Characterizing the relationship between the religious affiliation and incidences of Covid-19 at U.S. universities.

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Introduction

Although Covid-19 pandemic may feel like a thing of the past, there is still much research to do in order to understand its nascence, spread, and lasting health effects. Indeed, there is still much to do to ensure that we, as a society, are prepared to handle the next highly-transmissible pathogen that may arise. As university students whose first two years in school were far from normal on account of the Covid-19 pandemic — whose lives were dominated by case counts and triweekly testing — we are interested in exploring the development of the pandemic at colleges and universities across the United States. In particular, we are interested in the differences in how different academic institutions were affected by the pandemic. It has been well established that, at least in the United States, responses to the Covid-19 pandemic were tightly bound to political and ideological questions, the responses to which differ across the administrations of the wide range of universities in this country. In this paper, we will explore the differences in the impact of the pandemic between institutions with religious affiliations and those without religious affiliations. We will attempt to characterize the relationship between case counts during the fall and spring semesters of the 2020-21 academic year — the academic year in which responses to the pandemic were perhaps most varied across universities — and whether a university has a religious affiliation. We not only hope to answer the question of whether religious affiliation has a statistically significant relationship with case counts during the 2020-21 academic year — we also hope to discover the other characteristics of universities may have an effect on this relationship. To do so, we will employ a range of statistical inference procedures, from group testing to hierarchical multilevel models.

Description of data and source

Our data for this project comes from three sources:

- 1. NYTimes Covid-19 Data. This data set is publicly available on GitHub and was the source for various New York Times maps and visuals in its coverage of the pandemic. It includes case counts from July 2020 May 2021, and we have specifically selected cases at Universities. This dataset has 1948 entries and includes 2020 cases, 2021 cases, University IPEDS ID, University Name, State, etc.
- 2. IPEDS Data Center. This is a publicly available data set on colleges and universities across the globe. It has many possible variables including demographics, admission rates, religious affiliation, etc. The IPEDS data center allowed us to select which variables to include in our data set. The smallest subset of universities that included all from the NYTimes database (by IPEDS ID) was 6125 rows, with all U.S. universities.
- 3. Centers for Disease Control. This publicly available data set tracks mask mandates in each state from April 8, 2020, to August 15, 2021.
- 4. The presidential elections data from STAT 139 Problem Set 4. Of this data set, we will be particularly focused on the gap20repub predictor, which we will use to help characterize the political climate of the state in which each institution is located.

After removing universities that were missing lots of data in the pull from the IPEDS data center, we were left with n = 1,855 observations.

Data Cleaning Procedures

Our first step in cleaning the data is to read our data from CSV files into R data frames. The colleges data frame stores the NYT data on Covid cases at universities, while the ipeds data frame stores the data will most of our predictor variables (university characteristics) taken from IPEDS. We then rename most of the columns in ipeds to make them shorter and easier to work with.

Next, we merge the colleges and ipeds data frames on the ipeds_id column and remove institutions with no IPEDS data. We then create the religious and private columns, which are simply indicators for whether an institution has any religious affiliation, whether it has a catholic affiliation, and whether it is a private university. Finally, we drop any unnecessary or redundant columns from the data frame.

We then look to add a column to the data frame that addresses the extent to which mask mandates were present in the state in which each institution is located. We read out the mask mandates data from the CDC into a data frame from the CSV file, treat the appropriate columns as factors, and convert date into R's Date type.

The next step is to create a new simpler data frame to merge with md. This data frame contains only two columns: One with the name of each state, and the other with the number of days between July 1, 2020, and May 26, 2021, during which face masks were required in public in that state. We then merge this data frame with md to create full.cases, and create a column total.cases in full.cases that sums the cases and cases_2021 columns.

Finally, we read the presidential election data from Problem Set 4 into a data frame, create a two-column data frame with the columns state and gap20repub, and merge this data frame with our data frame of observations on the state variable.

Description of variables

After performing the data cleaning procedures outlined above, we are left with the following ADJUST NUMBER! columns:

- ipeds id
- institution.name
- state
- private
- religious.affiliation
- religious
- catholic
- tuition
- total.headcount
- percent.american.native
- percent.asian
- percent.black
- percent.hispanic.latino
- percent.pacific.islander

- percent.white
- percent.two.more.races
- percent.NA.race
- percent.nonres.alien
- percent.women
- · avg.grant.money
- grad.rate
- · percent.fin.aid
- percent.student.loan
- occupational.degree
- hs.equivalent.degree
- on.campus.housing
- · dorm.capacity
- city
- college
- cases
- cases 2021
- · religious
- catholic
- private
- · mask.mandated.days
- total.cases
- gap20repub

Group Testing

To begin our analyses, we will perform a range of group tests to determine whether the institutions with a religious affiliation had a higher true average number of Covid cases than religious institutions without a religious affiliation. In the following analyses, we will test whether or not the true average number of cases in the fall semester — i.e., the case counts for just 2020 in the NYT data set, cases — were different for these two groups of institutions, as well as whether the true average number of cases for the entire academic year — see the description of total.cases — different for the two groups of institutions. We will perform both sets of analyses, because they are so fast and easy to perform and interpret. Later, as we bfit linear models to perform more complicated statistical inference procedures with respect to our data set, we will demonstrate why a focus will be placed on case counts from the fall semester only (see "Determining whether data from 2020 or 2020 and 2021 should be used").

Checking the assumptions for t-based methods

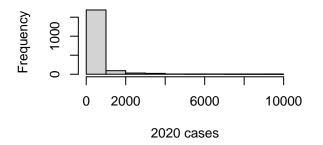
We begin with the most commonly used test for a difference in means: the Student-t test. Of course, before we can perform this test, we must make sure that its underlying assumptions are reasonable. Because we have no reason to assume that the variances in the observations between both groups — religiously affiliated

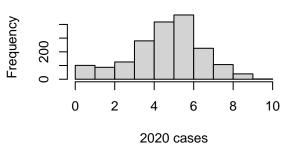
and not religiously affiliated universities — are the same, we will use the unpooled t-test. For unpooled t-based test for a difference in sample means, there are three assumptions:

- 1) Observations are independent. We claim that this observation is reasonable. Even though the geographic proximity of universities or just a relationship between universities in which students from one frequently visit the other might have caused there to be some correlation between case counts at these different schools, we claim that since universities are somewhat insular communities students tend to stay within their own social sphere of their university this is not a major concern. Overall, with such a rich data set, in which a wide and diverse range of characteristics are expressed across all 1,855 observations, this assumption of independence of observations seems reasonable.
- 2) Groups are independent of one another. There is no reason to suggest that the two groups in question religious institutions and non-religious institutions are not independent from one another. Above, we justified that all of the observations in our data set are sufficiently independent from one another if this is true, there is no reason to suggest that these two groups of religious institutions would not be independent of one another.
- 3) **Observations are normally distributed.** As is shown in the plot below (left), both of the response variables in question are *not* normally distributed; after log-transforming these responses, however, we see that their distribution is symmetrical enough to satisfy this assumption. Of course, we do not need to seek perfect normality with respect to these distributions, since t-based statistical inference procedures are robust to this assumption (as was demonstrated in Question 5 in Problem Set 3).



