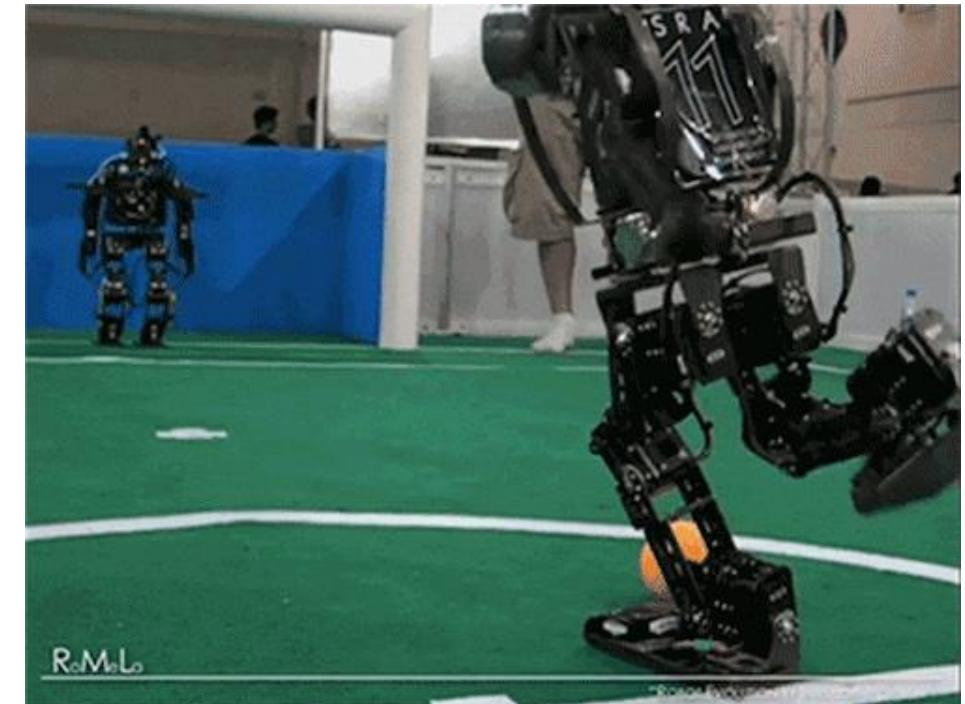


# Why Study Multi-Agent Systems?

Some of humanities greatest feats are multi-agent problems!



Robots/Agents should also possess these capabilities!

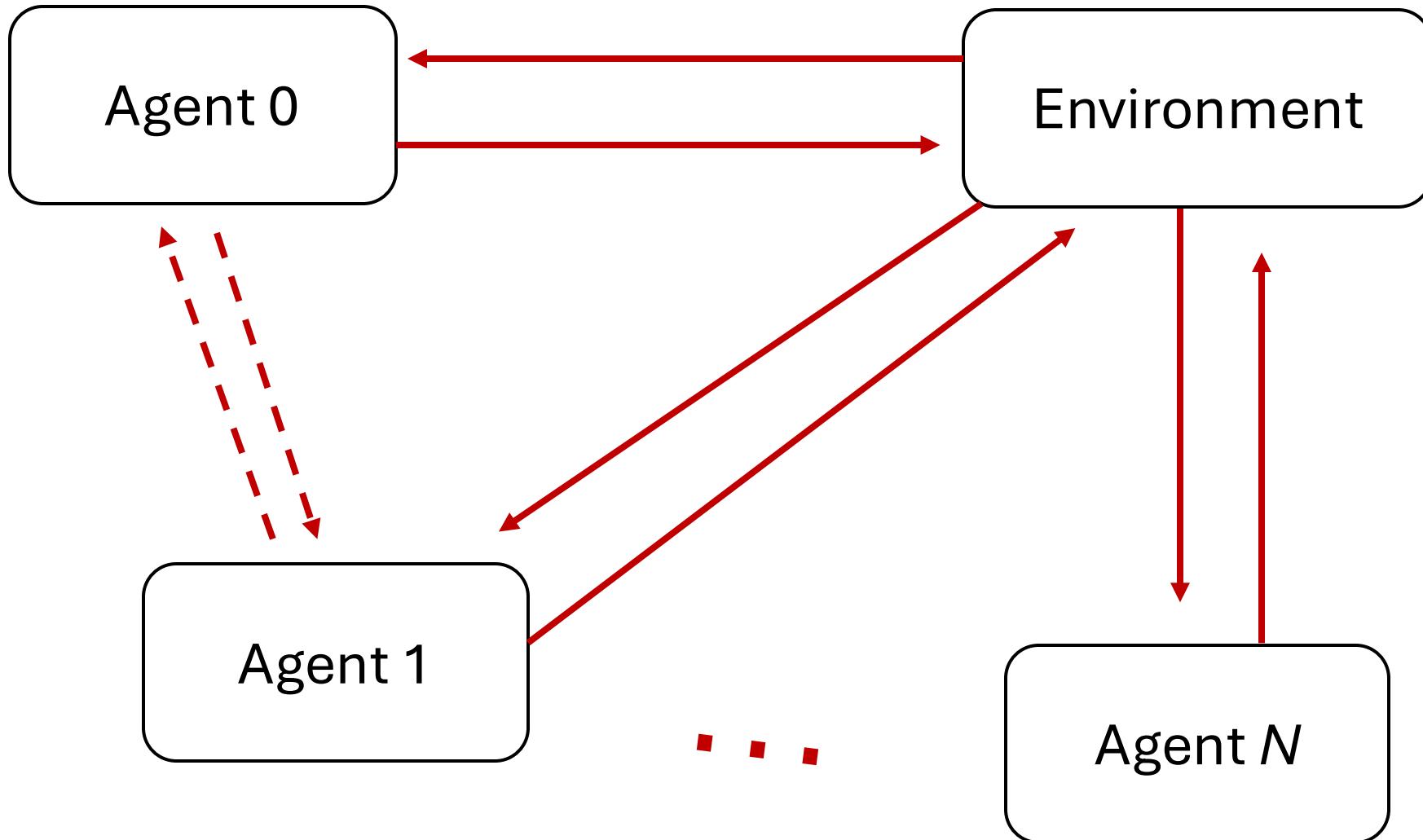


*Examples:*

Team Sports, Government, International Relations, Academic Research, Game Theory, Resource Allocation, etc.

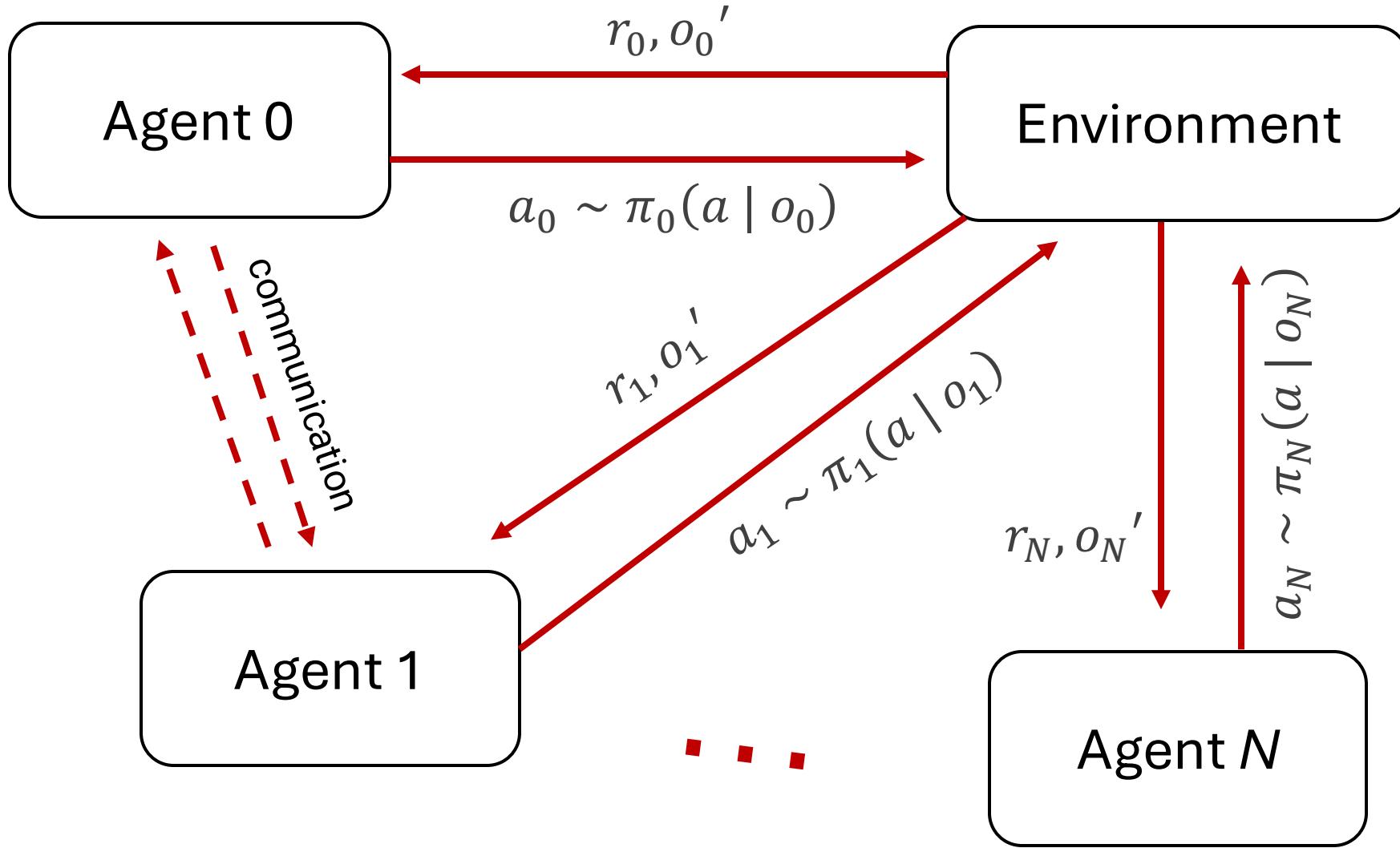
(we have a long way to go!)

