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## DSC 40B - Homework 08

Due: Wednesday, March 8

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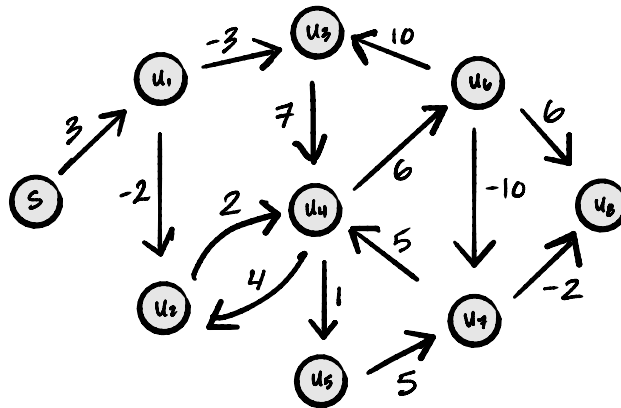
Write your solutions to the following problems by either typing them up or handwriting them on another piece of paper. Unless otherwise noted by the problem's instructions, show your work or provide some justification for your answer. Homeworks are due via Gradescope at 11:59 p.m.

**Note!** Because the midterm is on Thursday, we would like to release the solutions to this homework immediately after the due date on Wednesday at midnight. Since this is before the late due date, we **cannot accept slip days for this homework**.

### Problem 1.

Run Bellman-Ford on the following graph using node  $s$  as the source. Below each node  $u$ , write the shortest path length from  $s$  to  $u$ . Mark the predecessor of  $u$  by highlighting it or making a bold arrow. You can assume that `graph.edges` produces the graph's edges in the following order:

$(u_2, u_4), (u_7, u_8), (u_6, u_3), (s, u_1), (u_1, u_2), (u_4, u_5), (u_1, u_3),$   
 $(u_3, u_4), (u_6, u_7), (u_4, u_6), (u_5, u_7), (u_7, u_4), (u_4, u_2), (u_6, u_8)$

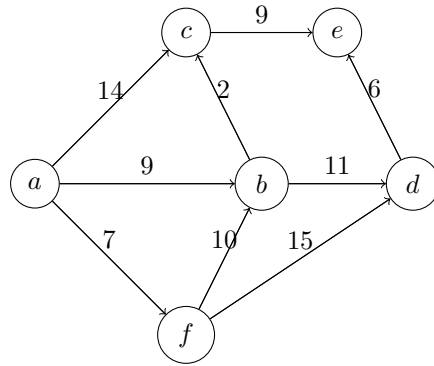


### Problem 2.

Recall that the Bellman-Ford algorithm (with early stopping) will terminate early if, after updating every edge, no predecessors have changed. Suppose it is known that the greatest shortest path distance in a graph  $G = (V, E)$  has  $\Theta(\sqrt{V})$  edges. What is the worst case time complexity of Bellman-Ford when run on this graph? State your answer using  $\Theta$  notation.

### Problem 3.

Run Dijkstra's Algorithm on the following graph using node  $a$  as the source. Below each node  $u$ , write the shortest path length from  $a$  to  $u$ . Mark the predecessor of  $u$  by highlighting it or making a bold arrow.



**Problem 4.**

True or False. Suppose  $G = (V, E, \omega)$  is a weighted graph for which all edges are positive, except for those edges of a node  $s$  which may or may not be negative. If Dijkstra's algorithm is run on  $G$  with  $s$  as the source, the correct shortest paths will be found. Assume that the graph does not have any negative loops. Justify your answer.