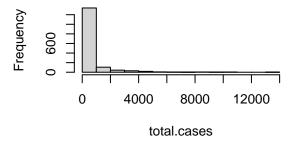
2020 cases, log-transformed

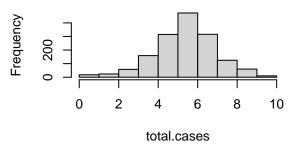




total.cases, untransformed

total.cases, log-transformed

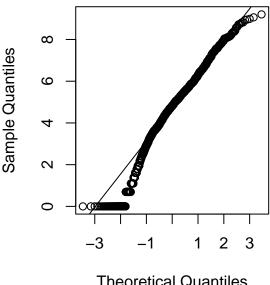


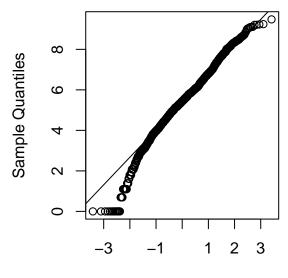


The Normal Q-Q Plots below corroborate the conclusion that this assumption is reasonable. In each plot, the data for the most part follows the line that we would expect if it were perfectly normally distributed; although, since the data sits below the line at both the positive and negative extremes of the graph, the left tail is a bit fatter and the right tail a bit skinnier than the perfectly normal distribution in each of these sample distributions.

Normal Q-Q Plot, 2020 cases

Normal Q-Q Plot, total.cases





Theoretical Quantiles

Theoretical Quantiles

Student-t Tests

Now that we have shown the assumptions of Student-t tests to be reasonable, we can proceed to perform the test itself. We perform two two-sided t-tests for a difference in means. In each case, the null hypothesis is that the true mean case counts in the two groups — religiously affiliated and non-religiously affiliated institutions — are equal over the given time period, and the alternative is that they are not equal. As in the rest of the paper, we will use the standard confidence level of $\alpha = 0.05$, for the sake of convenience and conformity. Below are the results from these tests.

sample	test.statistic	df	p.value
2020 only	1.379947	969.4587	$0.1679212 \\ 0.5726786$
entire year	-0.564321	885.7181	

In both tests, we see that our p-value is greater than the significance level of 0.05; we thus fail to reject the null hypothesis in both cases — we do not have statistically significant evidence to suggest that the true mean case counts, both for the fall semester and for the entire year, are different between the religiously affiliated and non-religiously affiliated institutions. Note that the degrees of freedom — which are not integers owing to R's use of the Welch approximation — are different for the two tests. This is because the test using the total.cases data has fewer observations, since some schools in our sample did not report case counts for the spring semester. This issue is tackled in greater detail below (see "Determining whether data from 2020 or 2020 and 2021 should be used").

Non-Parametric Testing — Wilcox Rank Sum Test

We will also perform the non-parametric Wilcox Rank Sum Test to determine whether the case counts are different between religiously affiliated and non-religiously affiliated schools. The strength of this nonparametric test lies in the fact that it does not rely on a assumption on the distribution of the data-generating process of the sample follows. Thus, though we are confident in having shown above that the distributions of the log-transformed responses are sufficiently approximately normal, for the sake of completeness, we will perform this non-parametric test, and see if it leads us to the same conclusions.

Again, we will perform the Wilcox Rank Sum Test on data from just the fall semester and on data from the entire academic year. For the following two tests, the null hypothesis is that the true average quantiles within the two groups — when the data from both groups are ranked together — are the same, while the alternative hypothesis is that there is an association between group status and the average quantile of the observations in the entire population.

sample	test.statistic	p.value
2020 only entire year	320824.0 225800.5	$\begin{array}{c} 0.2990076 \\ 0.7547593 \end{array}$

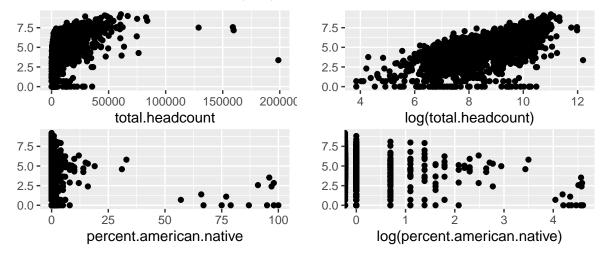
As the results above show, neither test was statistically significant at the 0.05 confidence level; we thus again fail to reject the null hypothesis, concluding that there is no statistically significant evidence to suggest that the there is an association between religious affiliation and average quantile of case counts in either sample.

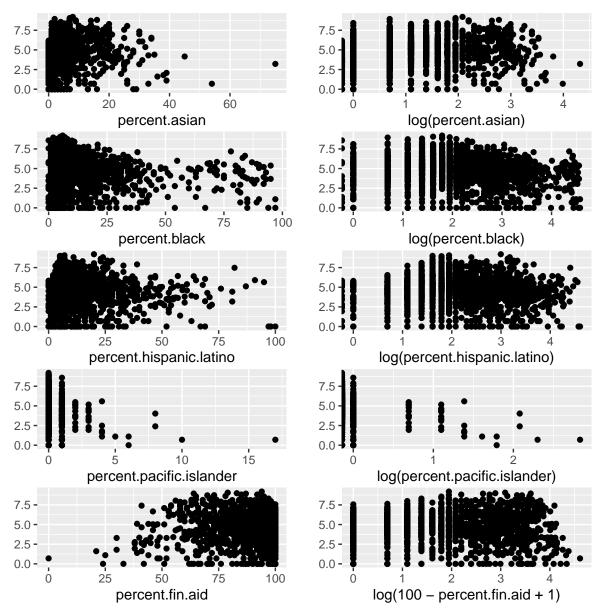
Basic Linear Regression Models

Of course, group tests are limited in that they do not take into account potential confounding variables that might reveal the significance of an institution's having a religious affiliation. To take into account the effects of these potential confounding variables — which we have already identified at length, as evidenced by the extensive list of predictors we compiled before beginning our analyses — we will fit linear models. We will then use these linear models to perform statistical inference on the coefficient of the religious predictor, determining whether there is a statistically significant relationship between an institution's religious affiliation and the number of cases that it recorded.

