

Step	Algorithm:
1a	
4	where
2	
3	while do
2,3	\wedge
5a	where
6	
8	
5b	
7	
2	
	endwhile
2,3	$\wedge \neg(\quad)$
1b	

Step	Algorithm: $[C] := \text{SYMM_LU_BLK_VAR1}(A, B, C)$
1a	$C = \widehat{C}$
4	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right), B \rightarrow \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right), C \rightarrow \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right)$ where A_{TL} is 0×0 , B_T has 0 rows, C_T has 0 rows
2	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right)$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right) \wedge m(A_{TL}) < m(A)$
5a	Determine block size b $\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \rightarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$ where A_{11} is $b \times b$, B_1 has b rows, C_1 has b rows
6	$\left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right) = \left(\begin{array}{c} A_{00}B_0 + A_{01}B_1^T + A_{02}B_2 + \widehat{C}_0 \\ \hline A_{01}^T + \widehat{C}_1 \\ \hline A_{02}^T B_0 + \widehat{C}_2 \end{array} \right)$
8	$C_1 := A_{11}B_1 + A_{12}B_2 + C_1$ $C_2 := A_{12}^T B_1 + C_2$
5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$
7	$\left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right) = \left(\begin{array}{c} A_{00}B_0 + A_{01}B_1 + A_{02}B_2 + \widehat{C}_0 \\ \hline A_{01}B_0 + A_{11}B_1 + A_{12}B_2 + \widehat{C}_1 \\ \hline A_{02}B_0 + A_{12}B_1 + \widehat{C}_2 \end{array} \right)$
2	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right)$
	endwhile
2,3	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right) \wedge \neg(m(A_{TL}) < m(A))$
1b	$[C] = \text{symm_lu}(A, B, \widehat{C})$

Algorithm: $[C] := \text{SYMM_LU_BLK_VAR1}(A, B, C)$

$$A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right), B \rightarrow \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right), C \rightarrow \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right)$$

where A_{TL} is 0×0 , B_T has 0 rows, C_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

Determine block size b

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \rightarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$$

where A_{11} is $b \times b$, B_1 has b rows, C_1 has b rows

$$C_1 := A_{11}B_1 + A_{12}B_2 + C_1$$

$$C_2 := A_{12}^T B_1 + C_2$$

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$$

endwhile

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5a	Determine block size
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	endwhile
2,3	$\wedge \neg(\quad)$
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Step	Algorithm: $[C] := \text{SYMM_LU_BLK_VAR1}(A, B, C)$
1a	$C = \widehat{C}$
4	where
2	$\left(\frac{C_T}{C_B} \right) = \left(\frac{A_{TL}B_T + A_{TR}B_B + \widehat{C}_T}{A_{TR}^T B_T + \widehat{C}_B} \right)$
3	while do
2,3	$\left(\frac{C_T}{C_B} \right) = \left(\frac{A_{TL}B_T + A_{TR}B_B + \widehat{C}_T}{A_{TR}^T B_T + \widehat{C}_B} \right) \wedge$
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	endwhile
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2,3	$\left(\frac{C_T}{C_B} \right) = \left(\frac{A_{TL}B_T + A_{TR}B_B + \widehat{C}_T}{A_{TR}^T B_T + \widehat{C}_B} \right) \wedge \neg(m(A_{TL}) < m(A))$
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2	$\begin{pmatrix} C_T \\ C_B \end{pmatrix} = \begin{pmatrix} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ A_{TR}^T B_T + \widehat{C}_B \end{pmatrix}$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\begin{pmatrix} C_T \\ C_B \end{pmatrix} = \begin{pmatrix} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ A_{TR}^T B_T + \widehat{C}_B \end{pmatrix} \wedge m(A_{TL}) < m(A)$
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5a	Determine block size b $\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \rightarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$ where A_{11} is $b \times b$, B_1 has b rows, C_1 has b rows
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5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$
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2	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right)$
	endwhile
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6	$\left(\begin{array}{c} C_0 \\ C_1 \\ C_2 \end{array} \right) = \left(\begin{array}{c} A_{00}B_0 + A_{01}B_1^T + A_{02}B_2 + \widehat{C}_0 \\ A_{01}^T + \widehat{C}_1 \\ A_{02}^T B_0 + \widehat{C}_2 \end{array} \right)$
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5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ B_1 \\ B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ C_1 \\ C_2 \end{array} \right)$
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2	$\left(\begin{array}{c} C_T \\ C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ A_{TR}^T B_T + \widehat{C}_B \end{array} \right)$
	endwhile
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6	$\left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right) = \left(\begin{array}{c} A_{00}B_0 + A_{01}B_1^T + A_{02}B_2 + \widehat{C}_0 \\ \hline A_{01}^T + \widehat{C}_1 \\ \hline A_{02}^T B_0 + \widehat{C}_2 \end{array} \right)$
8	$C_1 := A_{11}B_1 + A_{12}B_2 + C_1$ $C_2 := A_{12}^T B_1 + C_2$
5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$
7	$\left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right) = \left(\begin{array}{c} A_{00}B_0 + A_{01}B_1 + A_{02}B_2 + \widehat{C}_0 \\ \hline A_{01}B_0 + A_{11}B_1 + A_{12}B_2 + \widehat{C}_1 \\ \hline A_{02}B_0 + A_{12}B_1 + \widehat{C}_2 \end{array} \right)$
2	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right)$
	endwhile
2,3	$\left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) = \left(\begin{array}{c} A_{TL}B_T + A_{TR}B_B + \widehat{C}_T \\ \hline A_{TR}^T B_T + \widehat{C}_B \end{array} \right) \wedge \neg(m(A_{TL}) < m(A))$
1b	$[C] = \text{symm_lu}(A, B, \widehat{C})$

Step	Algorithm: $[C] := \text{SYMM_LU_BLK_VAR1}(A, B, C)$
	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right), B \rightarrow \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right), C \rightarrow \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right)$ <p>where A_{TL} is 0×0, B_T has 0 rows, C_T has 0 rows</p>
	while $m(A_{TL}) < m(A)$ do
	<p>Determine block size b</p> $\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \rightarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$ <p>where A_{11} is $b \times b$, B_1 has b rows, C_1 has b rows</p>
	$C_1 := A_{11}B_1 + A_{12}B_2 + C_1$ $C_2 := A_{12}^T B_1 + C_2$
	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c c c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$
	endwhile

Algorithm: $[C] := \text{SYMM_LU_BLK_VAR1}(A, B, C)$

$$A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right), B \rightarrow \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right), C \rightarrow \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right)$$

where A_{TL} is 0×0 , B_T has 0 rows, C_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

Determine block size b

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \rightarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$$

where A_{11} is $b \times b$, B_1 has b rows, C_1 has b rows

$$C_1 := A_{11}B_1 + A_{12}B_2 + C_1$$

$$C_2 := A_{12}^T B_1 + C_2$$

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline 0 & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} A_{00} & A_{01} & A_{02} \\ \hline 0 & A_{11} & A_{12} \\ \hline 0 & 0 & A_{22} \end{array} \right), \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline B_1 \\ \hline B_2 \end{array} \right), \left(\begin{array}{c} C_T \\ \hline C_B \end{array} \right) \leftarrow \left(\begin{array}{c} C_0 \\ \hline C_1 \\ \hline C_2 \end{array} \right)$$

endwhile