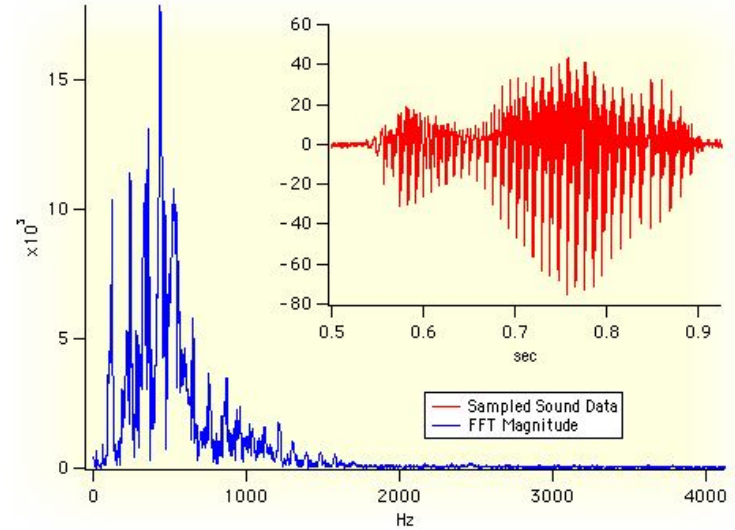


Without The Fluff: Deep Learning

Fourier Transforms



Fourier transform and inverse Fourier transform, respectively (Krantz 1999, p. 202).

Note that some authors (especially physicists) prefer to write the transform in terms of angular frequency ω , which destroys the symmetry, resulting in the transform pair

$$\begin{aligned} H(\omega) &= \mathcal{F}[h(t)] \\ &= \int_{-\infty}^{\infty} h(t) e^{-i\omega t} dt \\ h(t) &= \mathcal{F}^{-1}[H(\omega)] \\ &= \frac{1}{2\pi} \int_{-\infty}^{\infty} H(\omega) e^{i\omega t} d\omega. \end{aligned}$$

To restore the symmetry of the transforms, the convention

$$\begin{aligned} g(y) &= \mathcal{F}[f(t)] \\ &= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(t) e^{-iyt} dt \\ f(t) &= \mathcal{F}^{-1}[g(y)] \\ &= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} g(y) e^{iyt} dy \end{aligned}$$

is sometimes used (Mathews and Walker 1970, p. 102).

In general, the Fourier transform pair may be defined using two arbitrary constants a and b as

$$\begin{aligned} F(\omega) &= \sqrt{\frac{|b|}{(2\pi)^{1-a}}} \int_{-\infty}^{\infty} f(t) e^{ib\omega t} dt \\ f(t) &= \sqrt{\frac{|b|}{(2\pi)^{1+a}}} \int_{-\infty}^{\infty} F(\omega) e^{-ib\omega t} d\omega. \end{aligned}$$