# What are Multi-Agent Systems?



**What information is being passed along the red arrows?**

# What are Multi-Agent Systems?



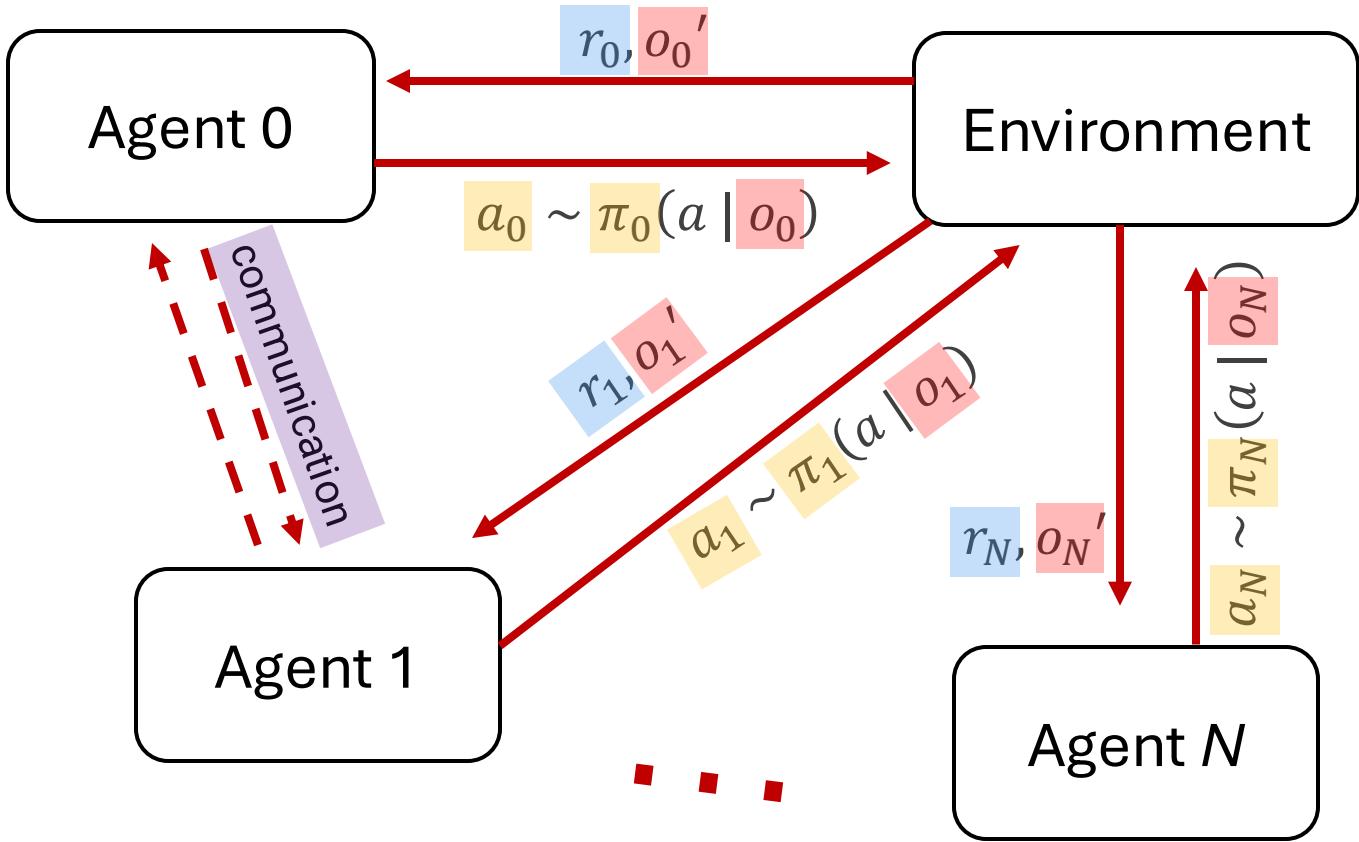
**What do you notice?**

Rewards?

Actions/Policies?

State/Observations?

# How does MARL differ from single-agent RL?



**Separate State Signals:** Agent 0 and Agent 1 receive  $o_0'$  and  $o_1'$ , respectively.

**Separate Reward Signals:** Agent 0 and Agent 1 receive  $r_0$  and  $r_1$ , respectively.

**Separate Policies:**  $\pi_i$  can be different for each agent (so  $a_i$  are different!)

**Communication:** Agents can communicate with each other (if allowed)

# Parallels to Single-Agent RL

**Same Desired Outcome:** Policies that maximize an expected return.

**Assumptions:** We don't know transition dynamics but have reward signals.

**Same Definitions of Value:** We can model/approximate  $V(s)$  and  $Q(s, a)$ .

# MARL is often the expansion of Single-Agent RL to trickier problems!

Single-Agent Learning	Multi-Agent Learning	Single-Agent Learning	Multi-Agent Learning	Single-Agent Learning	Multi-Agent Learning
Behavioral Cloning	<a href="#">Imitation-MA (2007)</a> <a href="#">Coord-MAIL (2017)</a>	Q-Learning	<a href="#">IQL (1993)</a>	TD3	<a href="#">MA-TD3 (2020)</a>
Advanced Behavioral Cloning	<a href="#">GMA-BC (2018)</a>	DQN	<a href="#">MA-DQL (2015)</a> <a href="#">VDN (2017)</a> <a href="#">QMIX (2018)</a>	Model-Based RL	<a href="#">MB-MARL (2022)</a>
Multi-Armed Bandits	<a href="#">Game Theory (Normal-Form Games)</a>	Policy-Gradient (REINFORCE)	<a href="#">Multi-Agent PG (2020)</a>	Offline RL	<a href="#">MARL-IGL (2023)</a>
Markov Decision Processes	<a href="#">Game Theory (Markov Games)</a>	A2C/A3C	<a href="#">SEAC (2020)</a>	RLHF	<a href="#">MARLHF (2024)</a>
Exact Solutions for MDPs	<a href="#">MARL-Textbook</a>	PPO	<a href="#">MAPPO (2022)</a>	Inverse RL	<a href="#">MAIRL (2021)</a>
Value-Based RL	<a href="#">MARL-Textbook</a>	SAC	<a href="#">Dec-SAC (2021)</a>	LLM Agents	<a href="#">Generative Agents (2023)</a>
TD Learning	<a href="#">MARL-Textbook</a>	DDPG	<a href="#">MADDPG (2020)</a>	...	...

We could spend an **entire semester** talking about MARL! See NYU's [TR GY 8103](#).

Single Agent  
Reinforcement  
Learning

Multi-Agent  
Reinforcement  
Learning

Game Theory



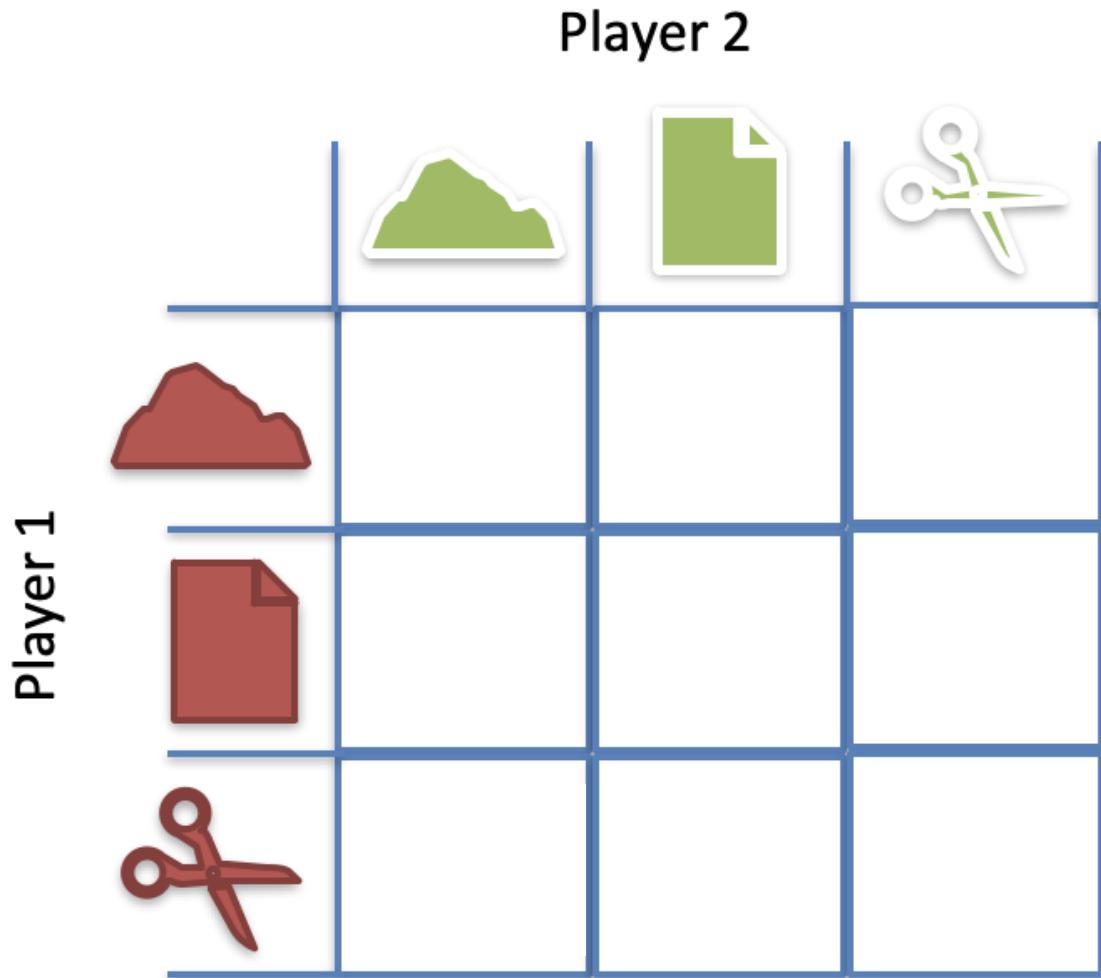
# Normal-Form Games (Bandits++)

**Definition 2 (Normal-form game)** A *normal-form game* consists of:

- *Finite set of agents*  $I = \{1, \dots, n\}$
- *For each agent*  $i \in I$ :
  - *Finite set of actions*  $A_i$
  - *Reward function*  $\mathcal{R}_i : A \rightarrow \mathbb{R}$ , where  $A = A_1 \times \dots \times A_n$

# Most Popular Normal-Form Game: Rock, Paper, Scissors!

- A single-shot, simultaneous, full-information game
- **Single shot:** Played once
- **Simultaneous:** Both actions are revealed at once
- **Full-information:** Everything about the game is known (in this case, the costs / rewards)



# Most Popular Normal-Form Game: Rock, Paper, Scissors!

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- **Single shot:** Played once
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		Player 2		
		Rock	Paper	Scissors
				
		(0,0)	(-1,1)	(1,-1)
Player 1			(1,-1)	(0,0)
		(-1,1)	(0,0)	(-1,1)
			(1,-1)	(0,0)

# Normal-Form Games (Bandits++)

	R	P	S
R	0,0	-1,1	1,-1
P	1,-1	0,0	-1,1
S	-1,1	1,-1	0,0

(a) Rock-Paper-Scissors

	A	B
A	10	0
B	0	10

(b) Coordination Game

	C	D
C	-1,-1	-5,0
D	0,-5	-3,-3

(c) Prisoner's Dilemma

Zero-Sum Game

Common Reward

Mixed Reward

We won't go over the various ways to solve NFGs from evaluative feedback, but this is a well studied area of game theory!