Checking the Assumptions of Linear Regression Models

Before we can fit more complicated models, we must first check the assumptions of linear regression. We begin by checking the assumption of linearity. To do so, we plotted cases versus all of the quantitative predictors that we would like to include in our analyses (the complete list of these plots can be found in Appendix A). We the identified that total.headcount, percent.american.native, percent.asian, percent.black, percent.hispanic.latino, and percent.pacific.islander would benefit from being log-transformed; given the left-skewness of its distribution, we also determined that percent.fin.aid would be best transformed using the following transformation log(100 - percent.fin.aid + 1). The following plots show that the distribution of these predictors before and after being transformed. In these plots, the y-axis is always log-transformed cases (2020); the axis label is not printed in order to save space.

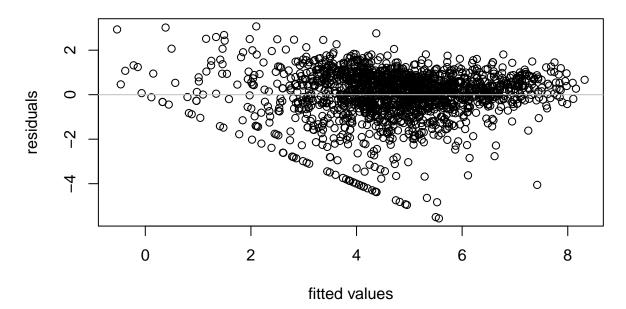




We claim that with these transformations, the assumption of linearity is reasonable.

What remains to be shown is that the assumption of homoskedasticity is reasonable. In order to check this assumption, we fit basic regression models for cases and total.cases using all of the predictors in our predictor set.

cases (2020)

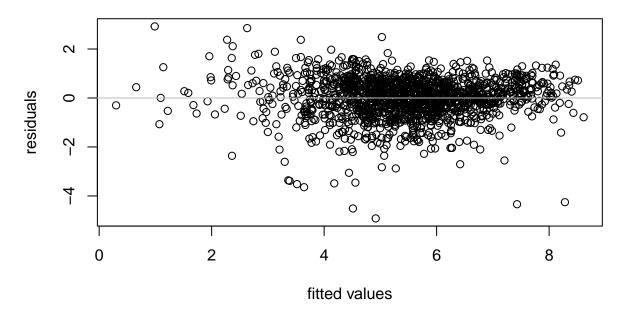


As is shown in the plot above, the spread of the residuals is not constant across the entire range of fitted values — thus, it is called into question whether the assumption of homoskedasticity is reasonable in this case. The behavior of this graph is interesting: Towards the left extreme of the graph, there appear to be bands of observations whose positions on this plot form negatively sloped lines. The left-most line corresponds to all those observations where the case counts are zero; the second-left-most line corresponds to the observations where the case count is two, etc. As one moves closer to the center of the plot, this patter disappears, and the plot assumes a form that is much better suited to linear regression.

Thus, this problem arises from the fact that our response variable is discrete, and from the fact that we have so many observations with very low case counts. As it stands, we are not in a position to accept the assumption of homoskedasticity. As we use techniques based on Gaussian regression to explore the association between the religious affiliation of a school and its reported case counts, we must therefore use heteroskedastic-consistent standard errors. Later in this paper, we will also employ the techniques of Poisson regression, which should solve the problem with this assumption.

Below, we recreate the same plot, but for the case counts for the entire 2020-21 academic year.

total.cases (2020-21)



In the above plot for the model for total.cases, the spread of the residuals appears much more consistent across the entire range of fitted values. If one looks carefully enough, however, they will see that the same behavior observed in the preceding plot is present in this one, the difference being that there are fewer schools that reported very low case counts (0, 1, or 2). This is likely due both to the fact that, with an extra five months of data, our response took on enough different values to begin to behave more like a continuous variable, and to the not insignificant number of schools that simply did not report case data for the spring semester (297 out of 1855 observations).

Determining whether data from 2020 or 2020 and 2021 should be used

Naturally, there is a temptation to forget about the case data for only 2020 and to focus on case data for the entire academic year (the entire time period during which case data was collected by the *New York Times*). There is one problem, however: While the *New York Times* was able to compile case data for all of the schools in our data set for the fall semester of that year, it was not able to find data for 297 schools for the spring semester. This is a nontrivial number of observations given that our data set only consists of 1855 different institutions; thus, to determine whether it would be sound to remove these 297 observations and fit models and perform statistical inferences on data from the entire academic year, we must determine whether the two groups of schools in question — those that reported data for the entire academic year, and those that did not — are sufficiently similar to one another.

The first step is to compare the coefficients of our baseline model (1m6 above) when it is fit to all 1855 observations, as well as individually to the two different groups of schools in question. The coefficient estimates, along with the p-values (not adjusted to be heteroskedastically consistent) are given below.

As we can see, when the sample of the institutions used to fit the model changes, some of the coefficient estimates change vastly. Take, for example, the coefficient estimate for religionYes, which can be interpreted as the change in cases that we would expect if a given school were to have a religious affiliation rather than not have one. This coefficient estimate is not statistically significant when all institutions are considered together, is positive and statistically significant when the institutions that reported data for the entire academic year are considered, and negative and statistically significant when the institutions that only reported data for the fall are considered. In fact, if one were to inspect the table above, they would notice that the majority of predictors included in this baseline models experienced changes in coefficient estimates and statistical significance as the sample of institutions considered was changed.

