

Step	Algorithm:
1a	
4	where
2	
3	while do
2,3	$\wedge$
5a	where
6	
8	
5b	
7	
2	
	endwhile
2,3	$\wedge \neg ( \quad )$
1b	

Step	<b>Algorithm:</b> $[C] := \text{SYMM\_LU\_BLK\_VAR2}(A, B, C)$
1a	$C = \hat{C}$
4	$B \rightarrow (B_L   B_R), C \rightarrow (C_L   C_R)$ <b>where</b> $B_R$ has 0 columns, $C_R$ has 0 columns
2	$(C_L   C_R) = (\hat{C}_L   \hat{C}_R)$
3	<b>while</b> $n(B_R) < n(B)$ <b>do</b>
2,3	$(C_L   C_R) = (\hat{C}_L   \hat{C}_R) \wedge n(B_R) < n(B)$
5a	<b>Determine block size</b> $b$ $(B_L   B_R) \rightarrow (B_0   B_1   B_2), (C_L   C_R) \rightarrow (C_0   C_1   C_2)$ <b>where</b> $B_1$ has $b$ columns, $C_1$ has $b$ columns
6	$(C_0   C_1   C_2) = (\hat{C}_0   \hat{C}_1   AB_2 + \hat{C}_2)$
8	$C1 := AB_1 + C_1$
5b	$(B_L   B_R) \leftarrow (B_0   B_1   B_2), (C_L   C_R) \leftarrow (C_0   C_1   C_2)$
7	$(C_0   C_1   C_2) = (\hat{C}_0   AB_1 + \hat{C}_1   AB_2 + \hat{C}_2)$
2	$(C_L   C_R) = (\hat{C}_L   \hat{C}_R)$
	<b>endwhile</b>
2,3	$(C_L   C_R) = (\hat{C}_L   \hat{C}_R) \wedge \neg(n(B_R) < n(B))$
1b	$[C] = \text{symm\_lu}(A, B, \hat{C})$

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$B \rightarrow \left( B_L \middle  B_R \right), C \rightarrow \left( C_L \middle  C_R \right)$ <b>where</b> $B_R$ has 0 columns, $C_R$ has 0 columns <b>while</b> $n(B_R) < n(B)$ <b>do</b> <b>Determine block size</b> $b$ $\left( B_L \middle  B_R \right) \rightarrow \left( B_0 \middle  B_1 \middle  B_2 \right), \left( C_L \middle  C_R \right) \rightarrow \left( C_0 \middle  C_1 \middle  C_2 \right)$ <b>where</b> $B_1$ has $b$ columns, $C_1$ has $b$ columns $C1 := AB_1 + C_1$ $\left( B_L \middle  B_R \right) \leftarrow \left( B_0 \middle  B_1 \middle  B_2 \right), \left( C_L \middle  C_R \right) \leftarrow \left( C_0 \middle  C_1 \middle  C_2 \right)$ <b>endwhile</b>

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