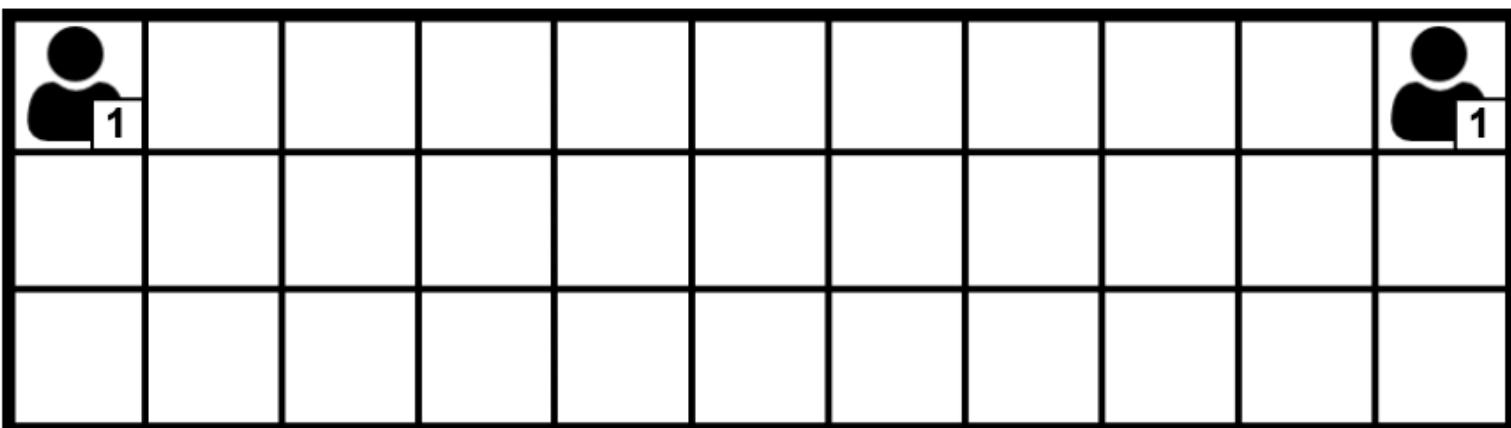
# Markov Games (MDPs++)

**Definition 3 (Stochastic game)** A stochastic game consists of:

- Finite set of agents  $I = \{1, \dots, n\}$
- Finite set of states  $S$ , with subset of terminal states  $\bar{S} \subset S$
- For each agent  $i \in I$ :
  - Finite set of actions  $A_i$
  - Reward function  $\mathcal{R}_i : S \times A \times S \rightarrow \mathbb{R}$ , where  $A = A_1 \times \dots \times A_n$
- State transition probability function  $\mathcal{T} : S \times A \times S \rightarrow [0, 1]$  such that

$$\forall s \in S, a \in A : \sum_{s' \in S} \mathcal{T}(s, a, s') = 1 \quad (3.1)$$

# Markov Games (MDPs++)



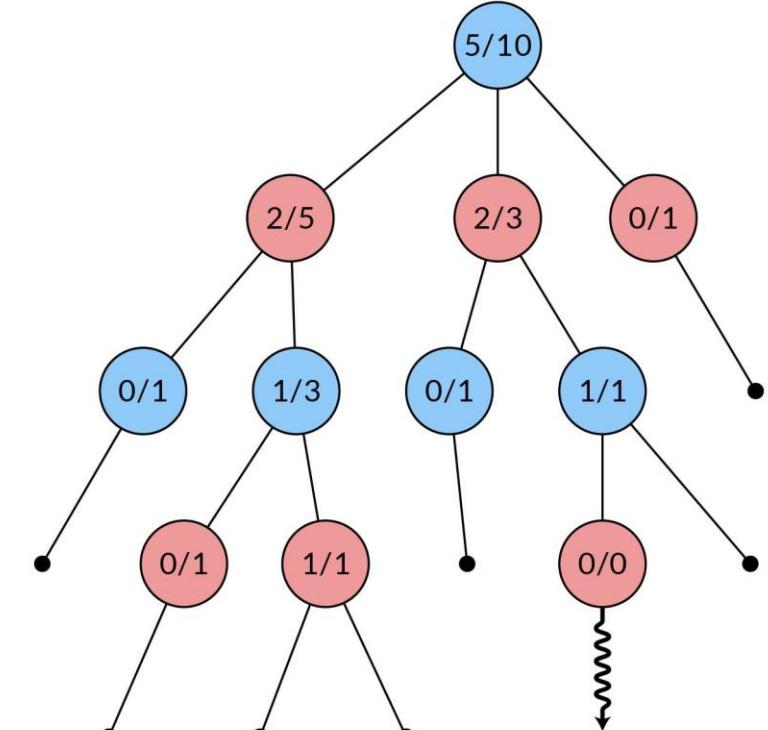
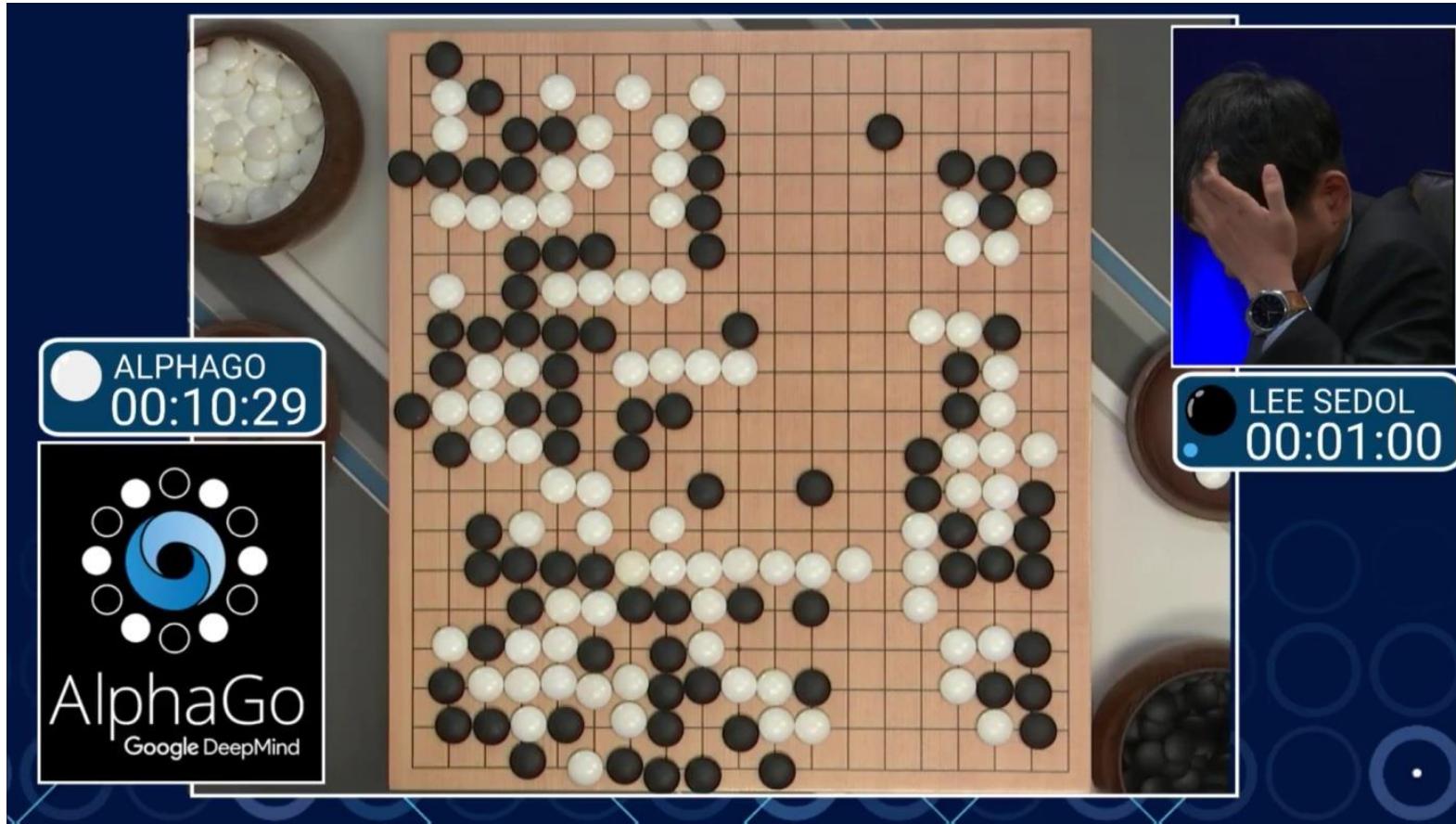
Each agent has four actions:  
{UP, LEFT, DOWN, RIGHT}

A step forward in the game is  
a **joint action**

$$a \in A = A_0 \times A_1 \times \cdots \times A_N$$

- **Sequential Decision Making:** state changes over time (could be finite or infinite horizon).
- **Simultaneous:** Both agents take actions at the same time.
- **System Dynamics:** The actions of both agents (joint action) determine the subsequent state.

# Competition (2-player games)



We already talked about strategies for learning turn-based 2-player games when we covered AlphaGo and AlphaZero!

# Cooperation!

For today, let's focus on the *collaborative* case.

All agents still have independent reward signals

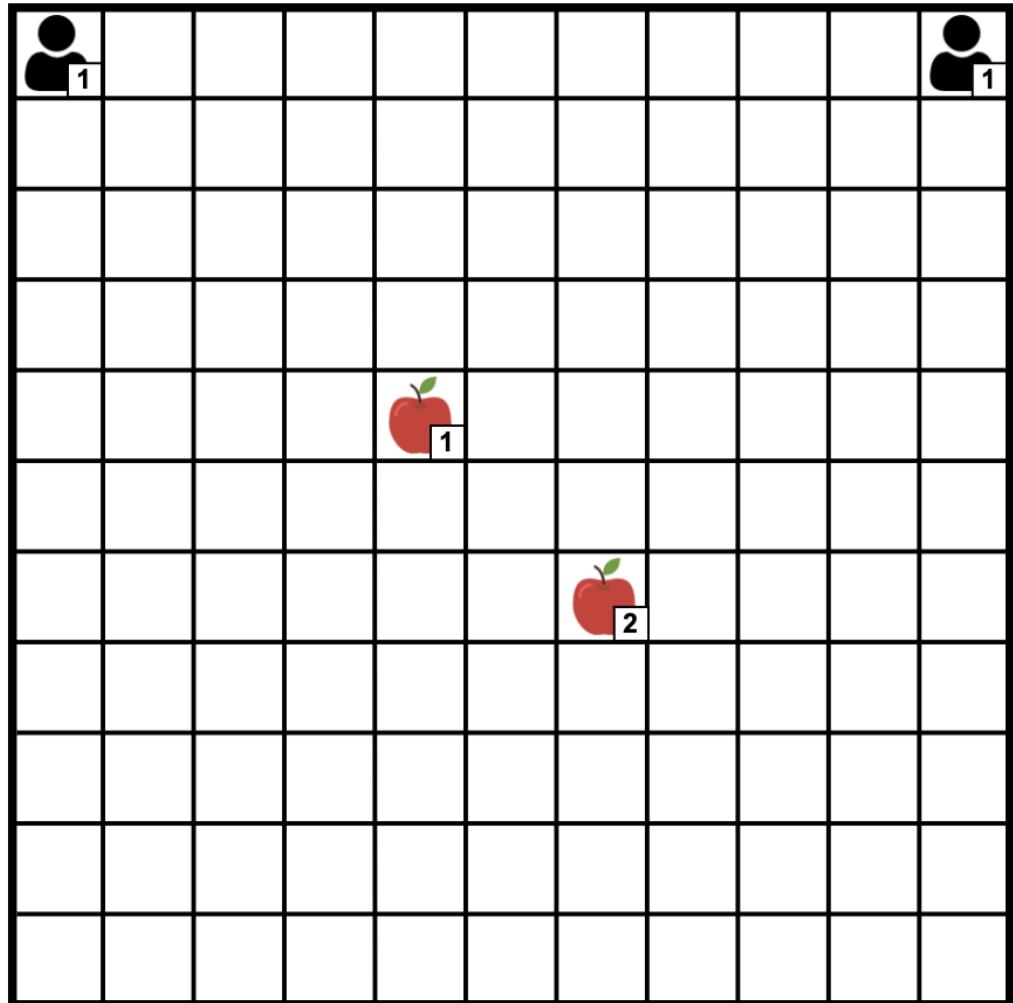
$$r_0, r_1, \dots, r_N$$

Our objective will be to **maximize the collective welfare** of the entire system.

$$\max_{(\pi_0, \pi_1, \dots, \pi_N)} E_{(\pi_0, \pi_1, \dots, \pi_N)} \left[ \sum_{t=0}^{\infty} \sum_{i=0}^N \gamma^t R_i(s_t, \pi_i(s_t), s_{t+1}) \right]$$

# Apple Picking Task

- N agents must collect all apples, but some apples cannot be picked alone and require teamwork!
- Each agent has a “level” that indicates how skilled they are at picking apples.
- Each apple has a “level” that indicates how difficult it is to pick that apple.
- An apple can only be collected if the sum of agent levels simultaneously picking it is greater than or equal to the level of the apple.
- Discrete action space with 6 actions.
  - $A = \{\text{UP}, \text{DOWN}, \text{LEFT}, \text{RIGHT}, \text{COLLECT}, \text{NO\_OP}\}$
- Reward is +1 for all agents every time an apple is picked.