	all schools			schools with data for both years		th only ata
	Est.	p	Est.	p	Est.	p
(Intercept)	-5.719	< 0.001	-4.975	< 0.001	-2.338	0.109
religiousYes	0.102	0.252	0.318	< 0.001	-0.701	0.049
tuition	0.00002	< 0.001	0.00001	< 0.001	-0.000003	0.878
log(total.headcount + epsilon)	0.920	< 0.001	0.915	< 0.001	0.491	< 0.001
log(percent.american.native + epsilon)	0.013	0.811	0.170	< 0.001	-0.300	0.072
log(percent.asian + epsilon)	-0.125	0.026	-0.225	< 0.001	-0.0006	0.998
log(percent.black + epsilon)	0.195	< 0.001	0.205	< 0.001	-0.057	0.716
log(percent.hispanic.latino + epsilon)	0.060	0.172	0.075	0.046	0.223	0.110
log(percent.pacific.islander + epsilon)	-0.289	0.015	-0.366	< 0.001	0.118	0.719
percent.white	0.018	< 0.001	0.015	< 0.001	0.014	0.017
percent.two.more.races	-0.025	0.026	-0.015	0.115	-0.066	0.097
percent.women	-0.011	< 0.001	-0.014	< 0.001	0.002	0.784
grad.rate	0.021	< 0.001	0.020	< 0.001	0.017	0.037
log(100 - percent.fin.aid + epsilon)	-0.043	0.162	0.024	0.349	-0.275	0.019
on.campus.housingYes	0.823	< 0.001	0.670	< 0.001	1.096	< 0.001
gap20repub	0.013	< 0.001	0.012	< 0.001	0.028	< 0.001
privateYes	-0.677	< 0.001	-0.377	0.003	-0.475	0.331
percent.student.loan	0.005	0.002	0.007	< 0.001	-0.0006	0.923
mask.mandated.days	0.0002	0.545	-0.0007	0.001	-0.00007	0.941
occupational.degreeYes	-0.184	0.017	-0.011	0.865	-0.938	< 0.001
hs.equivalent.degreeYes	0.136	0.154	-0.083	0.287	0.314	0.381
Num.Obs.	1705		1469		236	
R2	0.604		0.694		0.408	
R2 Adj.	0.599		0.690		0.353	
AIC						
BIC						
Log.Lik.	-2590.545		-1808.194		-424.879	
RMSE	1.11		0.83		1.46	

Clearly, then, there are some underlying differences between the schools that did and the schools that did not report case data for the spring semester of the 2020-21 academic year. Consider, the coefficient estimate for religiousYes, which represents the natural logarithm of the multiplicative change in the number of cases that we would expect given that a school were to be religiously affiliated, with all other predictors held constant. The coefficient estimate for religiousYes is quite different in the two models fit to data from only one of the two subgroups, which is especially interesting for our research purposes. Indeed, searching for the differences between these subgroups in terms of religious and other predictors might help us to answer the questions about the association between religious affiliation and reported Covid cases that are motivating this paper.

First, we investigate the difference in the political leanings of the states in which these schools were located, as given by gap20repub. To do so, we perform a *t*-test (the assumptions that allow us to do so have been explored above), with the null hypothesis being that the true means gap20repub are equal between the two groups of institutions, and the alternative being that the true means are different. The result of this test is shown below.

	predictor	test.statistic	df	p.value
t	gap20repub	-6.289246	445.719	0

With a p-value that is much smaller than our $\alpha=0.05$ (again, because we do not assume equal variances between the groups, the Welch approximation for degrees of freedom is used), we reject the null hypothesis, concluding that the true mean gap20repub is different for the schools that did report case data for 2021 versus those that did not. As it turns out, the 95% t-based confidence interval for the mean gap20repub for the schools that did report 2021 case data minus the mean gap20repub for the schools that did not is (-9.468120, -4.959647) — thus, we conclude that the schools that did report 2021 case data are located in states that are considerably more left-leaning than the schools that did not.

We repeat this sort of analysis for total.headcount, tuition, percent.fin.aid, mask.mandated.days, on.campus.housing, and religious, predictors that we have chosen based on large differences in the coefficient estimates produced by the models above when fit to only one of the two subgroups of institutions. We use a two-sided t-test for the quantitative variables and two-sided z-tests for proportions (ADDRESS) for the categorical predictors. The hypotheses are similar to above, the null being that the true means/proportions are equal between the two groups, and the alternative being that they are not equal. As per the results shown below, the tests for all six of these predictors showed statistically significant differences between the two groups of universities.

predictor	test.statistic	df	p.value
total.headcount	10.4880993	872.6989	0.0000000
tuition	3.7184096	397.6510	0.0002293
percent.fin.aid	0.5400659	349.3054	0.5894957
mask.mandated.days	8.9492453	376.7757	0.0000000
on.campus.housing	26.5612204	1.0000	0.0000003
religious	14.2542757	1.0000	0.0001597

The existence of these statistically significant differences between these two groups of institutions leads us to two distinct conclusions: Firstly, that we should perform all further analyses on data only from the fall 2020 semester, and secondly, that we should consider interaction effects in our model to help better isolate and take into account these demonstrated differences between these two different groups of institutions.

Linear Models with Interaction Effects

Above we performed several linear regressions with no interactions and multiple predictors. Our "base model" includes all of the predictors we include in this paper, which are: religious, tuition, total.headcount, percent.american.native, percent.asian, percent.black, percent.hispanic.latino, percent.pacific.islander, percent.white, percent.two.more.races, percent.women, grad.rate, percent.fin.aid, on.campus.housing, gap20repub, private, percent.student.loan, mask.mandated.days, occupational.degree and

hs.equivelant.degree. Above we discuss using 2020 cases, 2021 cases, or the total number of cases, concluding that we will use only 2020 cases for the remaining models.

We will first look at three linear models with all of the predictors in this paper: our "base model," an interaction model between the religious predictor and the others (religiousInteraction), and a full interaction model (fullInteraction).

	coefficients	p.value
tuition	0.0000174	0.0000161
$\log(\text{total.headcount} + \text{epsilon})$	0.9199545	0.0000000
$\log(\text{percent.asian} + \text{epsilon})$	-0.1251276	0.0257048
$\log(\text{percent.black} + \text{epsilon})$	0.1946336	0.0000088
$\log(\text{percent.pacific.islander} + \text{epsilon})$	-0.2890057	0.0146274
percent.white	0.0178880	0.0000000
percent.two.more.races	-0.0254703	0.0262692
percent.women	-0.0107628	0.0000245
grad.rate	0.0210106	0.0000000
on.campus.housingYes	0.8225306	0.0000000
gap20repub	0.0127476	0.0000000
privateYes	-0.6765733	0.0000051
percent.student.loan	0.0053149	0.0017920
occupational.degreeYes	-0.1840886	0.0173571

Above is the base model. We see that there are a lot of statistically significant coefficients on the predictors, holding all else constant. These are noted with a star next to them in the above table. Notably, the coefficient for the religious variable does not carry statistical significance, with a p-value of .25190, significantly above $\alpha = 0.05$. This could be for a number of reasons, including that 1) Religious affiliation (either Yes: Religious or No: Not Religious) simply has no correlation with 2020 Covid cases or 2) The religious variable shares predictive power (has some degree of collinearity) with other predictor variables.

