Problem 16

We collect data on the play times of 100 games of *Chutes and Ladders* (sometimes known as *Snakes and Ladders*) and want to use this data to perform a hypothesis test.

Problem 16.1

Which of the following pairs of hypotheses can we test using this data?

Option 1: **Null Hypothesis:** In a random sample of Chutes and Ladders games, the average play time is 30 minutes. **Alternative Hypothesis:** In a random sample of Chutes and Ladders games, the average play time is not 30 minutes.

Option 2: **Null Hypothesis:** In a random sample of Chutes and Ladders games, the average play time is not 30 minutes. **Alternative Hypothesis:** In a random sample of Chutes and Ladders games, the average play time is 30 minutes

Option 3: **Null Hypothesis:** A game of Chutes and Ladders takes, on average, 30 minutes to play. **Alternative Hypothesis:** A game of Chutes and Ladders does not take, on average, 30 minutes to play.

Option 4: **Null Hypothesis:** A game of Chutes and Ladders does not take, on average, 30 minutes to play. **Alternative Hypothesis:** A game of Chutes and Ladders takes, on average, 30 minutes to play.

	Option	1
	Option	2
	Option	3

Option 4

Problem 16.2

We use our collected data to construct a 95% CLT-based confidence interval for the average play time of a game of *Chutes and Ladders*. This 95% confidence interval is [26.47, 28.47]. For the 100 games for which we collected data, what is the mean and standard deviation of the play times?

Problem 16.3

Does the CLT say that the distribution of play times of the 100 games is roughly normal?

Yes

O No

Problem 16.4

Of the two hypotheses you selected in part (a), which one is better supported by the data?

- Null Hypothesis
- Alternative Hypothesis

Problem 12

In the game *Spot It*, players race to identify an object that appears on two different cards. Each card contains images of eight objects, and exactly one object is common to both cards.



Problem 12.1

Suppose the objects appearing on each card are stored in an array, and our task is to find the object that appears on both cards. Complete the function find_match that takes as input two arrays of 8 objects each, with one object in common, and returns the name of the object in both arrays.

For example, suppose we have two arrays defined as follows.

```
objects1 = np.array(["dragon", "spider", "car", "water droplet", "spiderweb", "candle", "ice complets2 = np.array(["zebra", "lock", "dinosaur", "eye", "fire", "shamrock", "spider", "carrot"
```

Then find_match(objects1, objects2) should evaluate to "spider". Your function must include a for loop, and it must take at most three lines of code (not counting the line with def).

Problem 12.2

Now suppose the objects appearing on each card are stored in a DataFrame with 8 rows and one column called "object". Complete the function find_match_again that takes as input two such DataFrames with one object in common and returns the name of the object in both DataFrames.

Your function may not call the previous function find_match, and it must take exactly **one line of code** (not counting the line with def).

Problem 6

In this question, we'll explore the relationship between the ages and incomes of credit card applicants.

Problem 6.1

The credit card company that owns the data in apps, BruinCard, has decided not to give us access to the entire apps DataFrame, but instead just a sample of apps called small apps. We'll start by using the information in small_apps to compute the regression line that predicts the age of an applicant given their income.

For an applicant with an income that is $\frac{8}{3}$ standard deviations above the mean income, we predict their age to be $\frac{4}{5}$ standard deviations above the mean age. What is the correlation coefficient, r, between incomes and ages in small_apps? Give your answer as a **fully simplified fraction**.

Click to view the solution.

Problem 6.2

Now, we want to predict the income of an applicant given their age. We will again use the information in $\frac{\text{small_apps}}{\text{small_apps}}$ to find the regression line. The regression line predicts that an applicant whose age is $\frac{4}{5}$ standard deviations above the mean age has an income that is s standard deviations above the mean income. What is the value of s? Give your answer as a **fully simplified fraction**.

Problem 6.3

BruinCard has now taken away our access to both apps and small_apps, and has instead given us access to an even smaller sample of apps called mini_apps, we know the following information: - All incomes and ages.

We use the data in mini_apps to find the regression line that will allow us to predict the income of an applicant given their age. Just to test the limits of this regression line, we use it to predict the income of an applicant who is -2 years old, even though it doesn't make sense for a person to have a negative age.

Let *I* be the regression line's prediction of this applicant's income. Which of the following inequalities are guaranteed to be satisfied? Select all that apply.

- I < 0
- \square I < mean income
- $|I \text{mean income}| \le |\text{mean age} + 2|$
- $egin{array}{c} & \frac{|I-{
 m mean\ income}|}{{
 m standard\ deviation\ of\ incomes}} \leq rac{|{
 m mean\ age}+2|}{{
 m standard\ deviation\ of\ ages}} \end{array}$
- None of the above.

Problem 6.4

Yet again, BruinCard, the company that gave us access to apps, small_apps, and mini_apps, has revoked our access to those three DataFrames and instead has given us micro_apps, an even smaller sample of apps.

Using micro_apps, we are again interested in finding the regression line that will allow us to predict the income of an applicant given their age. We are given the following information:

- The correlation coefficient, r, between ages and incomes is $-\frac{1}{3}$ (note the negative sign).
 The mean income is $\frac{7}{2}$ (remember, incomes are measured in tens of thousands of dollars).
- The mean age is 33.
- The regression line predicts that a 24 year old applicant has an income of $\frac{31}{2}$.

Suppose the standard deviation of incomes in micro_apps is an integer multiple of the standard deviation of ages in micro_apps. That is,

standard deviation of income = $k \cdot \text{standard}$ deviation of age.

What is the value of k? Give your answer as an **integer**.

Problem 7

Below, we define a new DataFrame called seven_apps and display it fully.

```
seven_apps = apps.sample(7).sort_values(by="dependents", ascending=False)
seven_apps
```

	status	age	income	homeowner	dependents
505	approved	52.16667	2.6600	yes	3
474	approved	39.00000	3.5000	yes	2
934	approved	22.25000	2.8000	yes	1
828	approved	21.41667	1.5896	no	0
970	approved	21.83333	2.0272	no	0
18	denied	35.58333	4.0000	no	0
784	approved	32.83333	2.5000	no	0

Consider the process of **resampling 7 rows from seven_apps with replacement**, and computing the maximum number of dependents in the resample.

Problem 7.1

If we take one resample, what is the probability that the maximum number of dependents in the resample is **less than** 3? Leave your answer **unsimplified**.

Click to view the solution.

Problem 7.2

If we take 50 resamples, what is the probability that the maximum number of dependents is **never** 3, in any resample? Leave your answer **unsimplified**.

Click to view the solution.

Problem 7.3

If we take 50 resamples, what is the probability that the maximum number of dependents is 3 in every resample? Leave your answer unsimplified.