what are this



**Let's look at an
example.**

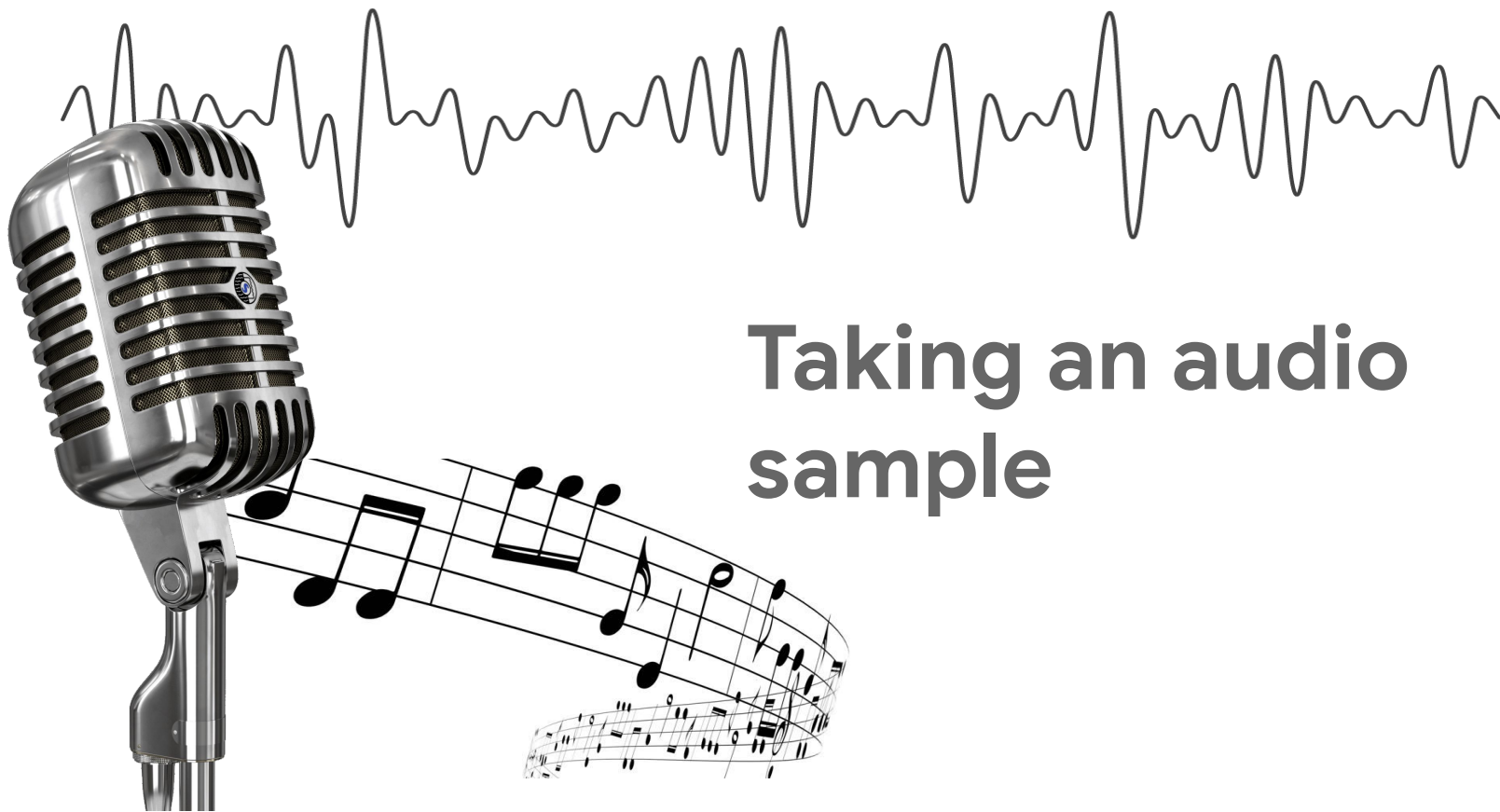




**Say you have a
smoothie.**

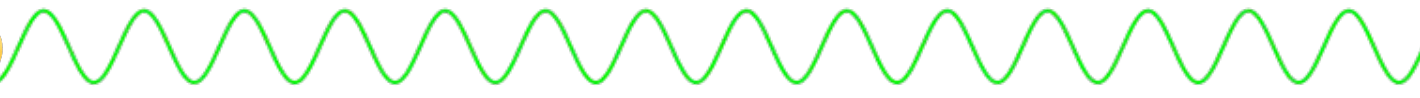






Taking an audio sample





What is AI?

A large blue shape on the left side of the slide, consisting of a vertical rectangle with a rounded right edge.

Artificial Intelligence

Any technique that enables
computers to mimic human behavior





Artificial Intelligence

Any technique that enables computers to mimic human behavior

Machine Learning

Ability to learn without being explicitly programmed





Artificial Intelligence

Any technique that enables computers to mimic human behavior

Machine Learning

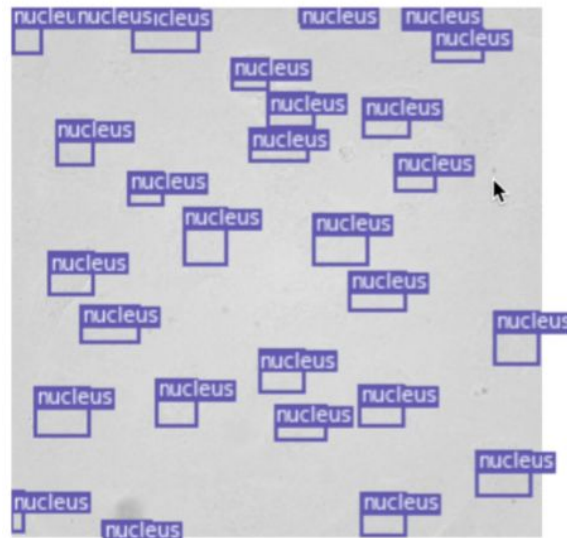
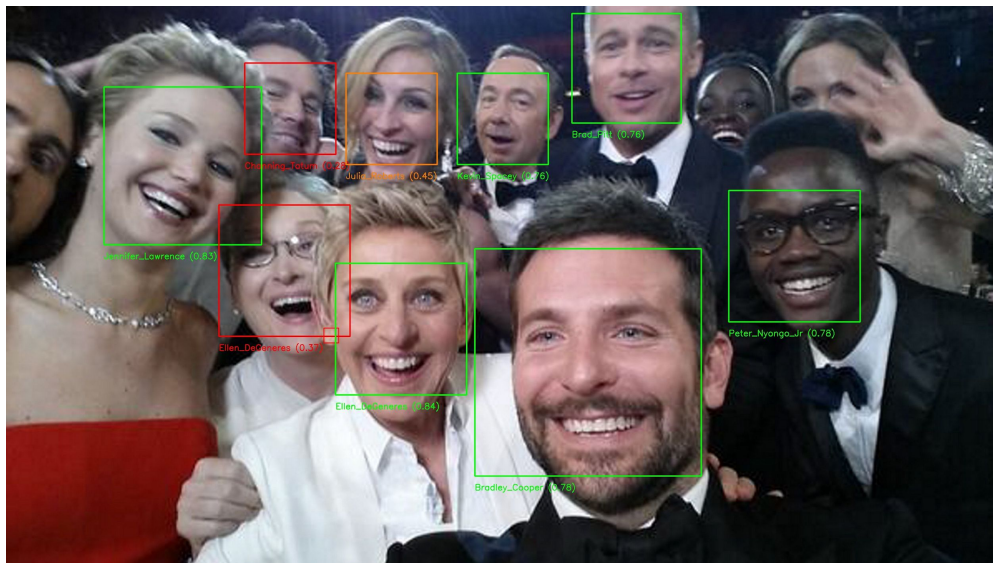
Ability to learn without being explicitly programmed