# Simplest Solution: Convert MARL to RL

The simplest way to apply RL algorithms to multi-agent settings is to **reduce the problem to a single-agent problem** and apply traditional RL techniques.

## Central Learning

- Apply one single-agent RL algorithm to **control all agents centrally**.
- A central policy is learned over the joint action space  $A = (A_1 \times A_2 \times \dots \times A_N)$ .

## Independent Learning

- Apply single-agent RL algorithms to each agent **independently**.
- Agents do not explicitly consider or represent each other!

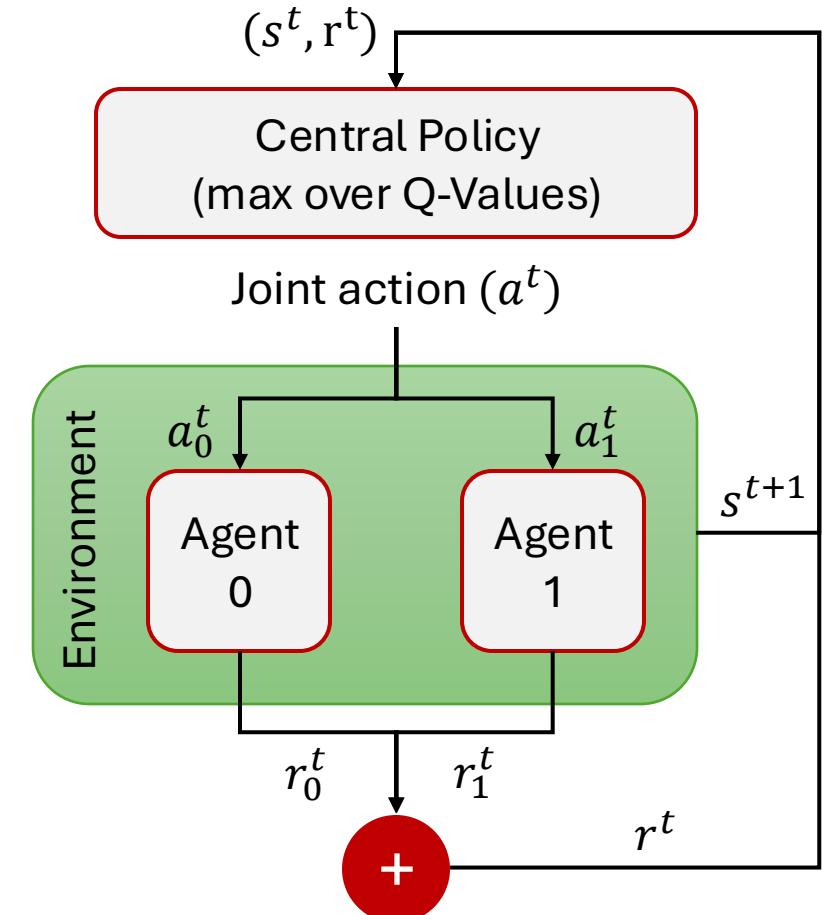
# Centralized Learning: Algorithm

## Algorithm 4 Central Q-learning (CQL) for stochastic games

- 1: Initialize:  $Q(s, a) = 0$  for all  $s \in S$  and  $a \in A = A_1 \times \dots \times A_n$
- 2: Repeat for every episode:
- 3: **for**  $t = 0, 1, 2, \dots$  **do**
- 4:   Observe current state  $s^t$
- 5:   With probability  $\epsilon$ : choose random joint action  $a^t \in A$
- 6:   Otherwise: choose joint action  $a^t \in \arg \max_a Q(s^t, a)$
- 7:   Apply joint action  $a^t$ , observe rewards  $r_1^t, \dots, r_n^t$  and next state  $s^{t+1}$
- 8:   Transform  $r_1^t, \dots, r_n^t$  into scalar reward  $r^t$
- 9:    $Q(s^t, a^t) \leftarrow Q(s^t, a^t) + \alpha [r^t + \gamma \max_{a'} Q(s^{t+1}, a') - Q(s^t, a^t)]$

We learn q-values over the space of joint-actions, so the algorithm doesn't know that we are training multiple agents.

Single-agent RL doesn't know how to process multiple reward signals, so we must transform the joint reward into a scalar reward.

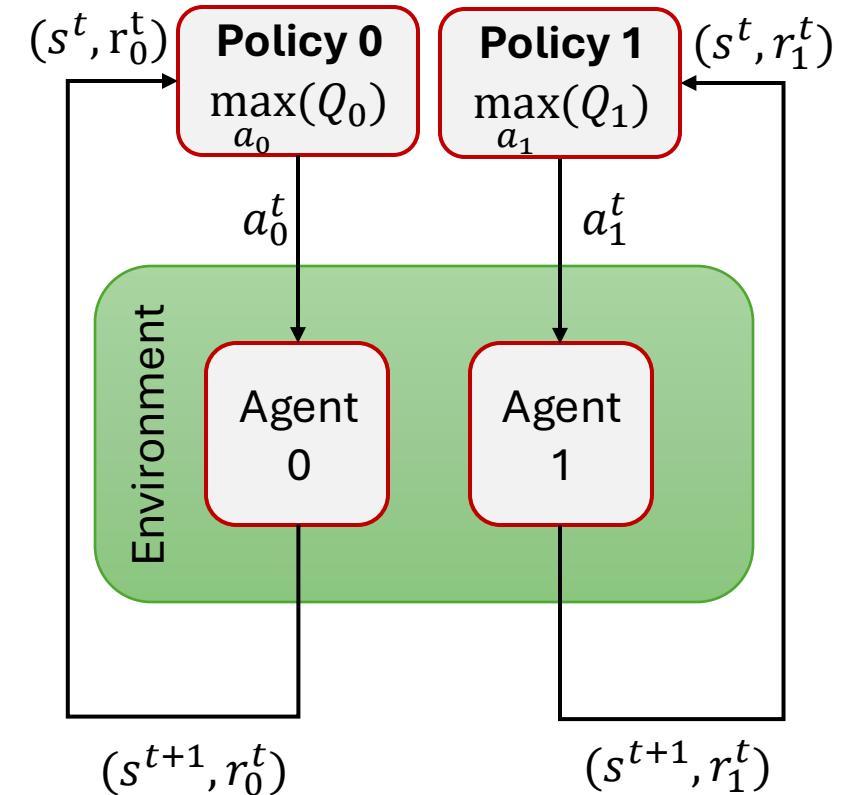


# Independent Learning: Algorithm

## Algorithm 5 Independent Q-learning (IQL) for stochastic games

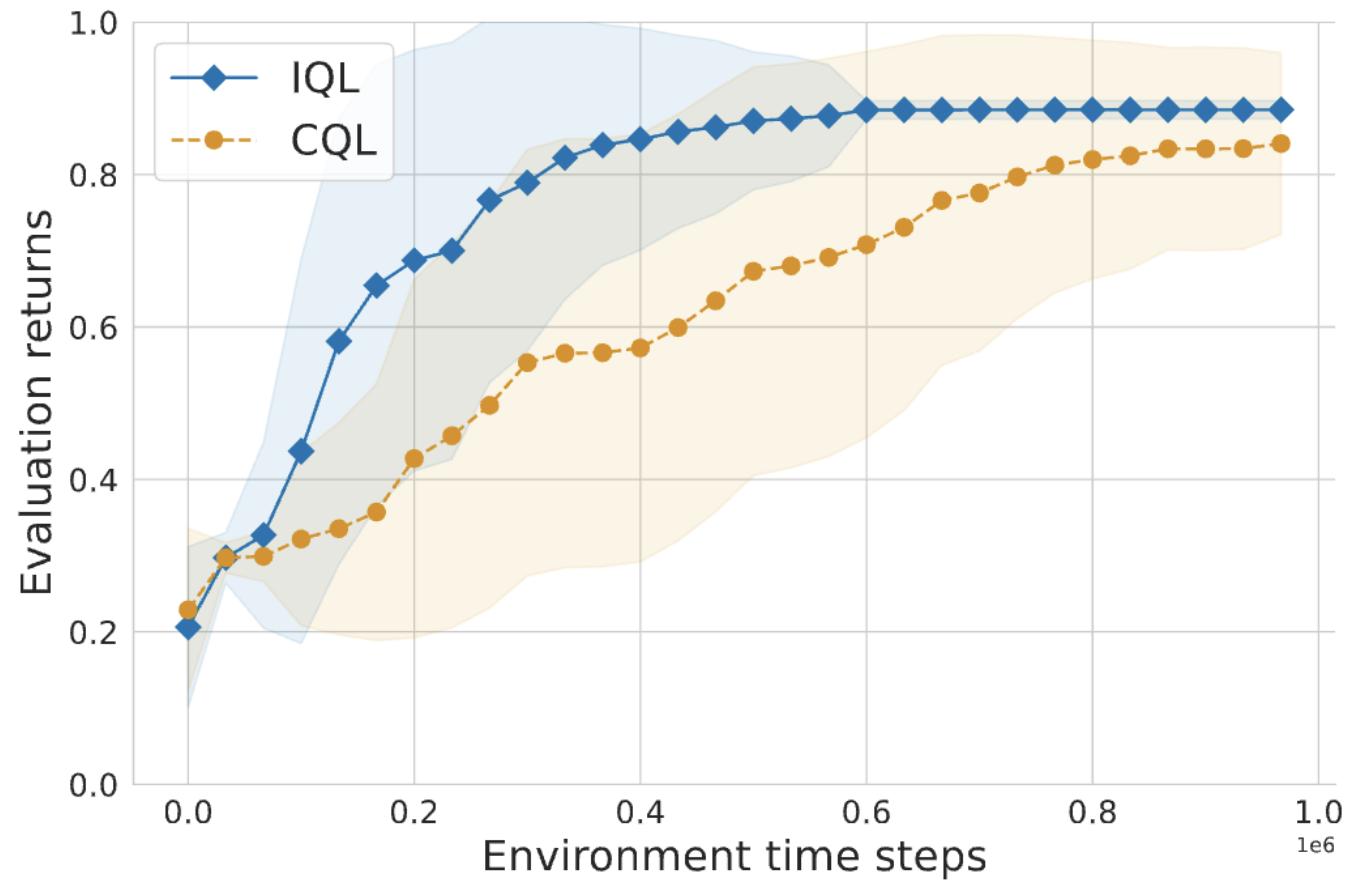
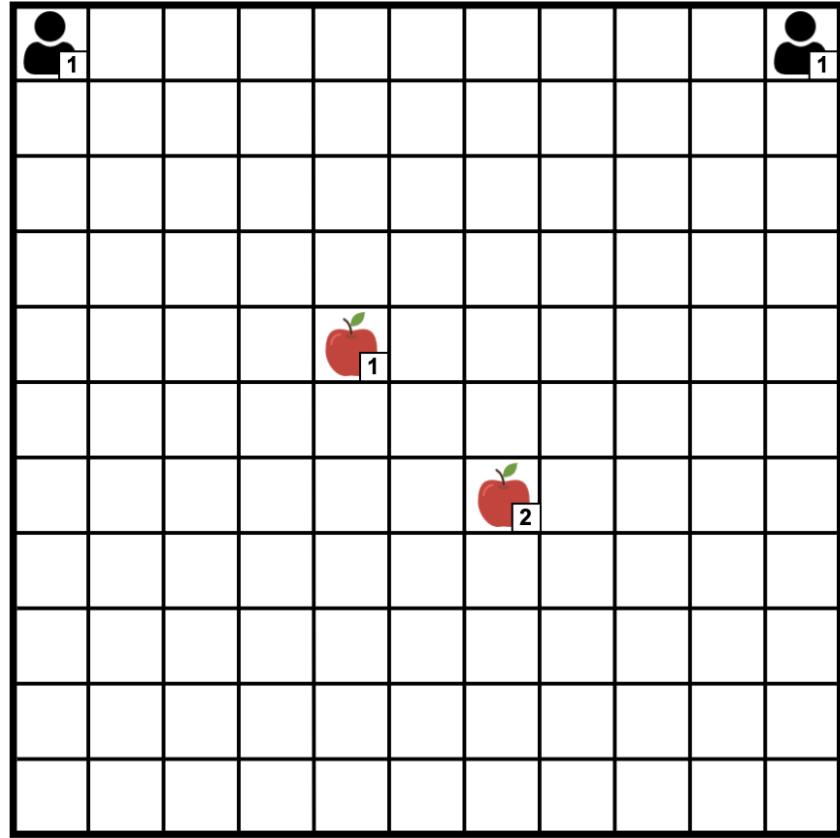
```
//Algorithm controls agent i
1: Initialize:  $Q_i(s, a_i) = 0$  for all  $s \in S, a_i \in A_i$ 
2: Repeat for every episode:
3:   for  $t = 0, 1, 2, \dots$  do
4:     Observe current state  $s^t$ 
5:     With probability  $\epsilon$ : choose random action  $a_i^t \in A_i$ 
6:     Otherwise: choose action  $a_i^t \in \arg \max_{a_i} Q_i(s^t, a_i)$ 
7:     (meanwhile, other agents  $j \neq i$  choose their actions  $a_j^t$ )
8:     Observe own reward  $r_i^t$  and next state  $s^{t+1}$ 
9:      $Q_i(s^t, a_i^t) \leftarrow Q_i(s^t, a_i^t) + \alpha [r_i^t + \gamma \max_{a'_i} Q_i(s^{t+1}, a'_i) - Q_i(s^t, a_i^t)]$ 
```

