## Observation of turbulent intermittency scaling with magnetic helicity in an MHD plasma wind-tunnel

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The intermittency in turbulent magnetic field fluctuations has been observed to scale with the amount of magnetic helicity injected into an experimental flux rope plasma. A selectively decayed Taylor state is created in the wind-tunnel configuration of the Swarthmore Spheromak Experiment. The level of intermittency is determined by finding the flatness of the probability distribution function of increments for magnetic pickup coil fluctuations,  $\dot{B}(t)$ . The intermittency increases with the injected helicity but spectral indices of the spectra is unaffected by this variation. Evidence for the role of current sheets and reconnection sites in the generation of this intermittency is provided, but the true nature of the observed intermittency remains unknown.

Varying levels of intermittency [1] in magnetic fluctuations have been observed in many different turbulent plasmas in both space and laboratory settings. Differences in magnetic intermittent character have been seen between fast and slow solar wind turbulence [2], at varying spatial scales in the solar wind [3], and between different confinement regimes in laboratory experiments, particular in reverse field pinches [4, 5]. Simulation generated intermittency in MHD turbulence [6–9] compared with in situ measurements in the solar wind has suggested a link between such non-Gaussian fluctuations and the presence of current sheets or reconnection layers [10, 11]. Since magnetic helicity of a plasma is reflective of the twistedness or knottedness of the magnetic field, a scan of magnetic helicity can be used to vary the magnetic field structure and potentially modify the character of current sheets in the plasma. A novel experiment was developed on the MHD wind-tunnel configuration of the Swarthmore Spheromak Experiment (SSX) [12, 13] to explore this possible relationship between the observed intermittency in magnetic fluctuations and the magnetic helicity of the plasma. Given the nature of the plasma source on SSX, magnetic helicity injection can be very finely controlled and thus resulting changes in turbulent characteristics—including both spectra and intermittency—can be carefully examined.

This paper presents the results of an experimental scan which establishes a connection between a controllable experimental quantity—magnetic helicity—and a turbulent characteristic—intermittency. As the amount of injected magnetic helicity is increased, the measured flatness or kurtosis of the probability distribution function of fluctuations in a magnetic pickup coil,  $dB/dt = \dot{B}(t)$ , are also shown to increase ranging from near Gaussian (F $\sim$  5) to values of F > 30. In contrast, the power-law behavior of the frequency spectra of these fluctuations are shown to be unaffected by this variation in helicity as shown by the power-law fit spectral indices. The scan is conducted on the wind-tunnel configuration of the Swarthmore Spheromak Experiment which consists of an 86cm

long by 15.5cm wide cylindrical copper flux conserver into which a plasma gun injects dense, highly magnetized ( $\sim 1 \times 10^{15} cm^{-3}$ ,  $\sim 5kG$ ) spheromak-shaped plasma that self-organizes by tilting and twisting into a Taylor state [12, 14, 15]. There is no guide or vacuum field in the chamber so the magnetic field embedded in the plasma is completely dynamical.

The injection of magnetic helicity into the plasma is a natural consequence of the formation procedure for a plasma gun. Magnetic helicity,

$$K_B = \int A \cdot BdV \tag{1}$$

is a measure of the amount of twistedness of the magnetic field lines and can be expressed in terms of square magnetic flux units (i.e. units of  $Wb^2$ ). This quantity can be recast in a more experimentally relevant quantity,

$$K_B = \int \Phi V_{gun} dt \tag{2}$$

where  $\Phi$  is the magnetic flux penetrating the plasma gun core and  $V_{gun}$  is the voltage drop across the gun gap. This is the form of the helicity that is calculated and reported in this paper. Since the plasma forms under the assumption of selective decay (conservation of magnetic helicity) [12], it is further assumed that the amount of helicity injected by the gun is conserved and present in the plasma under observation. Though the voltage across the gun gap is recorded for the entire duration of the shot, only the first  $20\mu s$  after initial trigger of the capacitor banks and breakdown of the hydrogen gas are used to estimate the injected helicity. Beyond  $20\mu s$ , the voltage measurement is significantly affected by breaking field lines during spheromak formation.