Deep Learning

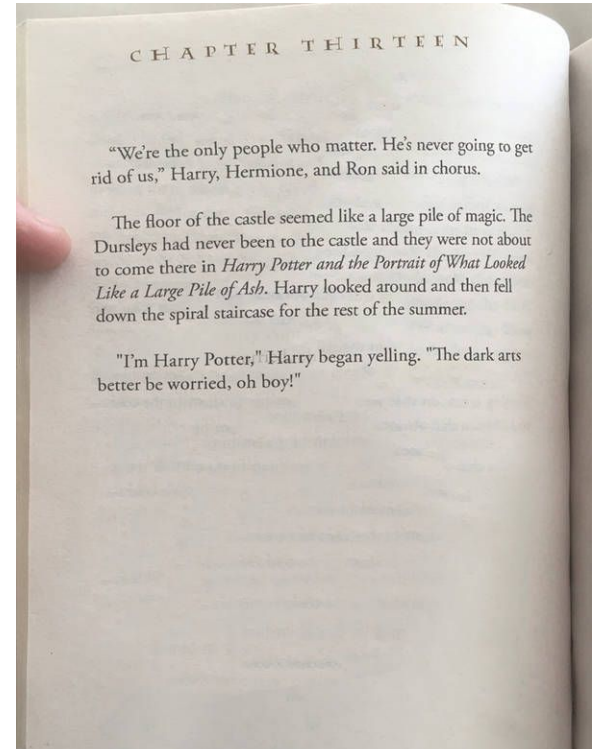
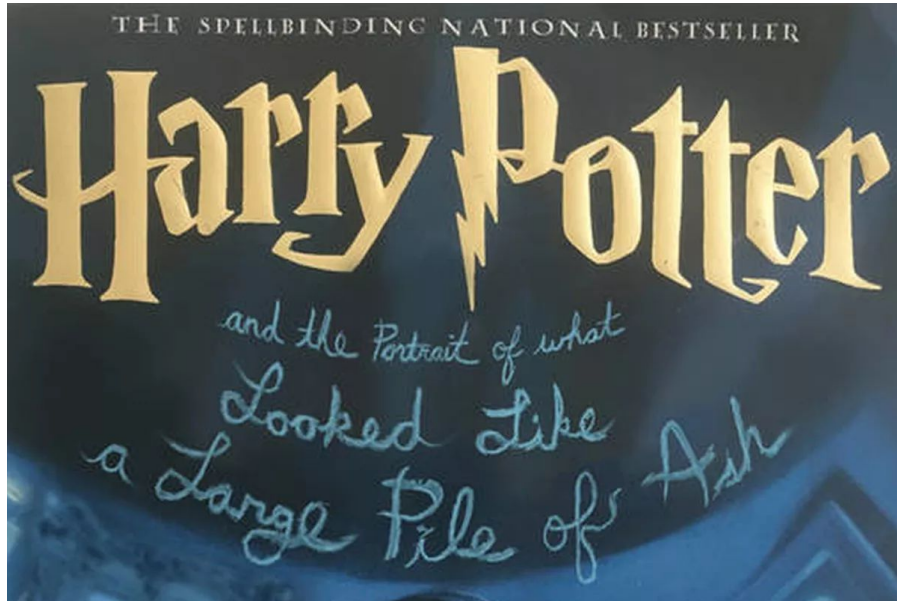
Learn underlying features in data by using neural networks



Images

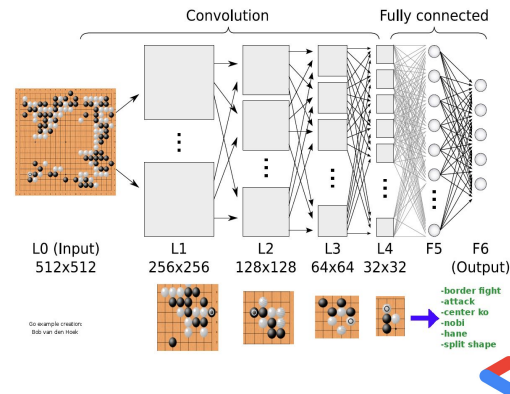
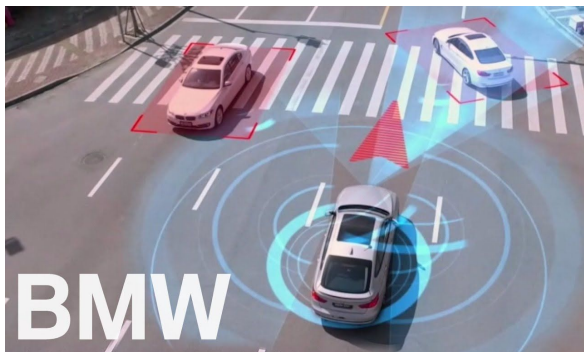


Text





And a whole lot more.



