

Winter 2024 Final Exam

Problem 9

Problem 9

In 2024, the Olympics will include breaking (also known as breakdancing) for the first time. The breaking competition will include **16 athletes**, who will compete in a single-elimination tournament.

In the first round, all 16 athletes will compete against an opponent in a face-to-face “battle”. The 8 winners, as determined by the judges, will move on to the next round. Elimination continues until the final round contains just 2 competitors, and the winner of this final battle wins the tournament.

The table below shows how many competitors participate in each round:

| Round | Competitors |
|-------|-------------|
| 1 | 16 |
| 2 | 8 |
| 3 | 4 |
| 4 | 2 |

After the 2024 Olympics, suppose we make a DataFrame called `breaking` containing information about the performance of each athlete during each round. `breaking` will have one row for each athlete’s performance in each round that they participated. Therefore, there will be $16 + 8 + 4 + 2 = 30$ rows in `breaking`.

In the `"name"` column of `breaking`, we will record the athlete’s name (which we’ll assume to be unique), and in the other columns we’ll record the judges’ scores in the categories on which the athletes will be judged (creativity, personality, technique, variety, performativity, and musicality).

Problem 9.1

How many rows of `breaking` correspond to the winner of the tournament? Give your answer as an integer.

Problem 9.2

How many athletes' names appear exactly twice in the `"name"` column of `breaking`? Give your answer as an integer.

Problem 9.3

If we merge `breaking` with itself on the `"name"` column, how many rows will the resulting DataFrame have? Give your answer as an integer.

Hint: Parts (a) and (b) of this question are relevant to part (c).

Problem 9.4

Recall that the number of competitors in each round is 16, 8, 4, 2. Write one line of code that evaluates to the array `np.array([16, 8, 4, 2])`. You **must use** `np.arange` in your solution, and you **may not use** `np.array` or the DataFrame `breaking`.

Winter 2025 Quiz 5

Problem 3

Question 3

UCSD uses a system called EASy for students to submit requests for enrollment if they need an exception to the enrollment requirements. Naturally, bigger classes generally receive more EASy requests.

Suppose the average number of seats per class (x) is 75, with a standard deviation of 25, and the average number of EASy requests per class (y) is 10, with a standard deviation of 4.

- a) For this subpart only, suppose the correlation between x and y is 0.5. Use the regression line to predict the number of EASy requests for a class with 100 seats. Give your answer as an **integer**.

- b) A Japanese class has 150 seats and receives 16 EASy requests. Say we use linear regression to predict the number of EASy requests from the number of seats, and find that the **squared** residual for this Japanese class is 4. What is the **smallest** possible correlation between x and y in this case? Give your answer as a **simplified fraction**.

Winter 2023 Final Exam

Problem 16

Problem 16

We collect data on the play times of 100 games of *Chutes and Ladders* (sometimes known as *Snakes and Ladders*) and want to use this data to perform a hypothesis test.

Problem 16.1

Which of the following pairs of hypotheses can we test using this data?

Option 1: **Null Hypothesis:** In a random sample of Chutes and Ladders games, the average play time is 30 minutes.

Alternative Hypothesis: In a random sample of Chutes and Ladders games, the average play time is not 30 minutes.

Option 2: **Null Hypothesis:** In a random sample of Chutes and Ladders games, the average play time is not 30 minutes.

Alternative Hypothesis: In a random sample of Chutes and Ladders games, the average play time is 30 minutes

Option 3: **Null Hypothesis:** A game of Chutes and Ladders takes, on average, 30 minutes to play. **Alternative**

Hypothesis: A game of Chutes and Ladders does not take, on average, 30 minutes to play.

Option 4: **Null Hypothesis:** A game of Chutes and Ladders does not take, on average, 30 minutes to play. **Alternative**

Hypothesis: A game of Chutes and Ladders takes, on average, 30 minutes to play.

☐ Option 1

☐ Option 2

☐ Option 3

☐ Option 4

Problem 16.2

We use our collected data to construct a 95% CLT-based confidence interval for the average play time of a game of *Chutes and Ladders*. This 95% confidence interval is [26.47, 28.47]. For the 100 games for which we collected data, what is the mean and standard deviation of the play times?

Problem 16.3

Does the CLT say that the distribution of play times of the 100 games is roughly normal?

☐ Yes

☐ No

Problem 16.4

Of the two hypotheses you selected in part (a), which one is better supported by the data?

☐ Null Hypothesis

☐ Alternative Hypothesis