${\bf Midterm~2 - DSC~40A,~Spring~2023}$

Instructions

- This is a 50-minute exam consisting of 6 questions worth a total of 32 points.
- You may use any number of handwritten note sheets, and no other resources.
- No calculators.
- Please write neatly and stay within the provided boxes.
- You may fill out the **front page only** until you are instructed to start.
- Leave all answers unsimplified in terms of permutations, combinations, factorials, exponents, etc.
- You do not need to show your work or provide justification, unless a problem specifically asks you to.

Statement of Academic Integrity

By submitting your exam, you are attesting to the following statement of academic integrity.

I will act with honesty and integrity during this exam.

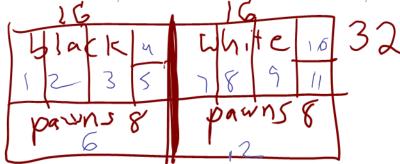
Name:		Solutions	
PID:		A12345678	
Seat you are in:			
Lecture Section:	○ A00 (10-10:50AM)	○ B00 (11-11:50AM)	

Version - A

② Chess Pieces 響

A set of chess pieces has 32 pieces. 16 of these are black, and 16 of these are white. In each color, the 16 pieces are

- 8 pawns,
- 2 bishops,
- 2 knights,
- 2 rooks,
- 1 queen, and
- 1 king.



When there are multiple pieces of a given color and type (for example, 8 white pawns), we will assume they are indistinguishable from one another.

(3 points). Censider an experiment where each of n people selects one piece from their own set of 32 chess pieces uniformly at random. The result of the experiment is a description of the colors and pieces each person selected. For example, if n = 3, one possible result is:

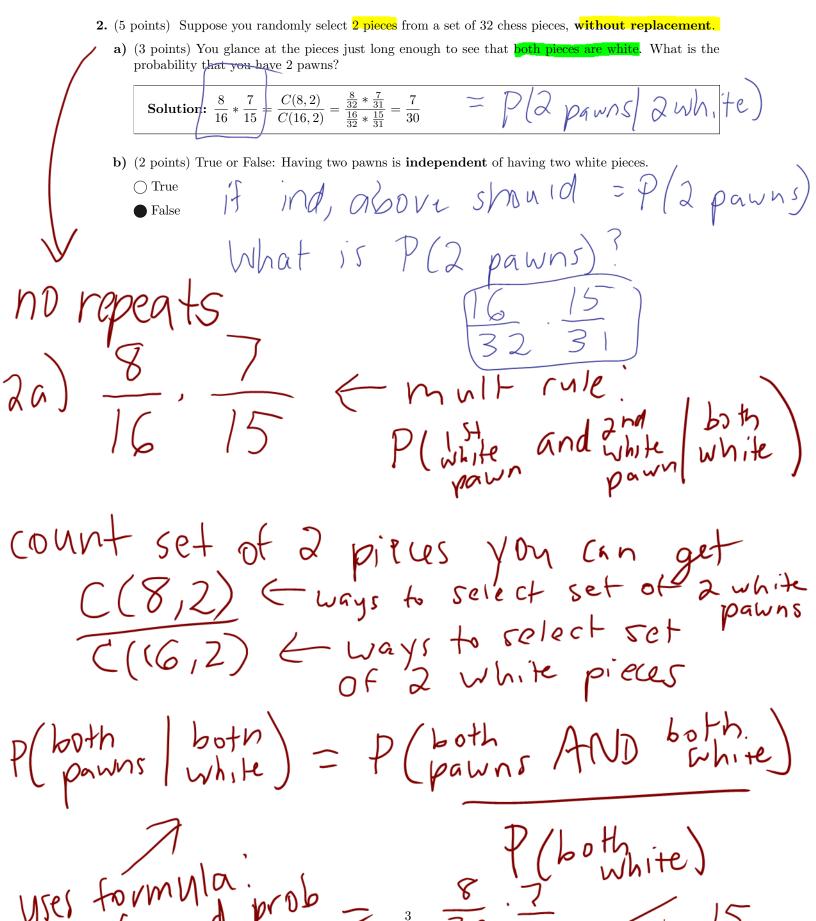
- Person 1 selected a white knight.
- Person 2 selected a black queen.
- Person 3 selected a black pawn.