**Let's try an
example.**



Imagine you work at a cheese factory

Your manager wants you to predict cheddar cheese quality based on data you've obtained from factory sensors.

- Acetic Acid
- H_2S
- Lactic Acid
- Taste



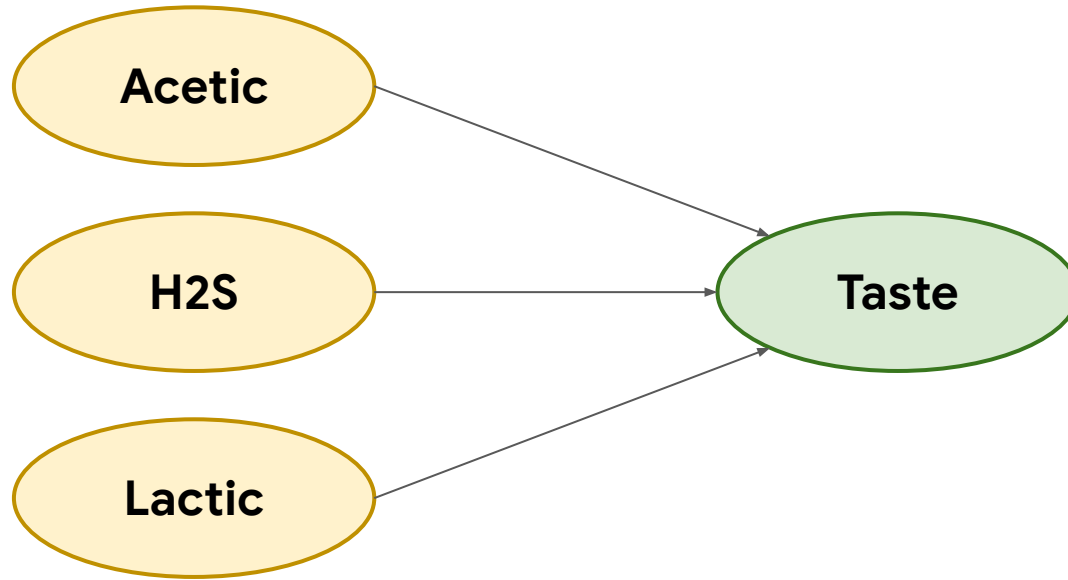
Data: Cheddar Cheese Quality

Description: Concentrations of acetic acid, H₂S, and lactic acid in 30 records of mature cheddar cheese. A subjective taste value is also provided.

Acetic	H ₂ S	Lactic	Taste
4.543	3.135	0.86	12.3
5.159	5.043	1.53	11.7
5.366	5.438	1.57	12.1
5.759	3.807	0.99	7.8



Example: Linear Regression



Deep Learning: Interaction Effects

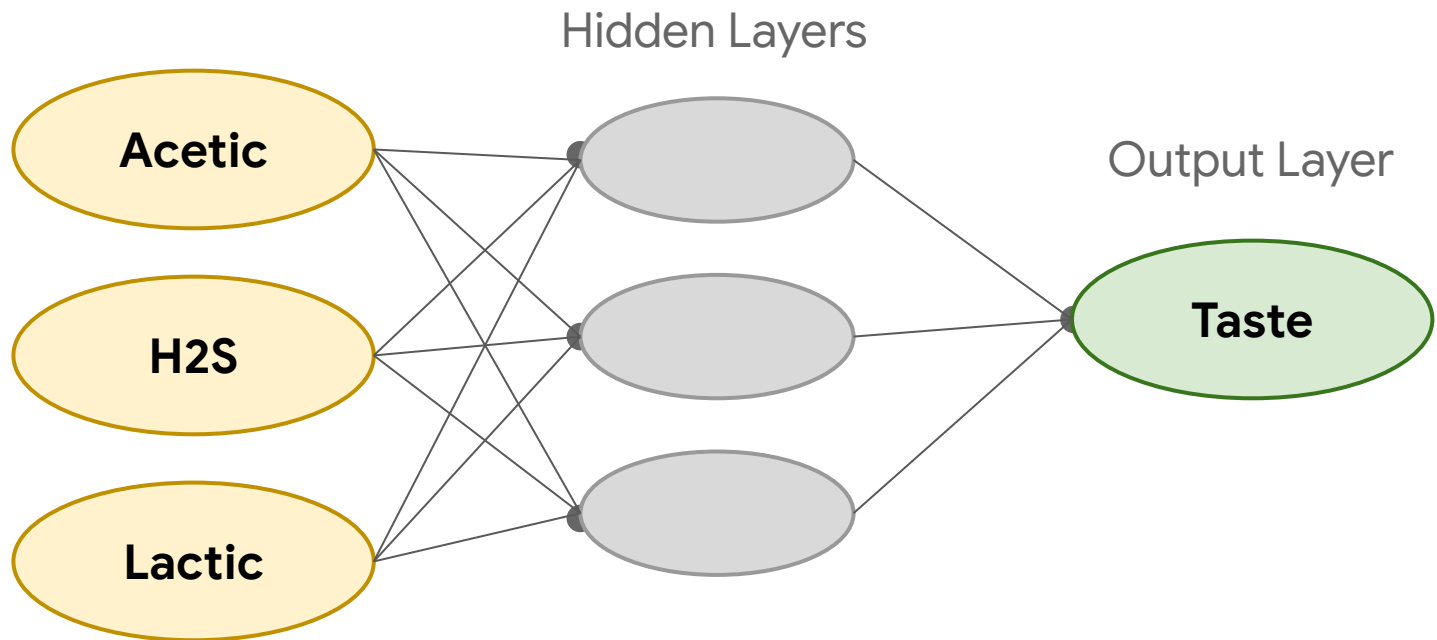
Neural networks are extremely good at dealing with high dimensional data.

