

$$w_1(x^{(1)})^2 + w_2|x^{(1)}| + w_3(x^{(1)} + x^{(2)}) = H(\underline{x^{(1)}}_{}, \underline{x^{(2)}}_{})$$

← form of eqn changes matrix

$x^{(1)}$	$x^{(2)}$	y
1	2	5
3	6	0
4	1	1

$$\begin{bmatrix} 1 & 1 & 3 \\ 9 & 3 & 9 \\ 16 & 4 & 5 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \\ w_3 \end{bmatrix} = \begin{bmatrix} 5 \\ 0 \\ 1 \end{bmatrix}$$

X w

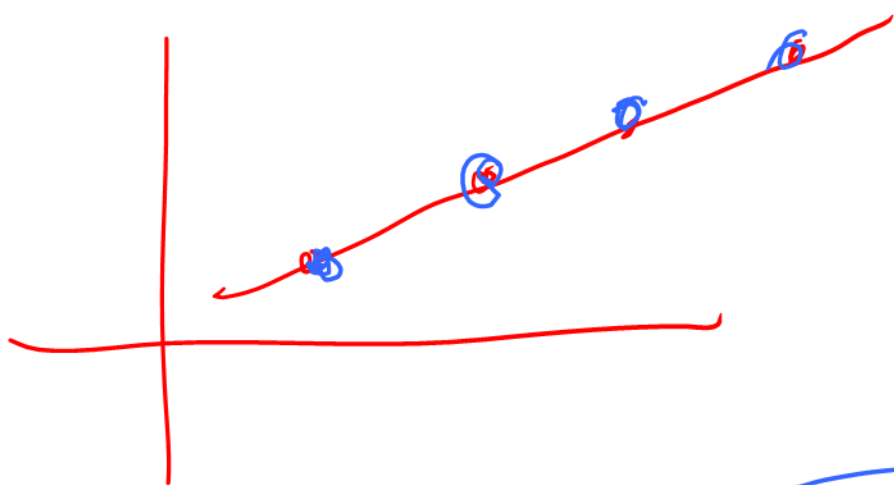
$$\begin{bmatrix} 5 \\ 0 \\ 1 \end{bmatrix}$$

y

$$\begin{bmatrix} H(x_1^{(1)}, x_1^{(2)}) \\ H(x_2^{(1)}, x_2^{(2)}) \\ H(x_3^{(1)}, x_3^{(2)}) \end{bmatrix}$$

← Xw is predictions

MSE is how different Xw are from y
 ideally, we'd have $Xw = y$



typically
 $X\vec{w} \approx \vec{y}$

$$\vec{0} \approx X\vec{w} - \vec{y}$$

$$\|\vec{v}\|^2 = v_1^2 + v_2^2 + \dots + v_{\# \text{comp.}}^2$$

$$(xw)_1 - y_1)^2 + ((xw)_2 - y_2)^2 + \dots = \|X\vec{w} - \vec{y}\|^2$$

the theory says^{to}

the way to minimize MSE is by solving normal eqns.

$$X^T X w = X^T y$$

$$\cancel{X}^T \cancel{X} w = \cancel{X}^T \cancel{y}$$

↑
parameters

let's pretend

$$w_1 = 7, w_2 = -3,$$

$$w_3 = 5$$

solves normal eqns

this means

$$7(x^{(1)})^2 - 3|x^{(1)}| + 5(x^{(1)} + x^{(2)})$$

has smaller MSE than
any other eqn of the
form $w_1(x^{(1)})^2 + w_2|x^{(1)}| + w_3(x^{(1)} + x^{(2)})$

which has smaller MSE,
the sol'n to
the normal eqns
where

$$X = \begin{bmatrix} 1 & 3 & 5 \\ 1 & 8 & 6 \\ 1 & 6 & 9 \\ 1 & 2 & 0 \end{bmatrix} \quad \text{or} \quad \text{plane}$$

$$H(x^{(1)}, x^{(2)}) = w_0 + w_1 x^{(1)} + w_2 x^{(2)}$$

$$X = \begin{bmatrix} 1 & 3 & 4 \\ 1 & 8 & 9 \\ 1 & 6 & 7 \\ 1 & 2 & 3 \end{bmatrix}$$