The gun voltage is set by a combination of the gun circuit and breakdown physics, but typically does not vary given a particular capacitor charge setting and gas input delay time. Thus, by Eqn. 2, the injected helicity is modified by the amount of magnetic flux penetrating the gun core. The flux can be ranged from 0.0 to 1.5mWb

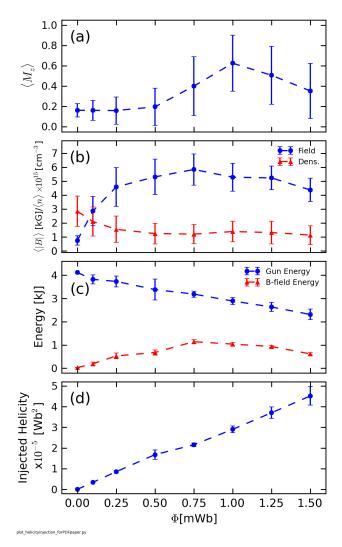


FIG. 1. (a)Mach probe axial edge Mach number (b) magnetic field magnitude (in blue) and HeNe interferometer measured line-integrated density (in red) averaged over the analysis period of  $40\text{-}60\mu s$ ,(c) injected gun energy and volume integrated magnetic field energy, and (d) amount of helicity injected in the first  $20\mu s$  after discharge trigger as a function of magnetic flux in gun core. Error bars for all four plots indicate the standard deviation in values of magnetic field and potential (and propagated into energy and helicity) over the time range and shot number.

which, given a gun voltage of approximately 900V, yields an injected helicity range of 0 to  $5\times10^{-5}Wb^2$ .

As indicated in Figure 1(d), the injected helicity scales linearly with the varied magnetic flux. Figures 1(a) and (b) show how the average bulk plasma features vary throughout the scan for the primary analysis period of  $40-60\mu s$ : the average magnetic field at the center of the chamber grows initially with flux, but saturates around 5kG. The average density drops initially, before saturating at about  $1\times10^{15}$  cm<sup>-3</sup>, while average edge flow, as measured by a Mach probe 1.5cm from the cylindrical edge, is initially at around M=0.2, but jumps to approximately M=0.5 beyond 0.5mWb. Figure 1(c) shows the energy content of the magnetic fields in relation to the amount supplied by the gun circuit. The gun energy is found by integrating the power,  $P = I_{gun}V_{gun}$ , from 0.0 to  $60.0\mu s$  and represents the maximum amount of energy that can be delivered into the plasma. This value begins around 4kJ which is about half of the possible circuit energy based on the 1mF, 4.0kV capacitor circuit, and decreases steadily with increasing flux. The magnetic energy is calculated by finding the energy density,  $B^2/2\mu_0$ , at 16 radial points in the chamber and integrating over the volume at each location. Figure 1 demonstrates the ability to linearly modify the helicity of the plasma without significantly changing the total energy content or the bulk plasma properties.

Two turbulence analysis techniques, frequency-domain power spectra and the probability distribution function (PDF) of increments are constructed using the magnetic pickup coil timeseries (i.e.  $\dot{B}$ ) data. Since the probe is fabricated using a single 3mm wide loop, the B(t) signal has the best temporal resolution and bit-depth (65MHz sampling and 14-bit dynamic range) and is used directly in the analysis rather than converting the timeseries to B(t) by integration. For spectra analysis, the transformed B(f) data can be scaled into B(f) in frequency space by dividing the power in each frequency bin by  $f^2$ . The PDF and flatness analysis, on the other hand, uses B(t) directly. The results reflect a time range of 40 to  $60\mu s$  after initial breakdown is in a quasi-stationary state between formation and decay of the plasma and an ensemble average of forty shots for each helicity state.