Deep Learning = many layers of nodes

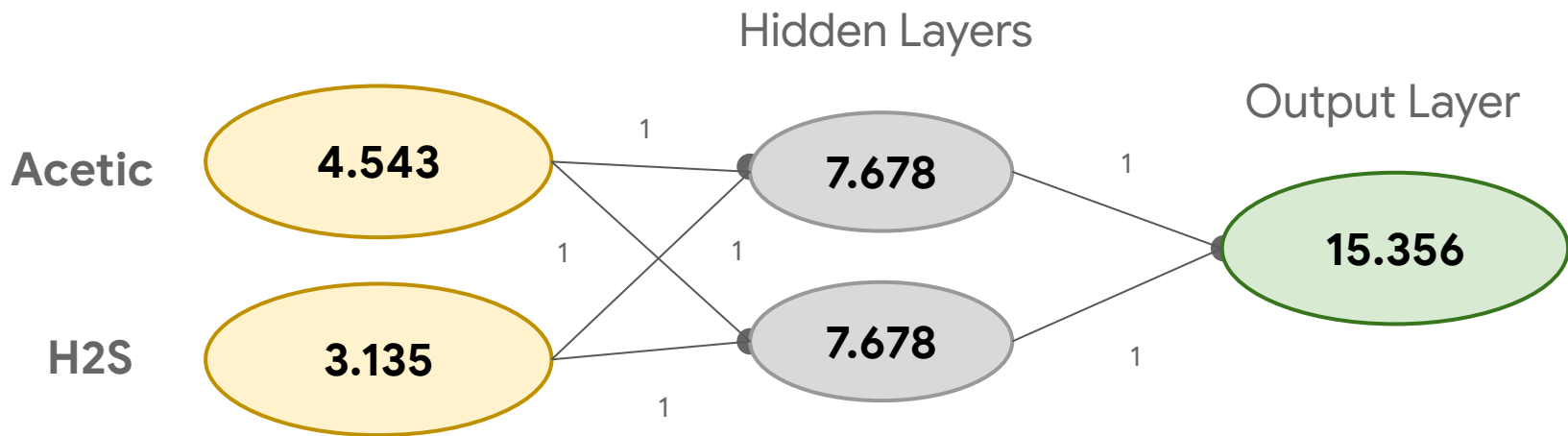
- Forward propagation
- Back propagation
- Gradient descent



Capturing Interactions: Hidden Layers



Let's try it: Forward Propagation



$$(4.543 \times 1) + (3.135 \times 1) = 7.678$$

$$(7.678 \times 1) + (7.678 \times 1) = 15.356$$



Code

```
import numpy as np

input_data = np.array([4.543, 3.135])
weights = { '0': np.array([1, 1]),
            '1': np.array([1, 1]),
            '2': np.array([1, 1])}

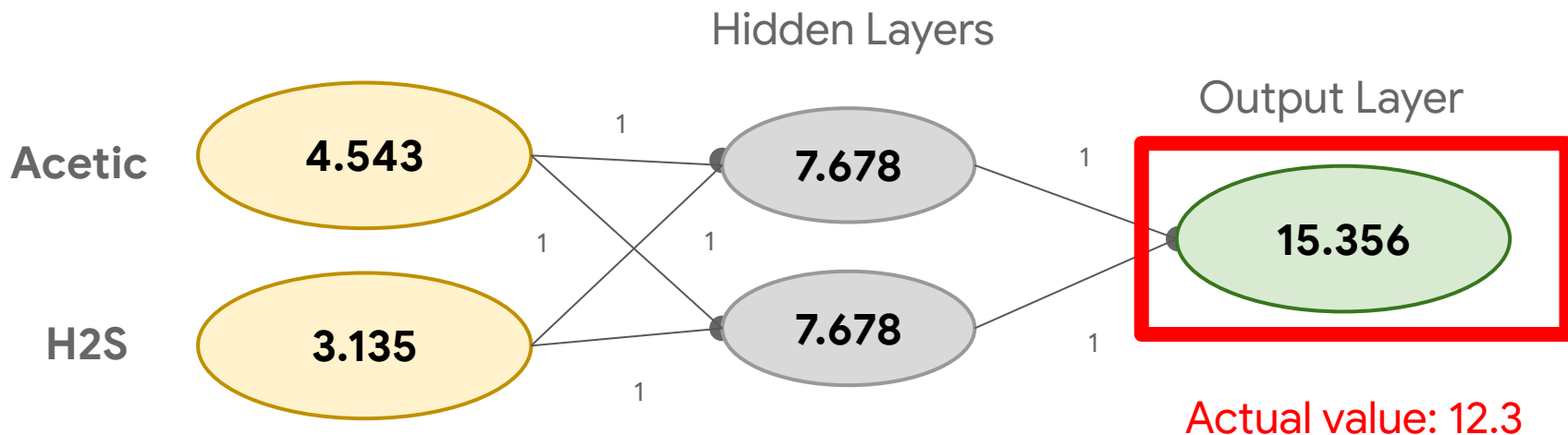
node_0 = (input_data) * weights['0'].sum()
node_1 = (input_data) * weights['1'].sum()

hidden_layer = np.array([node_0, node_1])
print(hidden_layer)

output = (hidden_layer * weights['2']).sum()
print(output)
```