$$H(x^{(1)}, x^{(2)}) = w_0 + w_1 x^{(1)} + w_2 x^{(2)}$$


where $x^{(2)} = x^{(1)} + 1$
 (plug in for $x^{(2)}$)

$$H(x^{(1)}, x^{(2)}) = w_0 + w_1 x^{(1)} + w_2 (x^{(1)} + 1)$$

line

$$y = w_0 + w_1 x$$

parabola

$$y = w_0 + w_1 x + w_2 x^2$$


$$= w_0 + w_1 x^{(1)} + w_2 x^{(2)} + w_2$$

$$= (w_0 + w_2) + (w_1 + w_2) x^{(1)}$$

line

$$= C_0 + C_1 x^{(1)}$$

Counting/ Prob.

52 cards, 13 in each
of 4 suits ($\heartsuit, \diamondsuit, \clubsuit, \spadesuit$)

someone deals you a
hand of 5 random cards

$$P(\text{all } \heartsuit\text{s}) = \frac{13}{52} \times \frac{12}{51} \times \frac{11}{50} \times \frac{10}{49} \times \frac{9}{48}$$

$$= \frac{P(13, 5)}{P(52, 5)}$$

sequences
of
5 cards

$$= \frac{C(13, 5)}{C(52, 5)}$$

sets
of
5 cards

$P(\text{all 5 cards have distinct values}) =$

$$1 \times \frac{48}{51} \times \frac{44}{50} \times \dots$$

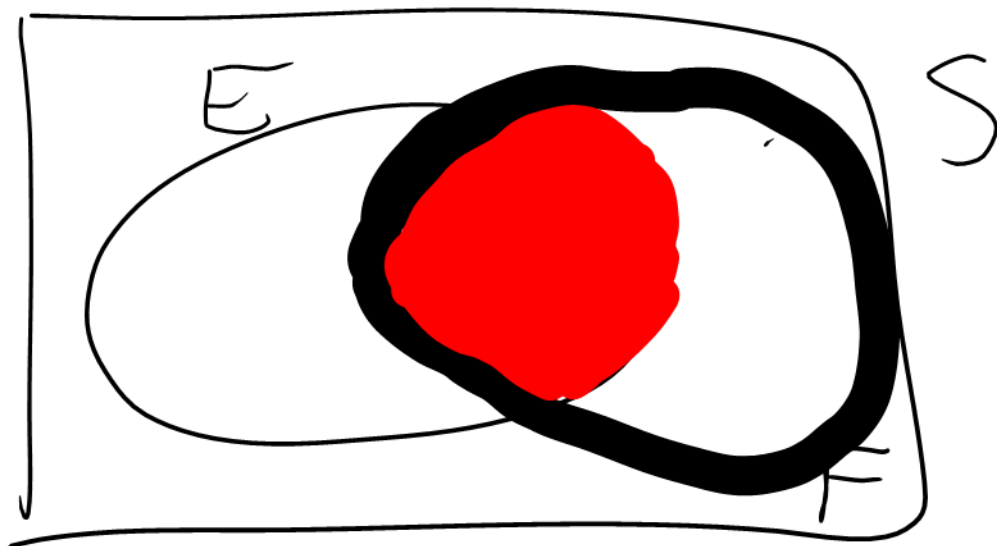
say K
not K ,
say 7
not K ,
not 7

$P(\text{all 5 cards have distinct values} \mid \text{all } \heartsuit)$

15

$$= 1$$

$$P(E|F) = \frac{P(E \cap F)}{P(F)}$$



$$P(\text{no } \heartsuit) = \frac{C(39, 5)}{C(52, 5)}$$

sets
of
5
cards

$$P(\text{all } \heartsuit) \neq 1 - P(\text{no } \heartsuit)$$

$$P(\text{at least } 1 \heartsuit) = 1 - P(\text{no } \heartsuit)$$

$$P(\text{all } \heartsuit) \cup (\text{exactly } 1 K)$$

$$P_{\text{prob}}(\text{all } \heartsuit) + P_{\text{prob}}(\text{exactly } 1 K) - P_{\text{prob}}(\text{all } \heartsuit \text{ and exactly one } K)$$

$$\frac{P(13, 5)}{P(52, 5)} + \frac{\overset{\text{pos. suit}}{5 \cdot 4 \cdot P(48, 4)}}{P(52, 5)} - \frac{5 \cdot P(12, 4)}{P(52, 5)}$$