We will determine this relationship by fitting the religiousInteraction model; a linear model that includes the interactions between the religious variable and the remaining confounding variables.

	coefficients	p.value
religiousYes	3.6653774	0.0002896
tuition	0.0000175	0.0007126
$\log(\text{total.headcount} + \text{epsilon})$	0.9491104	0.0000000
$\log(\text{percent.black} + \text{epsilon})$	0.2514204	0.0000003
$\log(\text{percent.pacific.islander} + \text{epsilon})$	-0.3163746	0.0229103
percent.white	0.0190307	0.0000000
percent.women	-0.0110546	0.0002047
grad.rate	0.0222312	0.0000000
on.campus.housingYes	0.8374462	0.0000000
gap20repub	0.0131810	0.0000000
privateYes	-0.6565577	0.0002535
percent.student.loan	0.0055159	0.0041419
religiousYes:log(percent.american.native + epsilon)	-0.4244315	0.0100105
religiousYes:log(percent.black + epsilon)	-0.3386581	0.0026832
religiousYes:grad.rate	-0.0133299	0.0414159
religiousYes:on.campus.housingYes	-1.6646194	0.0013667
religiousYes:mask.mandated.days	0.0022753	0.0000643

The religious Interaction model clarifies the significance of the religious predictor: When accounting for the interactions between religious and other predictors, as seen in this model, religious becomes a statistically significant predictor, with a p-value of 0.000290, significantly below the p-value of $\alpha = 0.05$. This indicates that the previous "base model" had religious as an insignificant predictor because it interacted

with other variables which were collinear and therefore shared a lot of predictive power. Given the number of confounding variables, this result makes sense. We see in this model that the coefficient on the religiousYes variable is 3.665, indicating that when looking at a religiously-affiliated school versus one that is not, holding all other variables constant, the religious affiliation alone implies an increase of 3.665 Covid cases.

religious had a statistically significant interactive term with 5 other variables, which were: percent.black, percent.american.native, percent.fin.aid, on.campus.housing, and mask.mandated.days. For example, the term religiousYes:mask.mandated.days in the summary results of the interaction model had a coefficient of 2.275e-03 and a p-value of 6.43e-05. This implies that it is statistically significant in this model, and for religiously affiliated schools, a one-day increase in mask mandates correlates with a very small increase in Covid cases compared to its non-religious counterpart. This result is interesting, and could prompt further investigation in a different paper.

Given the significance of the interaction terms in our partial interaction model, we will now look at a full interaction model with all predictive variables in this paper to predict the 2020 Covid cases. Significant results relating to the religious predictor are printed below.

	coefficients	p.value
religiousYes:log(percent.asian + epsilon)	-0.3936018	0.0422889
religiousYes:log(percent.black + epsilon)	-0.4388041	0.0288920
religiousYes:on.campus.housingYes	-1.4964379	0.0384122
religiousYes:mask.mandated.days	0.0017751	0.0350710

The religious variable in the above model with all interactive terms is not statistically significant in predicting 2020 Covid cases at Universities, with a p-value of 0.290212. But, very few terms alone are significant in the model; only percent.black, percent.two.more.races, and on.campus.housing. Even the predictor total.headcount is not statistically significant in this model, whereas it is consistently very significant in other models given the obvious relationship between the total number of people on a given campus and the number of Covid cases amongst them. This result suggests that a lot of the variables are correlated with one another to varying degrees. Thus, there are many interactions, and therefore predictive terms in this model. These have taken the predictive power from the religious variable by itself; though some interactions with the religious term are statistically significant, such as percent.asian, percent.black, mask.mandated.days, and on.campus.housing. This indicates that in relation to 2020 Covid cases, the religious affiliation has an affect on the predictive power of those variables. Ultimately a high number of predictive terms in a model dealing with highly collinear data will inherently diminish the predictive power from a term that shares a lot of correlation with others (referencing religious, amongst other terms). With so many predictors, the t-tests used to determine the statistical significance of each coefficient estimate are also not very powerful, as the number of degrees of freedom is quite high.

Model	R.Squared
base model	0.6035471
religiousInteraction	0.6208401
fullInteraction	0.7215086

We see in the above table that the R^2 value for the three models increases as the number of interactive terms increases. This indicates the significance of the interactive terms in the prediction model. It is unsurprising that the greatest increase is between the religiousInteraction model and the fullInteraction model. This can be explained by the sheer number of interactive terms in the model, as well as the collinearity between a lot of variables in the data.

We now perform ESS F-tests to compare the predictive power the base model to religiousInteraction and religiousInteraction to fullInteraction. In each test, the null hypothesis is that the true coefficients of the additional predictors included in the larger model — religiousInteraction in the first test, and fullInteraction in the second — are all zero; the alternative hypothesis is that the true coefficient of one or more of these predictors is not zero, i.e., that the additional predictors provide explanatory power. The result of these ESS F-tests are shown below.

ESS.F.test	F.statistic	df	p.value
base model vs. religiousInteraction	4.221356	18	0
religiousInteraction vs. fullInteraction	3.160287	171	0

In the first test, because the p-values of each test are below our $\alpha=0.05$, we reject the null hypothesis, and conclude that there is evidence that the religious interaction terms contribute to the model. Furthermore, in the second ESS F-test between the religiousInteraction model and the fullInteraction model, we again reject the null hypothesis, concluding that there is evidence that the additional interaction terms in fullInteraction have some explanatory power. This indicates that both religious interaction with the confounding variables (as discussed above) and the predictors interacting with one another are significant and improve (from the R^2 results) their respective models.

We used a variance-covariance matrix result to view the covariance values between religious and all other variables to create a simplified linear regression model with the most correlated confounding variables removed. The refined full interaction model is below, with the terms private, percent.pacific.islander, percent.hispanic.latino, on.campus.housing, percent.native.american, gap20repub, percent.women, grad.rate, percent.white, percent.student.load, and mask.mandated.days removed.

	coefficients	p.value
religiousYes	2.2235383	0.0046053
religiousYes:tuition	0.0000239	0.0014909
religiousYes:log(total.headcount + epsilon)	-0.3492881	0.0001207

We see above that we have artificially made the religious predictor significant in the full interactive model by removing terms that it is collinear with. But, this comes at the expense of the R^2 value, now 0.5368185 which has decreased even from the "base model" with all predictors but no interactions. This indicates that the variables we removed are important in the prediction of 2020 Covid cases.