IQL doesn't have any information about the other agents.



It solely tries to model its own reward interactions in it's Q table.

# CQL + IQL: Results



# Quiz: Why does IQL learn faster than CQL?

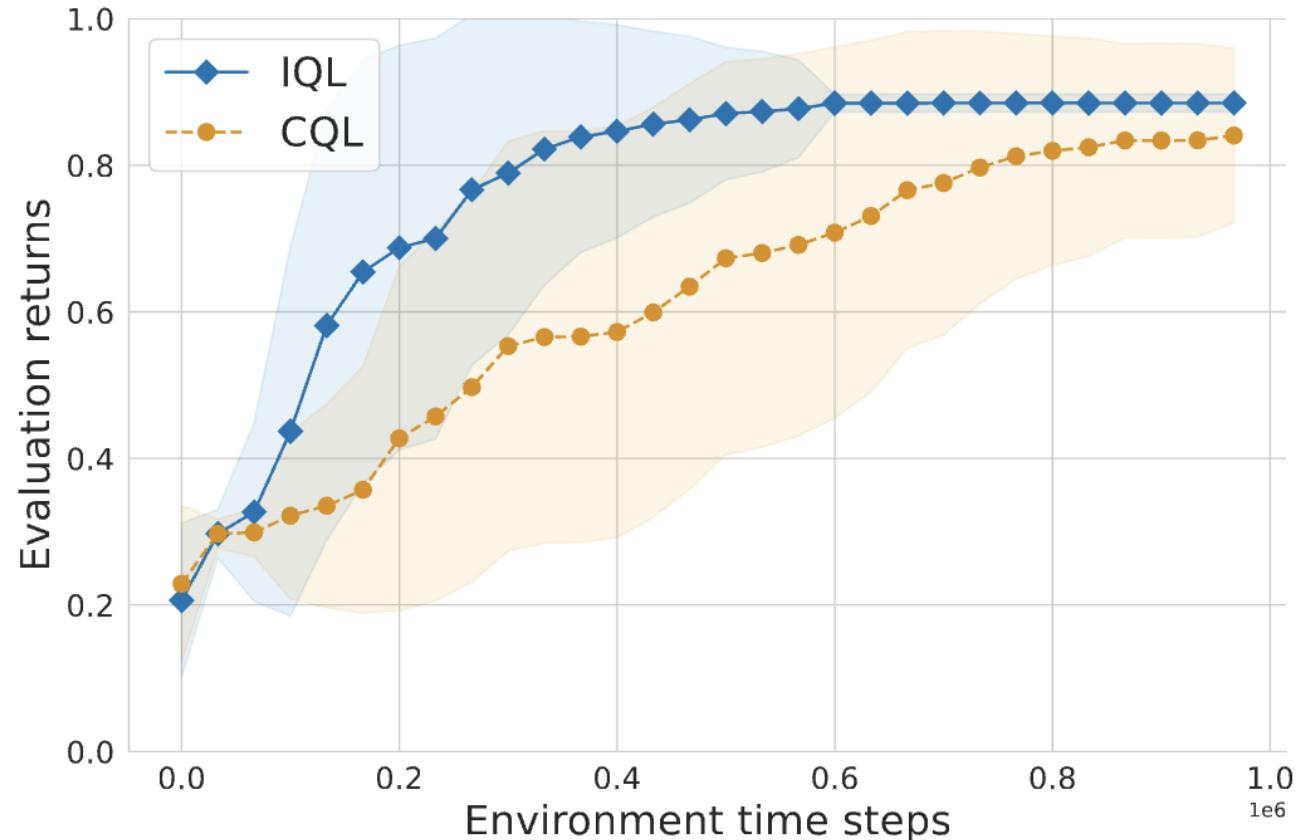
## Algorithm 4 Central Q-learning (CQL) for stochastic games

```
1: Initialize:  $Q(s, a) = 0$  for all  $s \in S$  and  $a \in A = A_1 \times \dots \times A_n$ 
2: Repeat for every episode:
3: for  $t = 0, 1, 2, \dots$  do
4:   Observe current state  $s^t$ 
5:   With probability  $\epsilon$ : choose random joint action  $a^t \in A$ 
6:   Otherwise: choose joint action  $a^t \in \arg \max_a Q(s^t, a)$ 
7:   Apply joint action  $a^t$ , observe rewards  $r_1^t, \dots, r_n^t$  and next state  $s^{t+1}$ 
8:   Transform  $r_1^t, \dots, r_n^t$  into scalar reward  $r^t$ 
9:    $Q(s^t, a^t) \leftarrow Q(s^t, a^t) + \alpha [r^t + \gamma \max_{a'} Q(s^{t+1}, a') - Q(s^t, a^t)]$ 
```

## Algorithm 5 Independent Q-learning (IQL) for stochastic games

// Algorithm controls agent  $i$

```
1: Initialize:  $Q_i(s, a_i) = 0$  for all  $s \in S, a_i \in A_i$ 
2: Repeat for every episode:
3: for  $t = 0, 1, 2, \dots$  do
4:   Observe current state  $s^t$ 
5:   With probability  $\epsilon$ : choose random action  $a_i^t \in A_i$ 
6:   Otherwise: choose action  $a_i^t \in \arg \max_{a_i} Q_i(s^t, a_i)$ 
7:   (meanwhile, other agents  $j \neq i$  choose their actions  $a_j^t$ )
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9:    $Q_i(s^t, a_i^t) \leftarrow Q_i(s^t, a_i^t) + \alpha [r_i^t + \gamma \max_{a'_i} Q_i(s^{t+1}, a'_i) - Q_i(s^t, a_i^t)]$ 
```



# Centralized Learning: Challenges

- Works great for low N! But exploration suffers exponentially as N grows.

Number of Agents in Apple Picking (N)	Size of Joint Action Space ( A )
2	36
3	216
4	1296
5	7776

$\left. \right\} \prod_{i=0}^N |A_i| = 6^N$

- Physical Limitations. In robotics/real world tasks we cannot assume that we have centralized control over all agents (or even if we do there are major communication/latency issues!)
- Requires the scalarization of reward signals, which is sometimes not possible.

# Independent Learning

- It performs fairly compared to a lot of SOTA MARL algorithms!
- All single-agent algorithms have been independently applied to MARL.

**Algorithm 17** Independent deep Q-networks

```

1: Initialize  $n$  value networks with random parameters  $\theta_1, \dots, \theta_n$ 
2: Initialize  $n$  target networks with parameters  $\bar{\theta}_1 = \theta_1, \dots, \bar{\theta}_n = \theta_n$ 
3: Initialize a replay buffer for each agent  $D_1, D_2, \dots, D_n$ 
4: for time step  $t=0, 1, 2, \dots$  do
5:   Collect current observations  $o_1^t, \dots, o_n^t$ 
6:   for agent  $i=1, \dots, n$  do
7:     With probability  $\epsilon$ : choose random action  $a_i^t$ 
8:     Otherwise: choose  $a_i^t \in \arg \max_{a_i} Q(h_i^t, a_i; \theta_i)$ 
9:   Apply actions  $(a_1^t, \dots, a_n^t)$ ; collect rewards  $r_1^t, \dots, r_n^t$  and next observations
 $o_1^{t+1}, \dots, o_n^{t+1}$ 
10:  for agent  $i=1, \dots, n$  do
11:    Store transition  $(h_i^t, a_i^t, r_i^t, h_i^{t+1})$  in replay buffers  $D_i$ 
12:    Sample random mini-batch of  $B$  transitions  $(h_i^k, a_i^k, r_i^k, h_i^{k+1})$  from  $D_i$ 
13:    if  $s^{k+1}$  is terminal2 then
14:      Targets  $y_i^k \leftarrow r_i^k$ 
15:    else
16:      Targets  $y_i^k \leftarrow r_i^k + \gamma \max_{a'_i \in A_i} Q(h_i^{k+1}, a'_i; \bar{\theta}_i)$ 
17:    Loss  $\mathcal{L}(\theta_i) \leftarrow \frac{1}{B} \sum_{k=1}^B (y_i^k - Q(h_i^k, a_i^k; \theta_i))^2$ 
18:    Update parameters  $\theta_i$  by minimizing the loss  $\mathcal{L}(\theta_i)$ 
19:    In a set interval, update target network parameters  $\bar{\theta}_i$ 
```