The wavelet power spectrum of magnetic field fluctuations for each helicity case is presented in Figure 2. The curves shown are constructed by taking the a sixth-order Morlet wavelet transform [16] of each  $\dot{B}_r(t)$  (radially aligned component) timeseries. The resulting  $\dot{B}(f)$  is scaled to  $\tilde{B}_r$  by dividing through by frequency squared. The absolute scale in Figure 2(a) has been artificially staggered to clearly illustrate the shape of each curve. Each spectrum exhibits a break-point at approximately 1MHz. Using a Maximum Likelihood Estimation method [17], two power-law fits are computed for linear regions just above and below the break-point. The spec-

tral index and error for each fit is indicated in Figure 2(b). Though the helicity is increasing linearly, the power-law fit for each spectra does not change significantly, hovering around a slope of 3 for low frequency fits and around 5 for high frequency fits. This trend indicates that the change in helicity does not appear to have an effect on the frequency spectra.

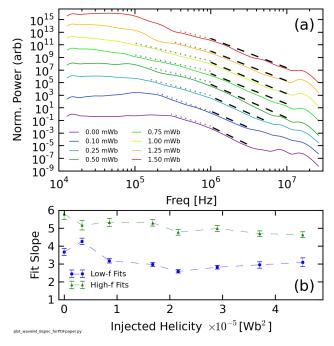


FIG. 2. (a) Magnetic field fluctuation spectra for the radial direction  $(B_r)$ , for each of the eight helicity states. The spectra are staggered in order to highlight the shape of each spectrum. (b) Fits for each spectra for either low or high frequencies. The width in frequency of each fit is indicated by the dashed lines in (a).

The calculation of spectra can be viewed as a secondorder moment of the PDF of increments; since the analysis of spectra shows little change for different values of helicity, it is natural to search for potential changes at higher order moments. We now show that the nature of the intermittency in the  $\dot{B}(t)$  fluctuations does appear to change with the helicity state. The PDF of increments is constructed by taking differences of values in a time signal—in this case,  $\dot{B}_r$ —separated by a time scale  $\Delta t$ with the increment defined as,

$$\Delta \dot{B}_r \equiv \dot{B}_r(t + \Delta t) - \dot{B}_r(t). \tag{3}$$

Figure 3 demonstrates how intermittency is determined through the measure of flatness. Fig. 3(a) shows the PDF of increments of a timeseries at  $2\times10^{-5}$  Wb<sup>2</sup> of injected helicity for two different timescales:  $0.15\mu s$  and  $15\mu s$ . The PDF with small time scale shows a highly pointed PDF with broad, fat tails indicating large excursions from the mean value—or intermittency. This non-Gaussian behavior is highlighted when the PDFs

are compared to a Gaussian curve. Dashed lines in Figure 3(a) indicate the best-fit Gaussian to each distribution. The PDF with a large time scale increment clearly show a much more Gaussian distribution compared to its best fit. The level of intermittency for each scale can be quantified by computing the normalized fourth-order moment of the PDF—also called flatness or kurtosis. The flatness for each PDF as a function of time scale and for each helicity state is shown in Fig. 3(b). Clearly, each state shows increasing flatness, and thus intermittency, with decreasing time scale. The flatness of a purely Gaussian distribution is indicated at F=3. Moreover, it is observed that the overall flatness of each curve increases as a function of helicity. In other words, the intermittency of the plasma increases with injected helicity—this is the main result of this paper.

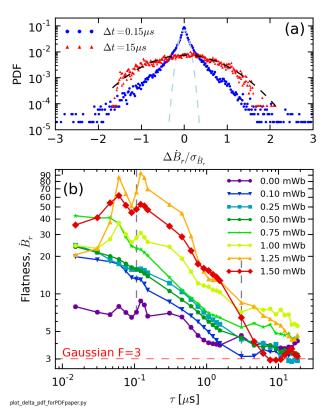


FIG. 3. (a) PDFs for a long and short  $\tau$  from data for  $K_B = 2 \times 10^{-5} Wb^2$  indicating the changing in intermittency with timescale. Dashed lines indicate the best-fit Gaussian curves for each PDF. (b) Flatness values for each timescale and each helicity state for the radial  $\dot{B}$  component.