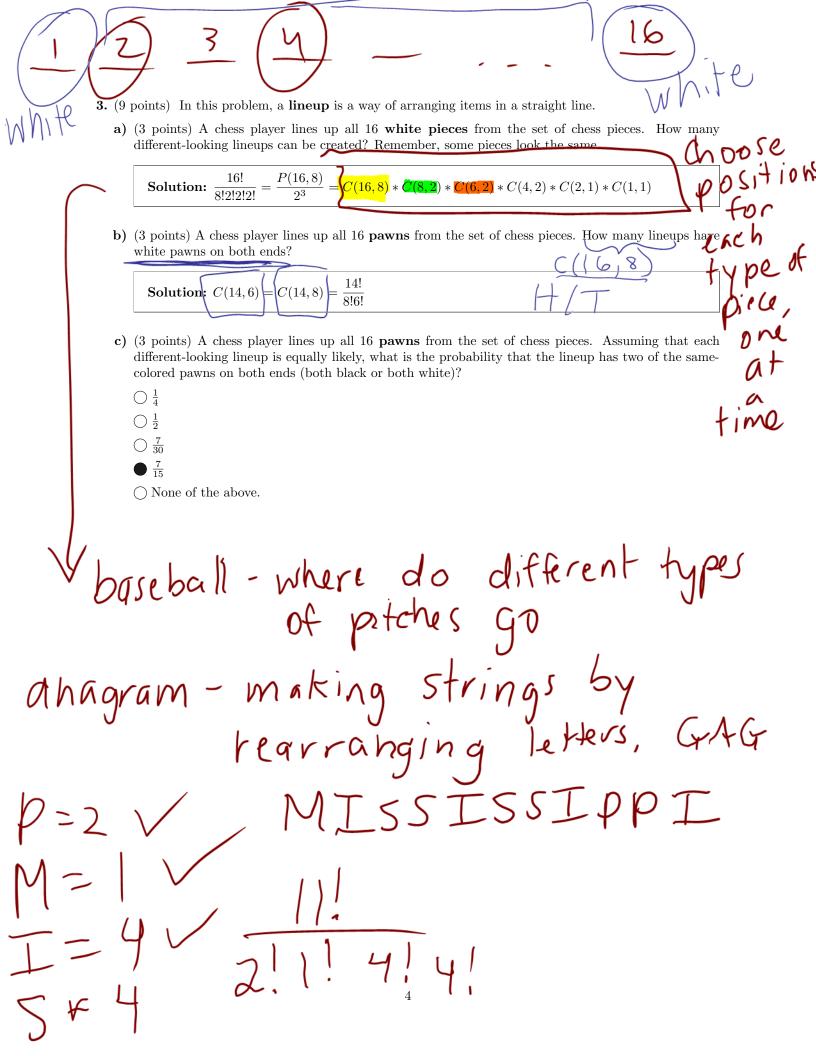
How many results are possible for this experiment with n people?

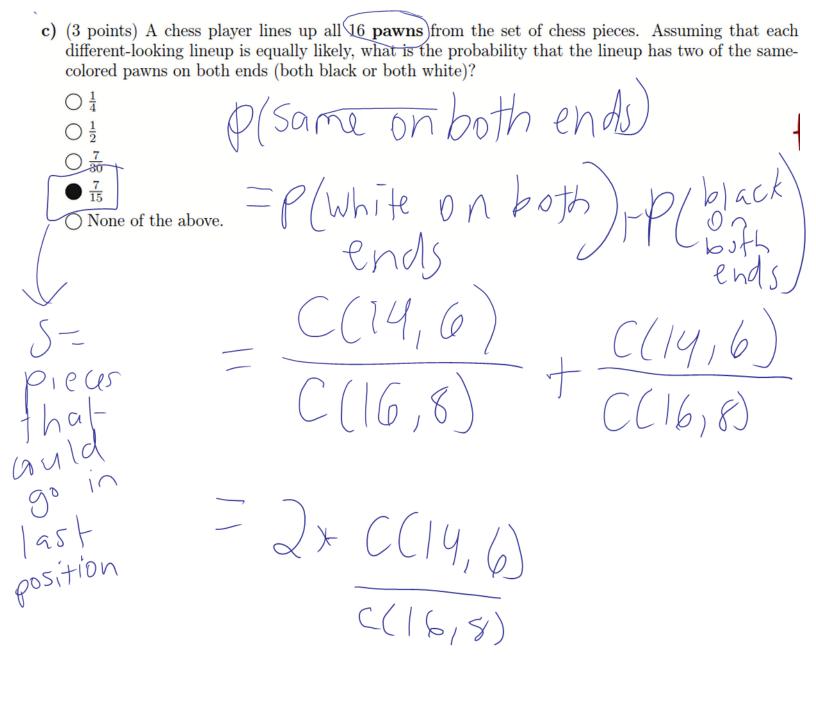
- $\bigcirc 2^n$
- $\bigcirc 6^n$
- 12^{n}
- $\bigcirc 16^n$
- $\bigcirc 32^n$
- O None of the above.