**Algorithm 18** Independent REINFORCE

```

1: Initialize  $n$  policy networks with random parameters  $\phi_1, \dots, \phi_n$ 
2: Repeat for every episode:
3:   for time step  $t=0, 1, 2, \dots, T-1$  do
4:     Collect current observations  $o_1^t, \dots, o_n^t$ 
5:     for agent  $i=1, \dots, n$  do
6:       Sample actions  $a_i^t$  from  $\pi(\cdot | h_i^t; \phi_i)$ 
7:       Apply actions  $(a_1^t, \dots, a_n^t)$ ; collect rewards  $r_1^t, \dots, r_n^t$  and next observations
 $o_1^{t+1}, \dots, o_n^{t+1}$ 
8:     for agent  $i=1, \dots, n$  do
9:       Loss  $\mathcal{L}(\phi_i) \leftarrow -\frac{1}{T} \sum_{t=0}^{T-1} \left( \sum_{\tau=t}^{T-1} \gamma^{\tau-t} r_\tau^\tau \right) \log \pi(a_i^t | h_i^t; \phi_i)$ 
10:      Update parameters  $\phi_i$  by minimizing the loss  $\mathcal{L}(\phi_i)$ 
```

**Algorithm 19** Independent A2C with synchronous environments

```

1: Initialize  $n$  actor networks with random parameters  $\phi_1, \dots, \phi_n$ 
2: Initialize  $n$  critic networks with random parameters  $\theta_1, \dots, \theta_n$ 
3: Initialize  $K$  parallel environments
4: for time step  $t=0 \dots$  do
5:   Batch of observations for each agent and environment:  $\begin{bmatrix} o_1^{t,1} \dots o_1^{t,K} \\ \vdots \\ o_n^{t,1} \dots o_n^{t,K} \end{bmatrix}$ 
6:   Sample actions  $\begin{bmatrix} a_1^{t,1} \dots a_1^{t,K} \\ \vdots \\ a_n^{t,1} \dots a_n^{t,K} \end{bmatrix} \sim \pi(\cdot | h_1^t; \phi_1), \dots, \pi(\cdot | h_n^t; \phi_n)$ 
7:   Apply actions; collect rewards  $\begin{bmatrix} r_1^{t,1} \dots r_1^{t,K} \\ \vdots \\ r_n^{t,1} \dots r_n^{t,K} \end{bmatrix}$  and observations  $\begin{bmatrix} o_1^{t+1,1} \dots o_1^{t+1,K} \\ \vdots \\ o_n^{t+1,1} \dots o_n^{t+1,K} \end{bmatrix}$ 
8:   for agent  $i=1, \dots, n$  do
9:     if  $s^{t+1,k}$  is terminal then
10:      Advantage  $Adv(h_i^{t,k}, a_i^{t,k}) \leftarrow r_i^{t,k} - V(h_i^{t,k}; \theta_i)$ 
11:      Critic target  $y_i^{t,k} \leftarrow r_i^{t,k}$ 
12:    else
13:      Advantage  $Adv(h_i^{t,k}, a_i^{t,k}) \leftarrow r_i^{t,k} + \gamma V(h_i^{t+1,k}; \theta_i) - V(h_i^{t,k}; \theta_i)$ 
14:      Critic target  $y_i^{t,k} \leftarrow r_i^{t,k} + \gamma V(h_i^{t+1,k}; \theta_i)$ 
15:    Actor loss  $\mathcal{L}(\phi_i) \leftarrow \frac{1}{K} \sum_{k=1}^K Adv(h_i^{t,k}, a_i^{t,k}) \log \pi(a_i^{t,k} | h_i^{t,k}; \phi_i)$ 
16:    Critic loss  $\mathcal{L}(\theta_i) \leftarrow \frac{1}{K} \sum_{k=1}^K (y_i^{t,k} - V(h_i^{t,k}; \theta_i))^2$ 
17:    Update parameters  $\phi_i$  by minimizing the actor loss  $\mathcal{L}(\phi_i)$ 
18:    Update parameters  $\theta_i$  by minimizing the critic loss  $\mathcal{L}(\theta_i)$ 
```

# Independent Learning: Challenges

- Much better scaling! Can be deployed easily on physical systems!
- Suffers from *non-stationary* environment dynamics.

Single Agent Dynamics

$$P(s' | s, a) = T(s'| s, a)$$

Probability of subsequent states stays constant over time.

Multi Agent Dynamics

$$P_i(s' | s, a_i) = \sum_{a_{-i} \in A_{-i}} T(s'| s, \langle a_i, a_{-i} \rangle) \left[ \prod_{j \neq i} \pi_j(a_j | s^t) \right]$$

Changes to environment state are not guaranteed to be the result of my actions

- Depending on reward formulation, it suffers from poor *credit assignment*.

# The Credit Assignment Problem

Temporal Credit Assignment

*Which of my **past actions** were responsible for my earned reward?*

Multi-Agent Credit Assignment

*Which **agent** was responsible for my earned reward?*

Recall that each agent its own reward signal

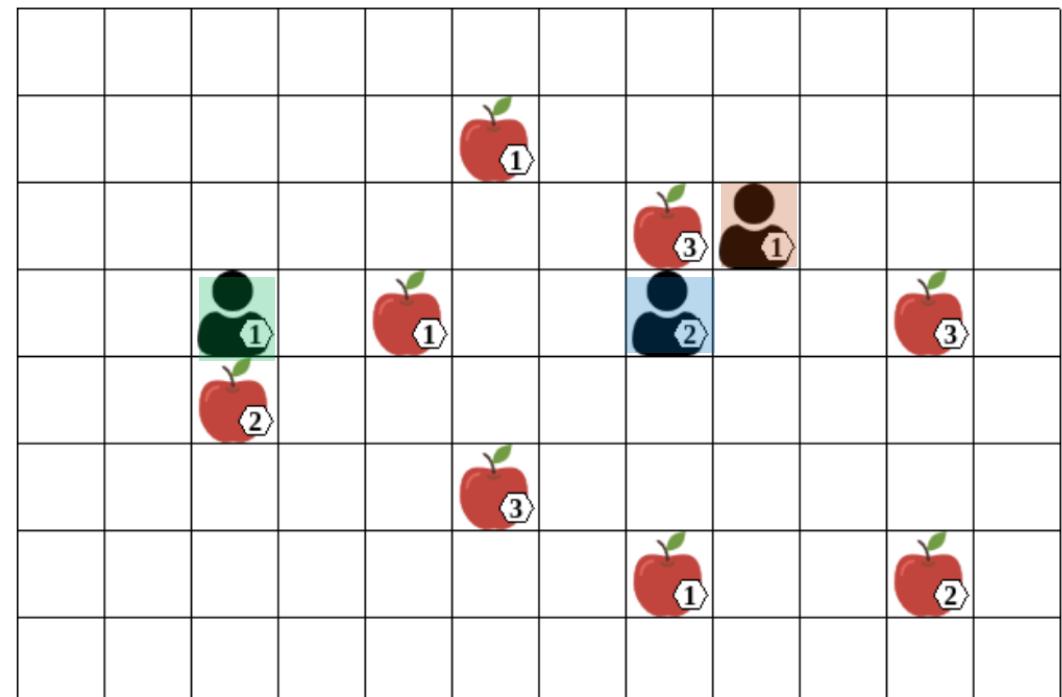
$$r_0, r_1, \dots, r_N$$

What happens when we shift to a common reward?  
(i.e. all agents receive the same reward signal at time t)

$$r_0 = r_1 = \dots = r_N$$

Now the **green agent** gets some reward for the apple  
that the **orange** and **blue** agents did!

Tasks are often formulated as common reward!



# Middle Ground? CTDE Methods!

*Can we create MARL algorithms that can still be deployed on a decentralized system while overcoming obstacles in scaling, stationarity, and credit assignment?*

**Independent Learning:** Decentralized Training, Decentralized Execution

**Central Learning:** Centralized Training, Centralized Execution

## Centralized Training, Decentralized Execution.

Utilize *privileged centralized information* at training time to determine how agent's actions affect the rewards of the system and share experiences between agents.

At execution time, ensure that all each policy can independently execute, with zero dependencies on centralized information.

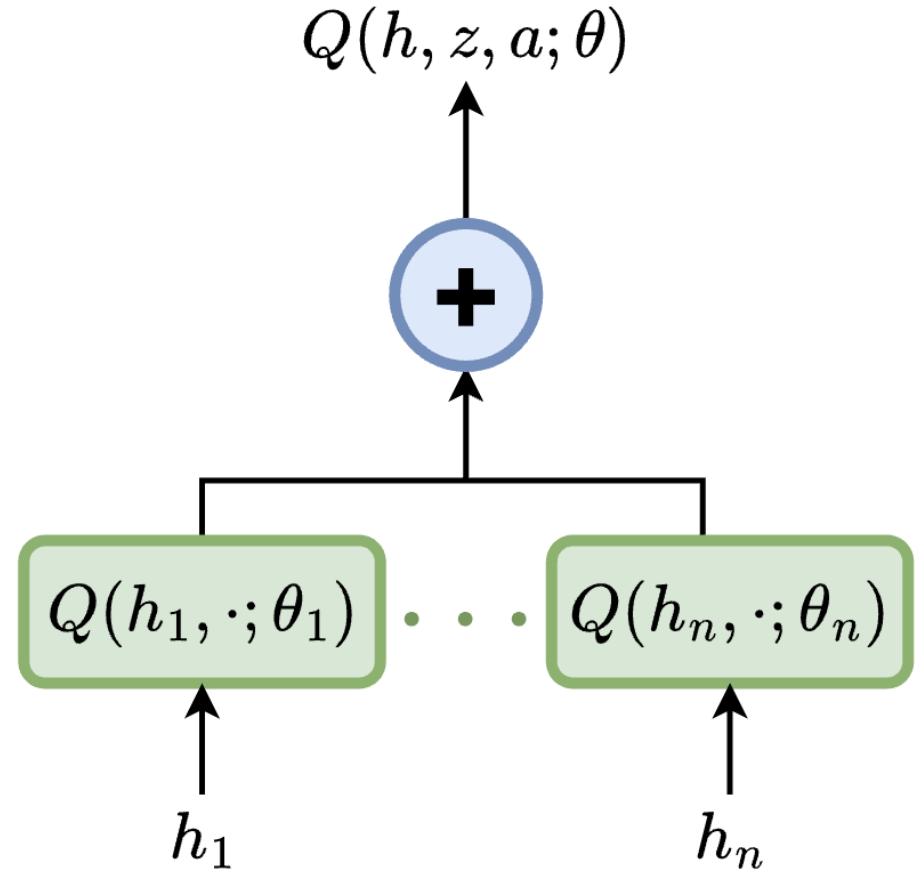
# Value Decomposition Networks

---

**Algorithm 21** Value decomposition networks (VDN)

---

- 1: Initialize  $n$  utility networks with random parameters  $\theta_1, \dots, \theta_n$
  - 2: Initialize  $n$  target networks with parameters  $\bar{\theta}_1 = \theta_1, \dots, \bar{\theta}_n = \theta_n$
  - 3: Initialize a shared replay buffer  $D$
  - 4: **for** time step  $t = 0, 1, 2, \dots$  **do**
  - 5:   Collect current observations  $o_1^t, \dots, o_n^t$
  - 6:   **for** agent  $i = 1, \dots, n$  **do**
  - 7:     With probability  $\epsilon$ : choose random action  $a_i^t$
  - 8:     Otherwise: choose  $a_i^t \in \arg \max_{a_i} Q(h_i^t, a_i; \theta_i)$
  - 9:   Apply actions; collect shared reward  $r^t$  and next observations  $o_1^{t+1}, \dots, o_n^{t+1}$
  - 10:   Store transition  $(h^t, a^t, r^t, h^{t+1})$  in shared replay buffer  $D$
  - 11:   Sample mini-batch of  $B$  transitions  $(h^k, a^k, r^k, h^{k+1})$  from  $D$
  - 12:   **if**  $s^{k+1}$  is terminal **then**
  - 13:     Targets  $y^k \leftarrow r^k$
  - 14:   **else**
  - 15:     Targets  $y^k \leftarrow r^k + \gamma \sum_{i \in I} \max_{a'_i \in A_i} Q(h_i^{k+1}, a'_i; \bar{\theta}_i)$
  - 16:     Loss  $\mathcal{L}(\theta) \leftarrow \frac{1}{B} \sum_{k=1}^B \left( y^k - \sum_{i \in I} Q(h_i^k, a_i^k; \theta_i) \right)^2$
  - 17:     Update parameters  $\theta$  by minimizing the loss  $\mathcal{L}(\theta)$
  - 18:   In a set interval, update target network parameters  $\bar{\theta}_i$  for each agent  $i$
- 