This change with helicity is summarized in Figure 4(a) where the calculated flatness of  $\dot{B}_r$ , as shown in the curves of Fig. 3(b) as well as those for  $\dot{B}_{\theta}$  and  $\dot{B}_z$  has been averaged between the scales indicated by the dashed gray lines: between  $0.1\mu s$  and  $3.0\mu s$ , which approximately corresponds to a frequency range of 333kHz to 10MHz—where the frequency spectra is generally linear in Figure 2(a). The average flatness generally increases with

helicity, although there is a brief trend reversal at about  $1\times10^{-5}$  Wb<sup>2</sup> before the curve begins to increase again.

It should be noted that while the change in axial flow indicated in Fig. 1(a) can potentially have an effect on the measured intermittency (i.e. faster flow would tend to shift the flatness curve to the right), the influence is minimized by averaging over many time scales. It is also clear that the average flatness has superior correlation to helicity than to the average edge Mach number. Care needs to be taken, though, when attempting to interpret a spatial scale from a temporal scale (i.e. invoking Taylor hypothesis).

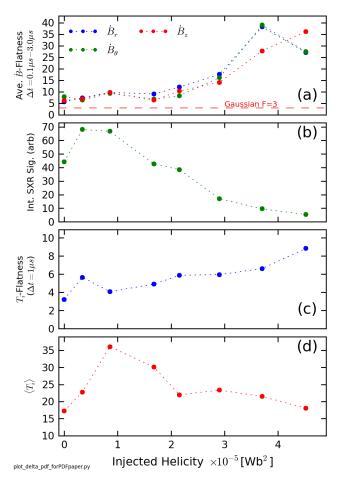


FIG. 4. (a) Flatness of magnetic component increments averaged over lags from  $0.1\mu s$  to  $3.0\mu s$  vs helicity. (b) Integrated soft X-ray signal versus helicity. (c) Flatness of  $T_i$  time series versus helicity. (d) Average  $T_i$  versus helicity.

While the physical origin of this observed intermittency and its trend with helicity is not completely understood in the context of this experiment, investigation of intermittency in space plasma yields some possible explanations. Simulations of MHD plasmas modeled after solar wind plasma with time series extracted in ways to match that of *in-situ* satellite observation [6, 7], have indicated a correlation between intermittency and the

passing of current sheets or reconnection sites. Past experiments on SSX have focused on observation of reconnection layers [18, 20]; thus, the experiment has a number diagnostics designed to measure signatures of reconnection including a set of soft X-ray photo-diodes [19] to measure X-rays generated by fast electrons and an ion Doppler spectrometer (IDS) system that measures bursts of ion temperature and flow [20]. Figure. 4(b-d) shows the output of these diagnostics for the same helicity scan and limited to the same time range as the turbulence data presented above. Soft X-ray measurement shows an initial increase in x-ray light going from zero to small amounts of helicity, but then a consistent decrease in measured light. Fig. 4(c) shows the flatness of PDFs constructed from  $T_i(t)$  as a function of helicity. Like, the flatness curve of  $\dot{B}$ , the  $T_i$  intermittency also increases with helicity. Meanwhile, the average, or background,  $T_i$  does not vary much, peaking slightly between 1 and  $2\times10^{-5}$  Wb<sup>2</sup>, but generally maintaining a value of between 20-25eV.

Taken together, these trends can be viewed as evidence for a connection between intermittency and reconnection. The hypothesis is that increasing the injected helicity increases the number of reconnection sites during Taylor relaxation (more  $T_i$ ) bursts but decreases their size (less X-ray light from electron acceleration). Given past observations of some of these effects in more controlled reconnection experiments on SSX [20], it is reasonable to think mechanisms are at play here as well. Alternate explanations, however, can involve helicity-related modification of fluctuations at the ion scale as a mechanism for the observed heating [21, 22]. Unfortunately, these hypotheses cannot be fully tested without higher spatial resolution (current spectroscopy diagnostics are line-integrated) and better temporal resolution in the ion measurements. In addition to improving diagnostics, comparisons to simulation may help as is done in solar wind research.