Let's try it: Forward Propagation



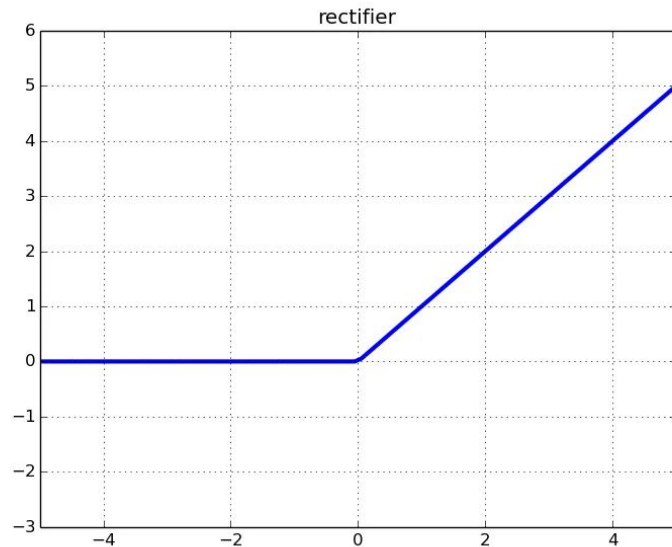
$$(4.543 \times 1) + (3.135 \times 1) = 7.678$$

$$(7.678 \times 1) + (7.678 \times 1) = 15.356$$



Activation functions: Improving models

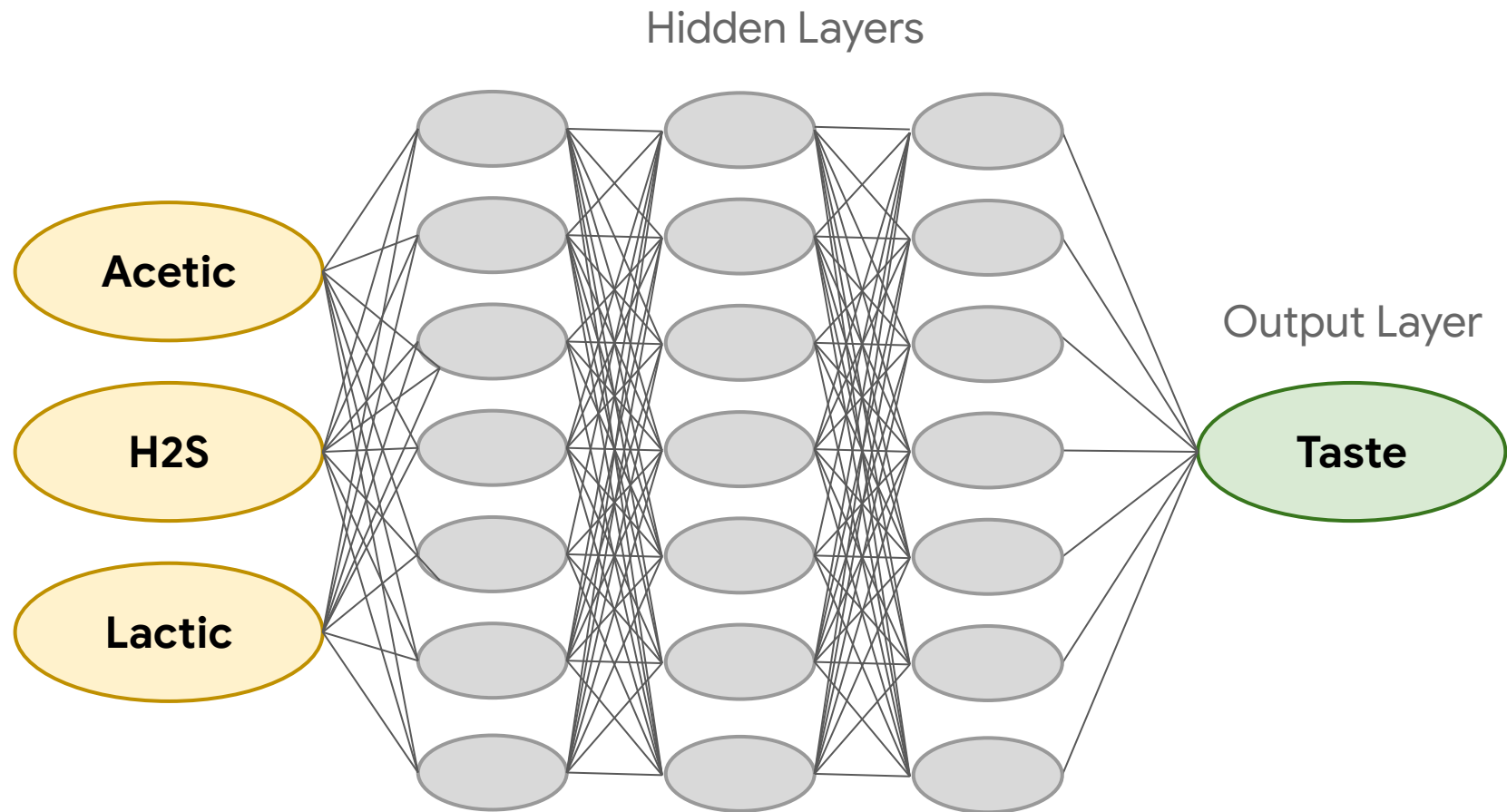
- Applied to node input to produce a node output
`relu(4.543 * 1 + 3.135 * 1)`
- Current industry standard is the *Rectified Linear Activation (ReLU)*