In Search of a Parsimonious Model: Sequential Variable Selection Models

Of course, both religiousInteraction and fullInteraction are large, complicated models with many predictors — this makes them hard to interpret, and also leaves our significance tests diminished in statistical power. In order to find more parsimonious models — i.e., remove some predictors from these models — we performed Sequential Variable Selection using AIC as our model comparison criteria, stepping backward, forward, and in both directions. Brief descriptions and results from each resulting model are below.

- Backward step model: For this model, we started with fullInteraction, stepping backwards until a reduction in AIC was no longer possible. This process removed 116 predictors, leaving the resulting model, back.step, with 94 predictors. This list includes religiousYes, as well as interaction between religious and eight other predictors: tuition, log(total.headcount log(percent.american.native + epsilon), + epsilon). log(percent.asian + epsilon), log(percent.black + epsilon), percent.two.more.races, on.campus.housingYes, Of the nine predictors related to religious included in this model, mask.mandated.days. only 4 were significant at the 0.05 level: religiousYes, religiousYes:log(percent.asian + epsilon), religiousYes:on.campus.housingYes, and religiousYes:mask.mandated.days. Thus, according to this model, the statistically significant relationship between religious and cases changes in nature based on the predictors log(percent.asian + epsilon), on.campus.housingYes, and mask.mandated.days. Also worth noting is that the backward-stepping method of sequential variable selection might not be the best for our purposes: As we wish to trim down our incredibly large list of predcitors, starting with the complete list of predictors — rather than starting with a smaller list, or even none at all — might lead the algorithm to converge to a local min that keeps many more predictors than a forward-stepping or bidirectionally stepping method.
- Forward step: For this model, we started with our base model, and stepped forward until a reduction in AIC was no longer possible. This process added 55 predictors, leaving

forward.step with 75 predictors. In terms of the predictors related to religious, this list included religiousYes, religiousYes:mask.mandated.days, religiousYes:on.campus.housingYes, religiousYes:tuition, religiousYes:log(percent.asian + epsilon), and religiousYes:percent.two.more.ra Interestingly, all of the religious interaction terms in this model were statistically significant at the 0.05 level, but the predictor religiousYes itself was not. We can interpret this model as saying that whether a school has a religious affiliation changes the relationship between cases and these other predictors, but that religious does not have a significant association with cases in of itself.

- Forward step 1: For this model, we stepped forward from an intercept model. As a result, forward.step1 incorporated 67 predictors. Rather tellingly, this list of predictors did not include religiousYes, or any interaction term with religious. This could be taken as evidence that religious really is not a relevant predictor at all.
- Bidirectional step: For this model, we used our base model as our starting point, and stepped in both directions (alternating forwards and backwards), until an improvement in AIC was no longer possible. As a result, 55 predictors were added to the base model to produce both.step, a model with 75 total predictors. This list of predictors for this model was extremely similar to the list of predictors included in the forward.step model; only four predictors were different between the two models, none of which were related to religious. Predictably, the same interaction terms with religious that were significant in forward.step were statistically significant in this model as well, and religiousYes was again not statistically significant. This model corroborates the idea that whether an institution is religious changes the relationship between cases and these other predictors, but that there is no relationship between the predictor religious and the response cases.

As we compare the final AIC values of all four models below, we see that theback.step model has the lowest AIC; however, the forward.step and both.step models do have comparable values for AIC.

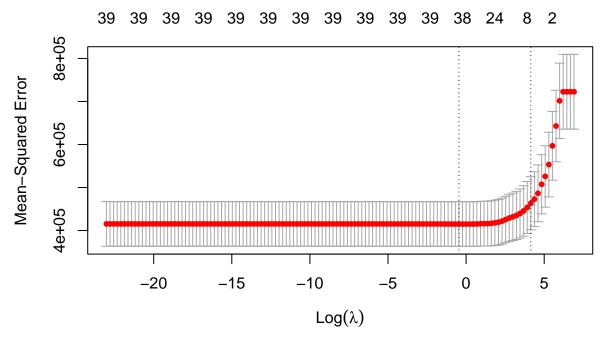
model	AIC
back.step	4816.395
forward.step	4833.366
forward.step1	4910.775
both.step	4828.786

LASSO for Variable Section

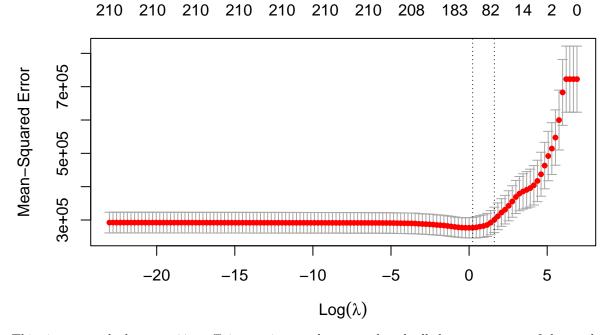
Because sequential variable selection can be sensitive to outliers and high-leverage observations, and in order to get a better idea of which of the three sequential variable selection models might be the most reliable, we will employ an alternative to this method: LASSO. A penalized form of regression, LASSO is able to function as a method of variable selection, since, unlike ridge regression, it actually does shrink coefficient estimates to exactly zero.

We will apply LASSO to both the religious Interaction and fullInteraction models, and interpret the results of each model. In each case, we will use cross-validation to select the best regularizing constant λ with which to fit each model.

First, we do so for the religiousInteraction model. We plot the λ values that we cross validated to make sure that the minimum value given by R is not the lower or upper bound of those considered (which would suggest that we widen our range of λ values considered); we then fit a LASSO model using the formula from religiousInteraction; call this model LASSO Model 1.



In LASSO Model 1, only the intercept estimate and the coefficient estimate for religiousYes:percent.women were shrunk all the way to zero. We now perform the same procedure with the fullInteraction model, creating LASSO Model 2:



This time around, there are 11 coefficient estimates that were shrunk all the way to zero; of those related to religious, only religiousYes:percent.women was shrunk to zero.

In order to determine which of the remaining predictors in each model are statistically significant, we refit a linear model using all the coefficients that were not shrunk to zero in each of LASSO Models 1 and 2. Note that even though the intercept was shrunk to zero by LASSO in both cases, we still include an intercept in this new model to make interpretation of the coefficient estimates in the resulting models easier. Call the new linear models LASSO-Selected Linear Model 1 and LASSO-Selected Linear Model 2. The two tables below show the coefficients that we found to be statistically significant in each of these two models.

