

**Problem Set 9 —Key**  
CENG 340—Introduction to Environmental Engineering  
Instructor: Deborah Sills  
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1. (12.5 pts) **Monod Kinetics**

A kinetic study of the bacterial utilization of methanol was conducted and yielded the following data:

Substrate, S (mg/L)	dS/dt ( $\frac{\text{mg}}{\text{L} \times \text{hr}}$ )
2	1
4	1.5
6	1.8
8	2
10	2.14

S = concentration of methanol.

In addition, biomass concentration (bacterial concentration, X) was maintained at a constant 100 mg/L during the study.

- (a) From this data, determine the parameters for a Monod substrate utilization model, presented below.

$$-\frac{dS}{dt} = \frac{\mu_{\max}XS}{K_s + S} \quad (1)$$

The model was fit to Eq.1 using Kaleidagraph's non-linear curve fitting package. The data and model fit are presented in Figure 1.

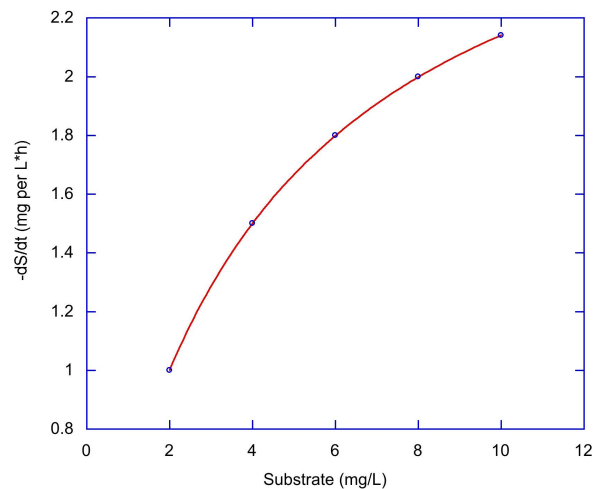


Figure 1: Growth rate of microorganisms as a function of substrate concentration. Circles represent data and the line represents a model fit.

The fitted parameters are as follows:

$$\mu_{max} = 0.03 \frac{\text{mg S}}{\text{mg X} \times \text{h}} = 0.72 \frac{\text{mg S}}{\text{mg X} \times \text{day}}$$

$$K_s = 4 \text{ mg/L}$$

- (b) This model can be used to predict the concentration of methanol in a well-mixed pond that has an indigenous bacteria population close to that used in the kinetic study above. The concentration of the bacteria in the pond is, however, 10% of that of the kinetic study, and this bacterial concentration is relatively constant in the pond. Determine the methanol concentration in the pond 5 days after the pond was contaminated with 200 mg/L of methanol. Assume the pond behaves as a batch reactor (no inflow/outflow) and that no methanol escapes by evaporation. Hint: employ the “diphasic” or “mixed-order” Monod model.

Since S is much bigger than  $K_s$ , Eq. 1 simplifies to a zero-order equation presented as Eq. 2:

$$-\frac{dS}{dt} = \mu_{max}X \quad (2)$$

Eq. 2 can be integrated, resulting in Eq. 3:

$$-(S(t) - S(0)) = \mu_{max}Xt \quad (3)$$

Eq. 3 can be rearranged resulting in Eq. 4:

$$S(t) = S(0) - \mu_{max}Xt \quad (4)$$

Inputting numbers results in:

$$S(5) = 200 \frac{\text{mg}}{\text{L}} - 0.72 \frac{\text{mg S}}{\text{mg X} \times \text{day}} \times 10 \frac{\text{mg X}}{\text{L}} \times 5 \text{ day}$$

$S = 164 \text{ mg/L}$ , which is still much bigger (at least one order of magnitude bigger) than  $K_s$ . In other words, the zero-order equation is still valid.

$$S = \frac{K_s(1 + k_d\theta_c)}{\theta_c(\mu_{max} - k_d) - 1}$$

$$\theta_{c(\min)} = \frac{1}{\mu_{max} - k_d}$$