This paper presents the observation of a clear change in the intermittent character of B fluctuations as a function of injected helicity while simultaneously showing little to no change in the turbulent frequency-domain power spectra. Though the spectra presented here is not direct evidence of the turbulent energy cascade process, the results perhaps suggest that the cascade process is not modified by the level of helicity in the plasma. The discrepancy between spectra and PDF results is also an indication of the need to study higher order moments in turbulence analysis (i.e. 4th order Flatness vs 2nd order spectra) in order to fully flesh out modifications in turbulence [23]. The experiment demonstrates a straightforward method for modifying the intermittency in a plasma for detailed study and highlights an advantage of turbulence research in an experimental setting as a complement to in-situ measurements and simulation. A possible connection to a physical mechanism was established through soft X-ray

and IDS measurements, which suggested the intermittency is related to the spatial size of reconnection sites in the plasma. However, given the limitations of the current diagnostics, definitive conclusions cannot be made, but do provide impetus for further comparison to simulation

Finally, since helicity observations have been made in many of the same turbulent plasmas that exhibit intermittency [24–26], a link between helicity and turbulent intermittency may be a useful metric for understanding turbulence in both space and experiment, including possible comparisons to the variation of intermittency as a function of solar distance [27] as well as differences between confinement regimes in fusion devices.

- Frisch, U. 1995, Turbulence (Cambridge: Cambridge Univ. Press)
- Sorriso-Valvo, L. et al. Geophys. Res. Lett. 26, 18011804 (1999).
- [3] Wan, M. et al. ApJ. 744 177 (2012).
- [4] Sorriso-Valvo, L. et al. Planet. Space Sci. 49, 11931200 (2001).
- [5] Marrelli, L. et al. Phys. Plasmas. 12, 030701 (2005).
- [6] Greco, A. et al. Geophys. Res. Lett. 35, L19111 (2008).
- [7] Greco, A. et al., ApJ **691**, L111 (2009).

- [8] Wan, M. et al. Phys. Plasmas 16, 080703 (2009).
- [9] Servidio, S. et al, J. Geophys. Res. 116, A09102 (2011).
- [10] P. Veltri. Plasma Phys. Cont. Fusion. 41 A787 (1999).
- [11] V. Carbone, P. Veltri and A. Mangeney. Phys. Fluids A. 2 1487 (1990).
- [12] T. Gray, M. R. Brown, and D. Dandurand. Phys. Rev. Lett. 110, 085002 (2013).
- [13] D.A. Schaffner et al. Turbulence analysis of an experimental flux rope plasma. Accepted by Plas. Phys. Cont. Fusion Dec 2013.
- [14] Taylor, J.B. Rev. Mod. Phys. 58, 741 (1986).
- [15] Matthaeus, W.H. and Montgomery, D. Ann. N.Y. Acad. Sci. 357, 203 (1980).
- [16] Torrence, C. and Compo, G.P. Bull. Am. Meteorol. Soc. 79, 6178 (1998).
- [17] Clauset, A., Rohilla Shalizi, C. and Newman, M.E.J. SIAM Rev. 51, 661703 (2009).
- [18] Gray, T. et al. Phys. Plasmas 17, 102106 (2010).
- [19] Chaplin, V.H., et al. Phys. Plasmas 16 042505 (2009).
- [20] Brown, M.R. et al. Phys. Plasmas 19 080704 (2012).
- [21] P. Wu et al. Phys. Rev. Lett. 111 121105 (2013).
- [22] K.T. Osman et al.. ApJ Lett. **727** L11 (2011).
- [23] Matthaeus, W.H. and Velli, M. Space Sci. Rev. 160 145-168 (2011).
- [24] Goldstein, M.L., Roberts, D.A. and Fitch, C.A. Jour. Geo. Res. 99 11519-11538 (1994).
- [25] Ji, H., Prager, S.C. and Sarff, J.S. Phys. Rev. Lett. 74 2945 (1995).
- [26] Telloini, D. et al.. ApJ. 751 19 (2012).
- [27] A. Greco et al. ApJ. **749** 105 (2012).