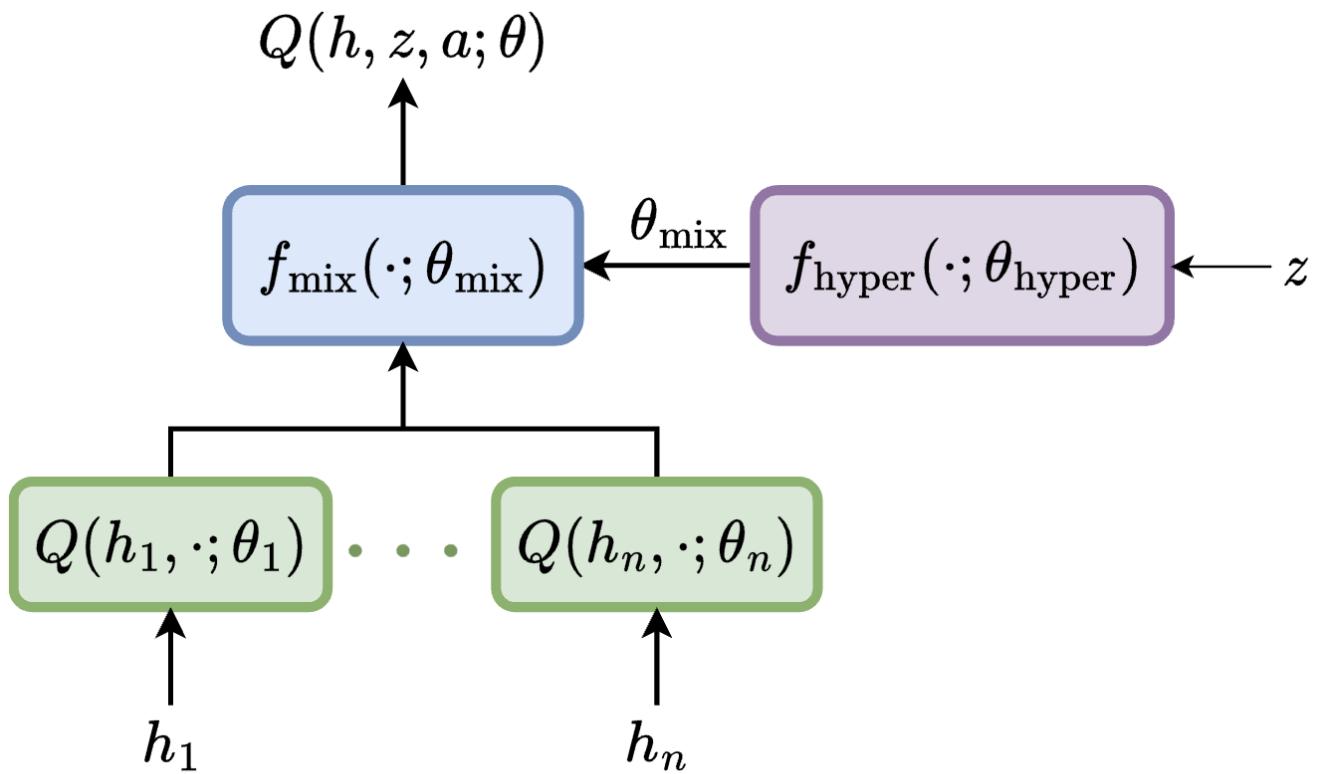
# QMIX: Non-Linear VDN

**Algorithm 22** QMIX

```

1: Initialize  $n$  utility networks with random parameters  $\theta_1, \dots, \theta_n$ 
2: Initialize  $n$  target networks with parameters  $\bar{\theta}_1 = \theta_1, \dots, \bar{\theta}_n = \theta_n$ 
3: Initialize hypernetwork with random parameters  $\theta_{\text{hyper}}$ 
4: Initialize a shared replay buffer  $D$ 
5: for time step  $t=0, 1, 2, \dots$  do
6:   Collect current centralized information  $z^t$  and observations  $o_1^t, \dots, o_n^t$ 
7:   for agent  $i=1, \dots, n$  do
8:     With probability  $\epsilon$ : choose random action  $a_i^t$ 
9:     Otherwise: choose  $a_i^t \in \arg \max_{a_i} Q(h_i^t, a_i; \theta_i)$ 
10:    Apply actions; collect shared reward  $r^t$ , next centralized information  $z^{t+1}$ 
       and observations  $o_1^{t+1}, \dots, o_n^{t+1}$ 
11:    Store transition  $(h^t, z^t, a^t, r^t, h^{t+1}, z^{t+1})$  in shared replay buffer  $D$ 
12:    Sample mini-batch of  $B$  transitions  $(h^k, z^k, a^k, r^k, h^{k+1}, z^{k+1})$  from  $D$ 
13:    if  $s^{k+1}$  is terminal then
14:      Targets  $y^k \leftarrow r^k$ 
15:    else
16:      Mixing parameters  $\theta_{\text{mix}}^{k+1} \leftarrow f_{\text{hyper}}(z^{k+1}; \theta_{\text{hyper}})$ 
17:      Targets  $y^k \leftarrow r^k + \gamma f_{\text{mix}} \begin{pmatrix} \max_{a'_1} Q(h_1^{k+1}, a'_1; \bar{\theta}_1), \\ \ddots \\ \max_{a'_n} Q(h_n^{k+1}, a'_n; \bar{\theta}_n) \end{pmatrix}; \theta_{\text{mix}}^{k+1}$ 
18:      Mixing parameters  $\theta_{\text{mix}}^k \leftarrow f_{\text{hyper}}(z^k; \theta_{\text{hyper}})$ 
19:      Value estimates  $Q(h^k, z^k, a^k; \theta) \leftarrow f_{\text{mix}}(Q(h_1^k, a_1^k; \theta_1), \dots, Q(h_n^k, a_n^k; \theta_n); \theta_{\text{mix}}^k)$ 
20:      Loss  $\mathcal{L}(\theta) \leftarrow \frac{1}{B} \sum_{k=1}^B (y^k - Q(h^k, z^k, a^k; \theta))^2$ 
21:      Update parameters  $\theta$  by minimizing the loss  $\mathcal{L}(\theta)$ 
22:      In a set interval, update target network parameters  $\bar{\theta}_i$  for each agent  $i$ 

```



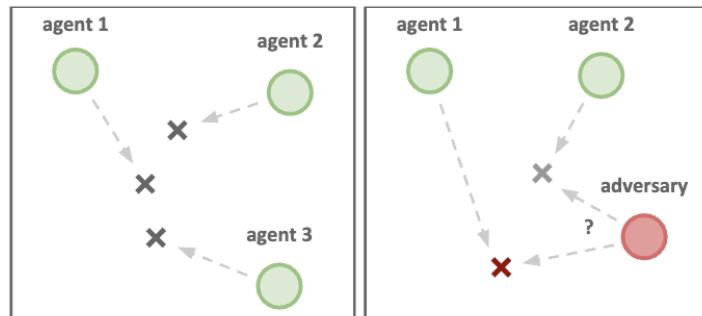
# Other CTDE Extensions

## Multi-Agent Actor-Critic for Mixed Cooperative-Competitive Environments

Ryan Lowe\*  
McGill University  
OpenAI

Yi Wu\*  
UC Berkeley

Aviv Tamar  
UC Berkeley



## The Surprising Effectiveness of PPO in Cooperative Multi-Agent Games

Chao Yu<sup>1#\*</sup>, Akash Velu<sup>2#\*</sup>, Eugene Vinitsky<sup>2b</sup>, Jiaxuan Gao<sup>1</sup>,  
Yu Wang<sup>1b</sup>, Alexandre Bayen<sup>2</sup>, Yi Wu<sup>13b</sup>

<sup>1</sup> Tsinghua University <sup>2</sup> University of California, Berkeley <sup>3</sup> Shanghai Qi Zhi Institute

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# Current Benchmarks and Challenges

Where to Deploy?

What Challenges require Multi-Agent Learning right now?

How does deployment difficulty scale?



# Current Benchmarks and Challenges

Article | Published: 30 October 2019

## Grandmaster level in StarCraft II using multi-agent reinforcement learning

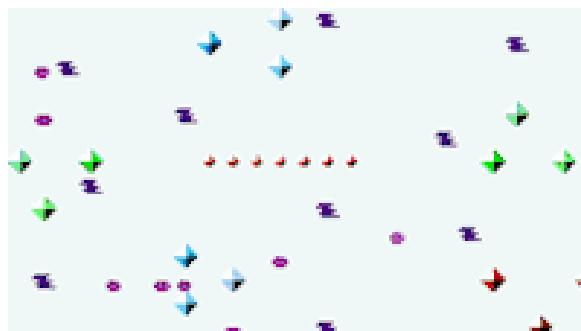
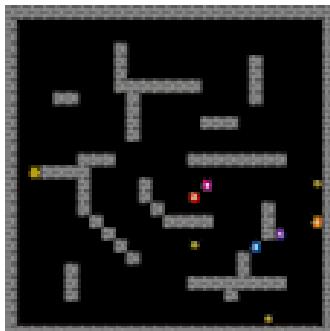
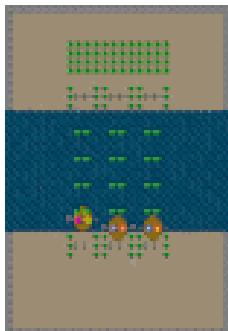
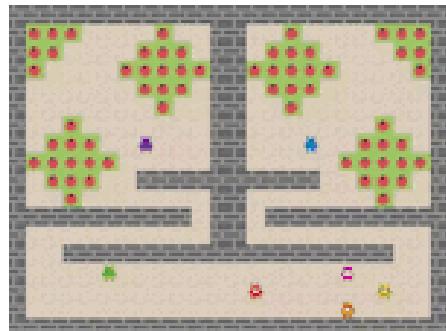
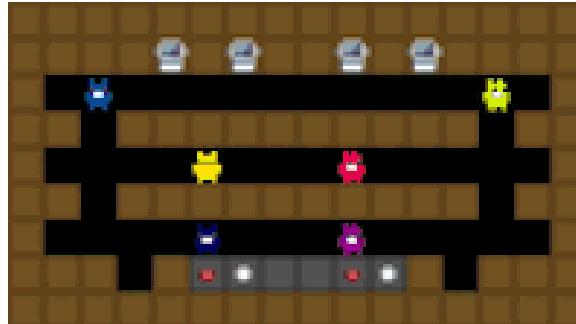
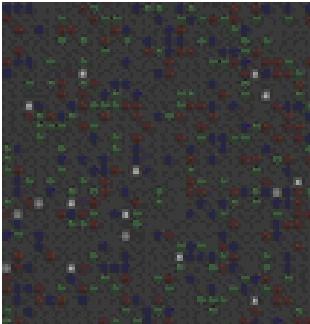
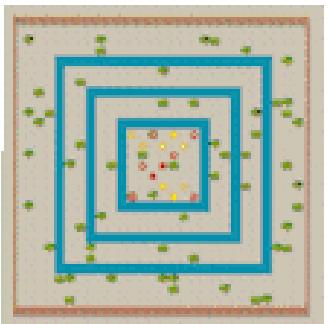
[Oriol Vinyals](#)✉, [Igor Babuschkin](#), [Wojciech M. Czarnecki](#), [Michaël Mathieu](#), [Andrew Dudzik](#), [Junyoung Chung](#), [David H. Choi](#), [Richard Powell](#), [Timo Ewalds](#), [Petko Georgiev](#), [Junhyuk Oh](#), [Dan Horgan](#), [Manuel Kroiss](#), [Ivo Danihelka](#), [Aja Huang](#), [Laurent Sifre](#), [Trevor Cai](#), [John P. Agapiou](#), [Max Jaderberg](#), [Alexander S. Vezhnevets](#), [Rémi Leblond](#), [Tobias Pohlen](#), [Valentin Dalibard](#), [David Budden](#), ... [David Silver](#)✉