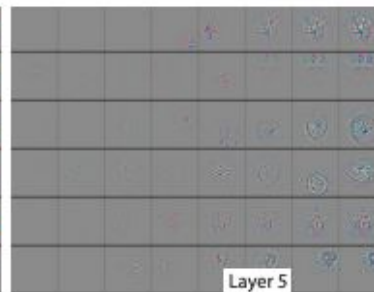
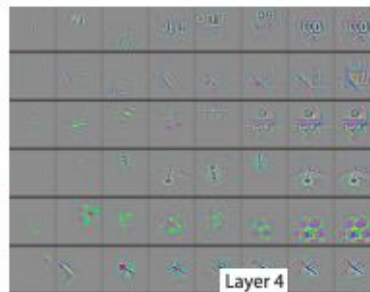
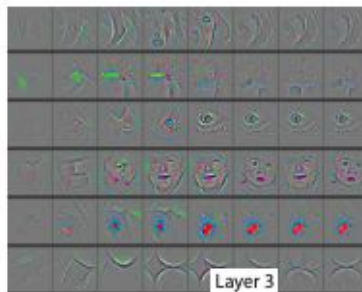
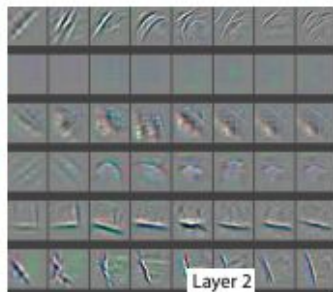
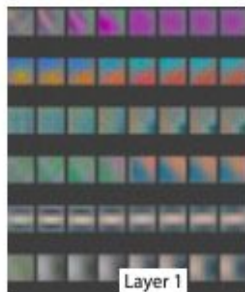
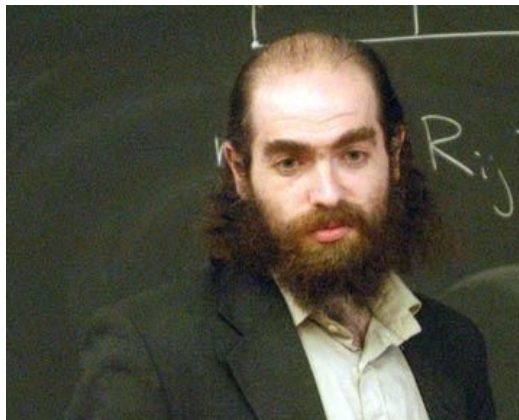


Where predicting gets tricky

- This a reduced-dimensionality example for a *single record*. The more features and records you add, this harder this process gets.
- At every set of weights, there are *many values* of the error.



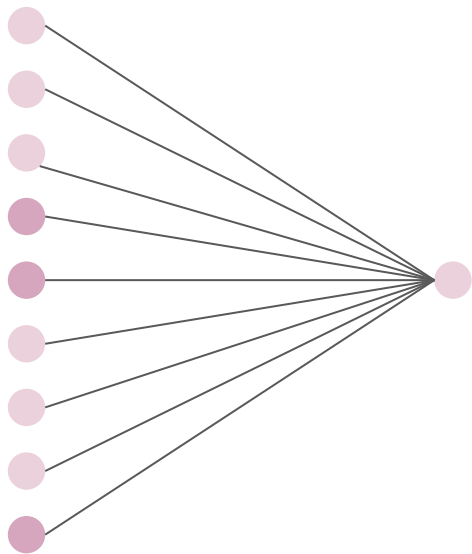




zeiler and fergus (2013)