Table 3: LASSO-Selected Linear Model 1

	coefficients	p.value
religiousYes	3.7873072	0.0000828
tuition	0.0000175	0.0006961
$\log(\text{total.headcount} + \text{epsilon})$	0.9491069	0.0000000
$\log(\text{percent.black} + \text{epsilon})$	0.2503230	0.0000004
log(percent.pacific.islander + epsilon)	-0.3143841	0.0236531
percent.white	0.0190369	0.0000000
percent.women	-0.0104931	0.0000577
grad.rate	0.0222903	0.0000000
on.campus.housingYes	0.8381158	0.0000000
gap20repub	0.0131994	0.0000000
privateYes	-0.6582761	0.0002423
percent.student.loan	0.0055166	0.0041280
religiousYes:log(percent.american.native + epsilon)	-0.4278807	0.0093028
religiousYes:log(percent.black + epsilon)	-0.3328287	0.0029103
religiousYes:grad.rate	-0.0130525	0.0445093
religiousYes:on.campus.housingYes	-1.7000670	0.0008971
religiousYes:mask.mandated.days	0.0022565	0.0000693

In both LASSO-Selected Linear Models 1 and 2, we find that religiousYes is statistically significant. Recall that this is the categorical indicator variable for religious, which can be interpreted as the natural logarithm of the multiplicative change in cases that we would expect for an institution with a given predictor set if it were to have a religious affiliation, rather than not have one, and all the other predictors were to remain constant.

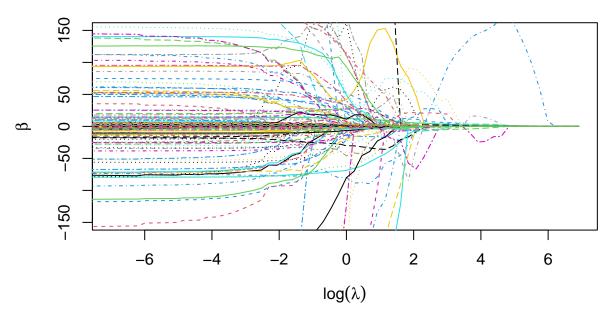
Interestingly, while five different religious interaction coefficients are statistically significant in LASSO-Selected Linear Model 1, only one religious interaction coefficient is statistically significant in LASSO-Selected Linear Model 2: religiousYes:mask.mandated.days. Thus, while the first model suggests that the relationship between religious and cases is affected by the value of five other predictors in the model, the second suggests that the association between religious and cases changes based on the value of mask.mandated.days of a given observation. It appears that the interaction effects deemed to be statistically significant in LASSO-Selected Linear Model 1 shared some level of collinearity with some of the additional interaction effects that were included in LASSO-Selected Linear Model 2. In this way, when these other interaction effects were included in the model, the religious interaction effects were no longer statistically significant, as the relationships that they helped to describe were better captured by other predictors.

The plot below demonstrates that there does indeed exist collinearity between the predictors of LASSO Model 2 (and thus LASSO-Selected Model 2). We have chosen to present this plot, because it is more readable than a printout of a massive variance-covariance matrix. This plot shows the trajectories of the coefficient estimates of LASSO Model 2 as the regularizing constant λ increases on a logarithmic scale. As is clear, not all of the coefficient estimates are shrunk uniformly towards zero; instead, some display sharp increases in magnitude as λ increases. This demonstrates that there is collinearity between some of the predictors: As one predictor in a collinear pair is shrunk to zero, the magnitude of the coefficient estimate for the other increases in order to make up for the lost predictive power.

Table 4: LASSO-Selected Linear Model 2 $\,$

religiousYes		ac-:t-	1
0.0452619	1	coefficients	p.value
on.campus.housingYes 4.4174840 0.0035187 religiousYes:mask.mandated.days 0.0016696 0.0474806 tuition:percent.two.more.races -0.0000049 0.0130804 tuition:percent.student.loan -0.0000006 0.0313698 tuition:percent.student.loan -0.0000006 0.0088660 log(total.headcount + epsilon):log(percent.black + epsilon) -0.1062718 0.0266786 log(percent.american.native + epsilon):gap20repub -0.0118856 0.0093360 log(percent.american.native + epsilon):log(percent.pacific.islander + epsilon) -0.5202528 0.0482986 log(percent.asian + epsilon):gap20repub -0.118856 0.0093360 log(percent.asian + epsilon):gap20repub -0.5202528 0.0482986 log(percent.black + epsilon):gap20repub -0.019322 0.0019242 log(percent.hispanic.latino + epsilon):grad.rate -0.0096110 0.0001176 log(percent.hispanic.latino + epsilon):grad.rate -0.0091300 0.0122518 percent.white:on.campus.housingYes -0.0143575 0.0338577 percent.two.more.races:mask.mandated.days -0.002355 0.0407143 percent.women:log(100 - percent.fin.a		0.=	
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grad.rate:gap20repub -0.0004421 0.0081894 grad.rate:hs.equivalent.degreeYes -0.0144991 0.0411769 on.campus.housingYes:percent.student.loan 0.0149356 0.0082776 on.campus.housingYes:mask.mandated.days -0.0021618 0.0119621 on.campus.housingYes:occupational.degreeYes -0.8963147 0.0024896 on.campus.housingYes:hs.equivalent.degreeYes -0.5515519 0.0392638	percent.women:percent.student.loan	0.0003121	0.0334358
grad.rate:hs.equivalent.degreeYes -0.0144991 0.0411769 on.campus.housingYes:percent.student.loan 0.0149356 0.0082776 on.campus.housingYes:mask.mandated.days -0.0021618 0.0119621 on.campus.housingYes:occupational.degreeYes -0.8963147 0.0024896 on.campus.housingYes:hs.equivalent.degreeYes -0.5515519 0.0392638	grad.rate:log(100 - percent.fin.aid + epsilon)	0.0060796	0.0205208
on.campus.housingYes:percent.student.loan 0.0149356 0.0082776 on.campus.housingYes:mask.mandated.days -0.0021618 0.0119621 on.campus.housingYes:occupational.degreeYes -0.8963147 0.0024896 on.campus.housingYes:hs.equivalent.degreeYes -0.5515519 0.0392638	grad.rate:gap20repub	-0.0004421	0.0081894
on.campus.housingYes:mask.mandated.days-0.00216180.0119621on.campus.housingYes:occupational.degreeYes-0.89631470.0024896on.campus.housingYes:hs.equivalent.degreeYes-0.55155190.0392638	grad.rate:hs.equivalent.degreeYes	-0.0144991	0.0411769
on.campus.housingYes:occupational.degreeYes -0.8963147 0.0024896 on.campus.housingYes:hs.equivalent.degreeYes -0.5515519 0.0392638	on.campus.housingYes:percent.student.loan	0.0149356	0.0082776
on.campus.housingYes:hs.equivalent.degreeYes -0.5515519 0.0392638	on.campus.housingYes:mask.mandated.days	-0.0021618	0.0119621
	on.campus.housingYes:occupational.degreeYes	-0.8963147	0.0024896
percent.student.loan:hs.equivalent.degreeYes 0.0198189 0.0004598	on.campus.housingYes:hs.equivalent.degreeYes	-0.5515519	0.0392638
	percent.student.loan:hs.equivalent.degreeYes	0.0198189	0.0004598

