

Step	Algorithm:
1a	
4	
	where
2	
3	while do
2,3	\wedge
5a	
	where
6	
8	
5b	
7	
2	
	endwhile
2,3	$\wedge \neg(\quad)$
1b	

Step	Algorithm: $[C] := \text{SYMM_LU_UNB_VAR1}(A, B, C)$
1a	$C = \widehat{C}$
4	$B \rightarrow \left(B_L \middle B_R \right), C \rightarrow \left(C_L \middle C_R \right)$ where B_L has 0 columns, C_L has 0 columns
2	$\left(C_L \middle C_R \right) = \left(\widehat{C}_L \middle \widehat{C}_R \right)$
3	while $n(B_L) < n(B)$ do
2,3	$\left(C_L \middle C_R \right) = \left(\widehat{C}_L \middle \widehat{C}_R \right) \wedge n(B_L) < n(B)$
5a	$\left(B_L \middle B_R \right) \rightarrow \left(B_0 \middle b_1 \middle B_2 \right), \left(C_L \middle C_R \right) \rightarrow \left(C_0 \middle c_1 \middle C_2 \right)$ where b_1 has 1 column, c_1 has 1 column
6	$\left(C_0 \middle c_1 \middle C_2 \right) = \left(AB_0 + \widehat{C}_0 \middle \widehat{c}_1 \middle \widehat{C}_2 \right)$
8	$c_1 := Ab_1 + c_1$
5b	$\left(B_L \middle B_R \right) \leftarrow \left(B_0 \middle b_1 \middle B_2 \right), \left(C_L \middle C_R \right) \leftarrow \left(C_0 \middle c_1 \middle C_2 \right)$
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2	$\left(C_L \middle C_R \right) = \left(\widehat{C}_L \middle \widehat{C}_R \right)$
	endwhile
2,3	$\left(C_L \middle C_R \right) = \left(\widehat{C}_L \middle \widehat{C}_R \right) \wedge \neg(n(B_L) < n(B))$
1b	$[C] = \text{symm_lu}(A, B, \widehat{C})$

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