AlphaStar (2019)



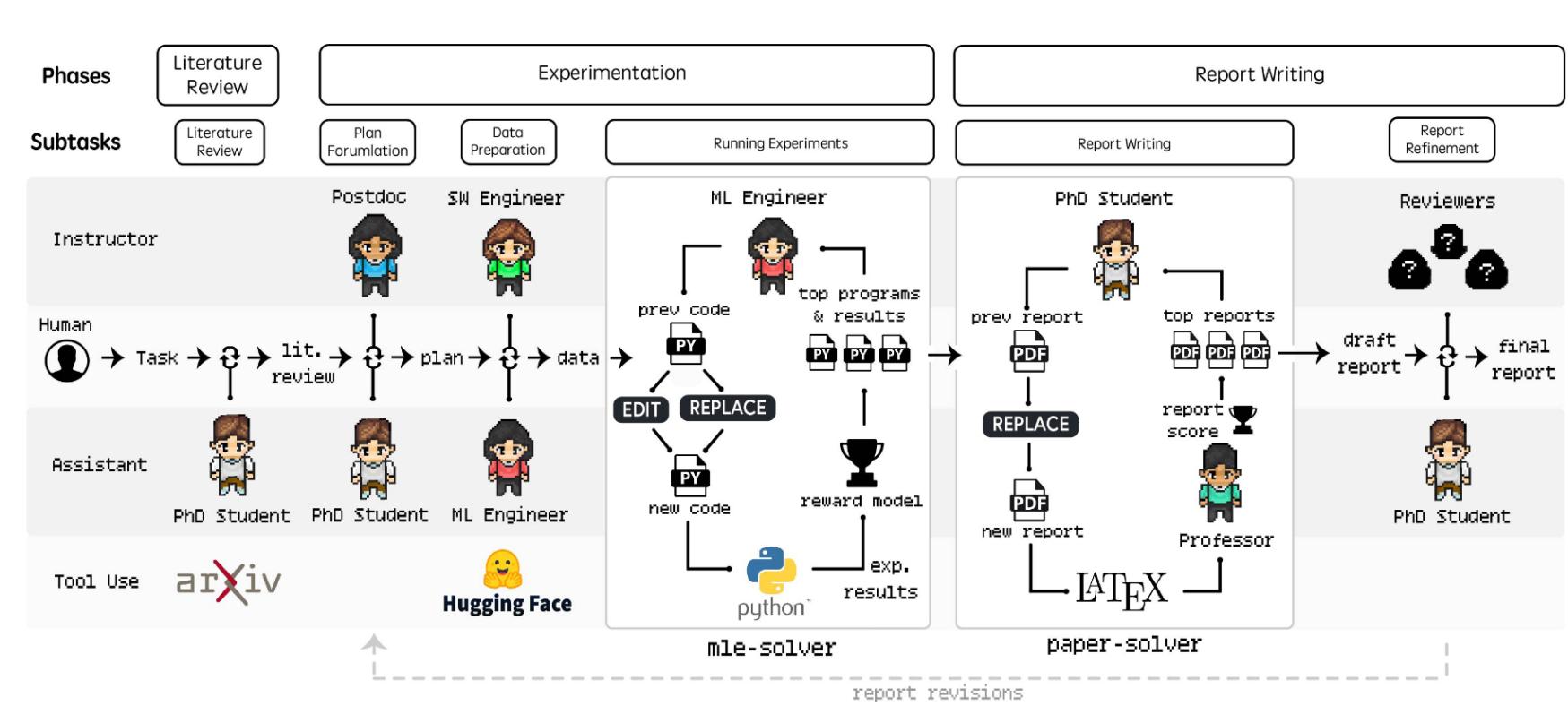
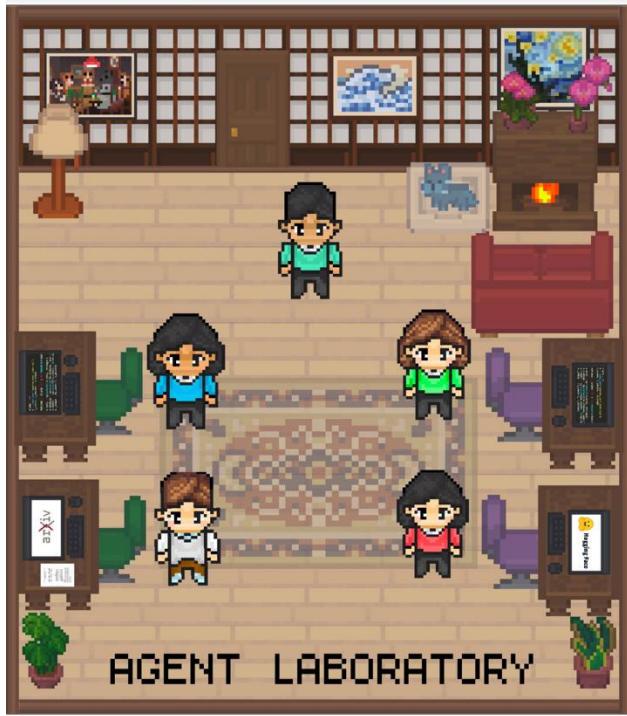
# Current Benchmarks and Challenges



# Current Explorations: LLMs

## Agent Laboratory: Using LLM Agents as Research Assistants

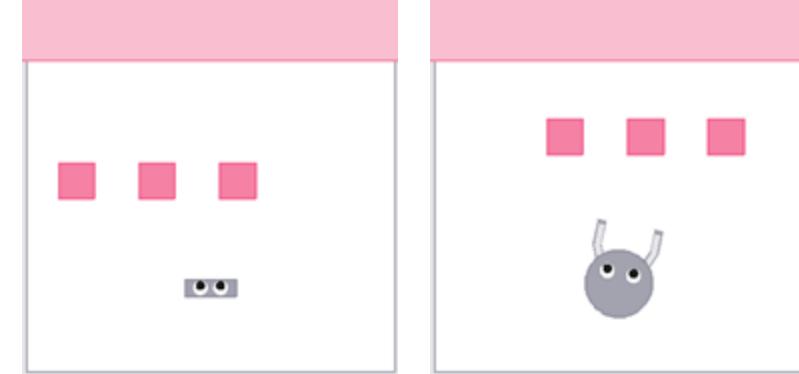
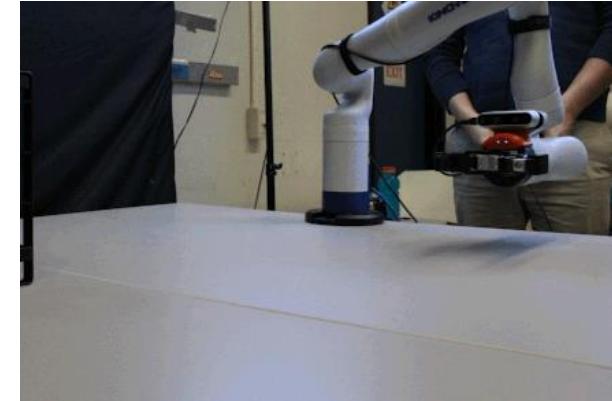
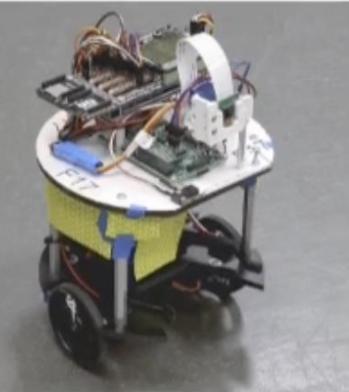
Agent Laboratory: Using LLM Agents as Research Assistants



# Current Explorations: LLMs



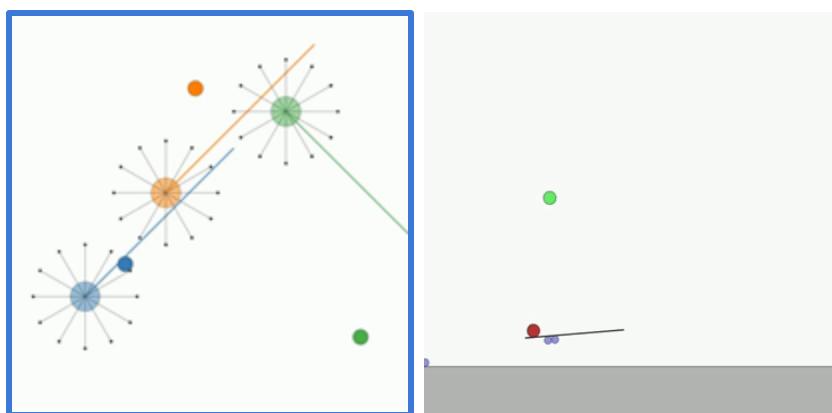
# What does my PhD Research Look Like?



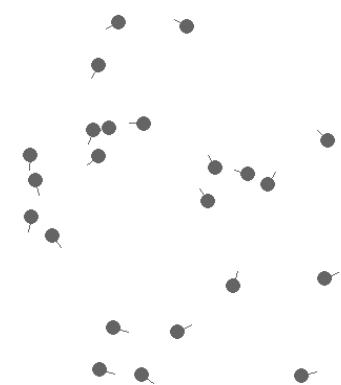
**Robot Swarm Learning + Sim2Real**  
[ICONS'24], [CoRR'24], [AAMAS'25]

**Assistive Robotics**  
[HRI'25], [SciData'24]

**X-Embodiment Learning**  
[RLJ'24]



**Multi-Agent Reinforcement Learning**  
[in preparation]



**Repr. Learning + Behavior Discovery**  
[GECCO'23], [MRS'23] [AAMAS'25]

Multi-Agent Learning  
is still a young field  
and there's lots of  
exciting work to do!



Let's chat!  
[c.mattson@utah.edu](mailto:c.mattson@utah.edu)