For every single node:



$$= \sigma(w_1 a_1 + w_2 a_2 + \dots + w_n a_n + b)$$

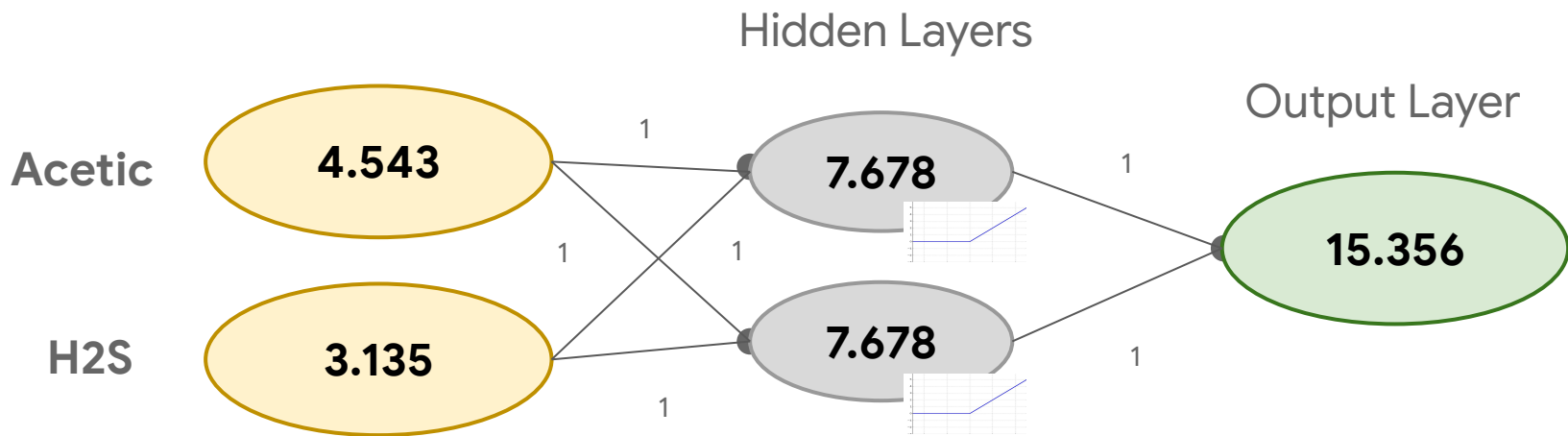
σ = activation function

w = weights

b = bias



Let's try it: Forward Propagation



$$(4.543 \times 1) + \text{relu}(3.135 \times 1) = 7.678$$

$$(7.678 \times 1) + \text{relu}(7.678 \times 1) = 15.356$$



Tinker With a **Neural Network** Right Here in Your Browser.

Don't Worry, You Can't Break It. We Promise.



Epoch
000,000

Learning rate

0.03

Activation

Tanh

Regularization

None

Regularization rate

0

Problem type

Classification

DATA

Which dataset do you want to use?



Ratio of training to test data: 50%



Noise: 0



Batch size: 10



REGENERATE

FEATURES

Which properties do you want to feed in?



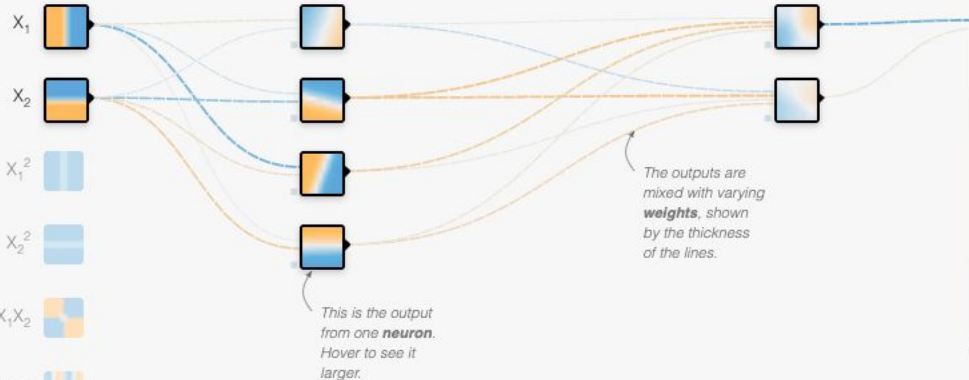
+ - 2 HIDDEN LAYERS



4 neurons



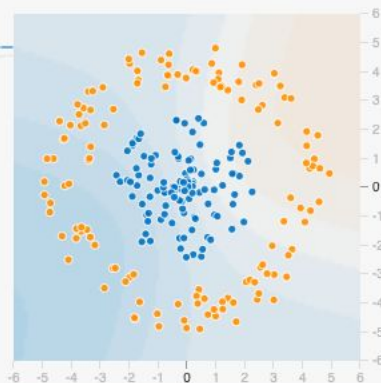
2 neurons



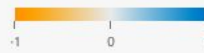
OUTPUT

Test loss 0.521

Training loss 0.516



Colors shows data, neuron and weight values.



Resources

- A Student's Guide to Maxwell's Equations
- Visualizing and Understanding Convolutional Networks
(Zeiler and Fergus, 2013)
- TensorFlow Playground



Thank you!