replacement, can be duplicated

2







90 P (beat Avi bear) = 0.1
4. (6 points) Suppose that there are three possible experience levels in these (beginner, intermediate, advanced). Only 10% of beginner players beat Avi at a game of chess, while 50% of intermediate players
and 80% of advanced players do. 5 o Avi signs up to participate in a certain chess tournament called the Avocado Cup. Aside from Avi, 50% of the players in the tournament are beginners, 40% are intermediate, and 10% are advanced.
The tournament proceeds in rounds. In the first round of the tournament, players are randomly paired up for a game of chess.
a) (3 points) What is the probability that Avi wins in the first round of the tournament?
0.33% $0.50%$ $0.50%$
● 67%
\bigcirc 83% \bigcirc None of the above.
(3 points) It turns out that, sadly, Avi loses to his opponent in the first round. What is the probability that Avi's opponent is an advanced player? Choose the closest answer among the choices listed.
015% P(adv/beat Avi) = P(adv). P(beat Avi
0 35% to Cheat.
045% 50% 90% 10% PLDCAVI
beg int gall
$ \left \left \left \right \right = 0.00 $
0.3
t Leat Avi

P(beg) = (0.5) + P(beg) + (0.1)
P(int) = 0.4 P(beat lint) = 0.5
p(adv)=0.D+ P(beat adv)=0.8
0.05102010000000000000000000000000000000
0.05+0.20+0.08=0.33 = P(beat Avi)

5. (3 points) You have a large historical dataset of all competitors in past years of the Avocado Cup chess tournament. Each year, hundreds of chess players compete in the tournament, and one person is crowned the winner. For each competitor in each year of the competition's history, you have information on their

- experience level (beginner, intermediate, advanced),
- birth month (January through December), and
- whether they won the tournament that year (yes or no).

Assume that birthdays of competitors are evenly distributed throughout the months.

You want to predict who will win this year's Avocado Cup. To do so, you use this historical data to train a Naive Bayes classifier and classify each competitor as a winner or non-winner, given their experience level and birth month. Which of the following reasons best explains **why your classifier is ineffective** in identifying the winner?

O Because it uses a variable (birth month) that likely has nothing to do with a person's chances of winning the tournament.

O Because it uses a variable (experience level) that likely has a strong connection with a person's chances of winning the tournament.

- Because it uses a dataset where there are many more non-winners than winners.
- O Because it uses a categorical response variable.

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6. (6 points) The Avocado Cup is organized into rounds. In each round, players who win advance to the next round, and players who lose are eliminated. Rounds continue on like this until there is a single tournament winner.

Define the following events in the sample space of possible outcomes of the Avocado Cup:

- A = Avi loses in the first round.
- B = Avi wins the tournament.
- C = Avi wins in the first round.
- a) (3 points) Which of the following statements is true? Select all that apply.
 - \nearrow A and B are independent.
 - \blacksquare A and B are conditionally independent given C.
 - A, B, and C form a partition of the sample space.
 - None of the above.
- b) (3 points) The events A and B are mutually exclusive, or disjoint. More generally, for **any** two disjoint events A and B, show how to express $P(\overline{A}|(A \cup B))$ in terms of P(A) and P(B) **only**. For this problem only, show your work and justify each step.

Solution:

A

C

B

P(AIB) | C) = P(A|C) + P(B|C) + Nonzero

(3 points) The events A and B are mutually exclusive, or disjoint. More generally, for **any** two disjoint events A and B, show how to express $P(\overline{A}|(A \cup B))$ in terms of P(A) and P(B) **only**. For this problem only, **show your work and justify each step.**

p (striped (green) - Plstriped and green) Placon What fraction of green What fraction of AUB is not P(A (AUB)) Otherson. P(AUB) - Complement (A) + P(B)