LASSO Model 2: Coefficient Estimate Trajectories

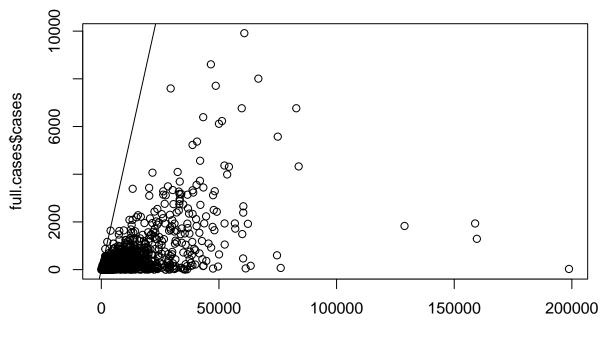


In the end, we lean towards accepting the conclusions presented by the second model: With a wider range of interaction effects to consider, it is less likely that the statistically significant predictors were only marked as such because they help explain a relationship between cases and another predictor with which they are collinear. The conclusion of the LASSO models alone appears to be that there is a statistically significant relationship between religious and cases, and that the nature of this relationship changes based on the value of mask.mandated.days. Interestingly, in LASSO-Selected Model 2, the interaction coefficient religiousYes:mask.mandated.days has a positive coefficient: An increase in the number of mask mandated days during the 2020-21 academic year is associated, in this model, with an increase in the multiplicative change that we would expect for a given school if that school were to have a religious affiliation, compared to if that same school were to not have a religious affiliation. This phenomenon also seems to be present in LASSO-Selected Model 1, in which the coefficient estimate for religious:mask.mandated.days is also positive.

Hierarchical Multi-level Models

Formally test whether the effect of university religious affiliation (on 2020 Covid cases) depends on gap20repub: (it does)

```
## refitting model(s) with ML (instead of REML)
## Data: full.cases
## Models:
## lmer3b: log(cases + 1) ~ gap20repub + religious + (1 | state)
## lmer3: log(cases + 1) ~ gap20repub * religious + (1 | state)
##
          npar
                         BIC logLik deviance Chisq Df Pr(>Chisq)
## lmer3b
             5 7373.9 7401.6 -3682.0
                                       7363.9
             6 7362.8 7395.9 -3675.4
## lmer3
                                       7350.8 13.158 1 0.0002863 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Warning in abline(summary(lmer2)): only using the first two of 9 regression
## coefficients
```



full.cases\$total.headcount

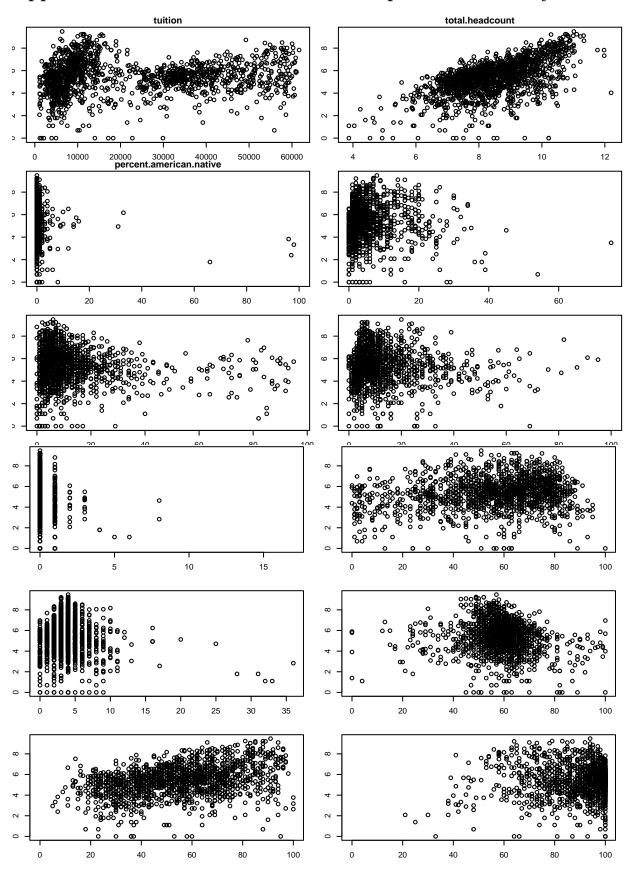
Conclusions

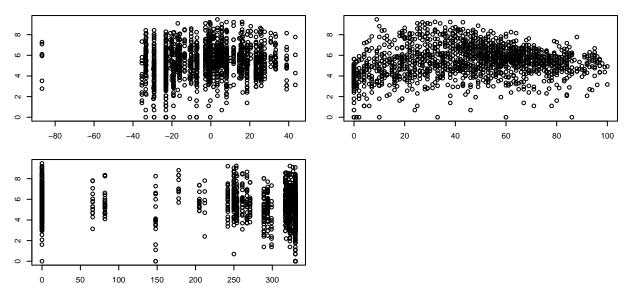
General points to discuss:

- Brief summary of first three sections: Group Testing, Assumptions, 2020/21/total.cases decision
- Linear model recap, determining the significance of religious relies a lot on its interactions
- AIC step comes to similar conclusions?

Discussing inferences: - Which coefficients related to religious (linear and interaction effects) did we find to be significant at each stage of our analyses? - Where the findings differ, which models do we choose to give more credit to? Which findings are we more confident in (based on number of models that support the significance of a predictor)? - Giving the interpretation of every predictor that is discussed?

Appendix A: Plots to Check the Assumption of Linearity





SOME EXPERIMENTING WITH MIXED-EFFECTS MODELS

Warning: Some predictor variables are on very different scales: consider
rescaling