



WORKSHOP ON LINEAR REGRESSION

DAY-1

WHAT IS LINEAR REGRESSION?

- Statistical approach:
 - Linear regression attempts to model the relationship between two variables by fitting a linear equation to observed data.
 - Machine learning approach:
 - Linear regression is used to predict a quantitative response Y from the predictor variable X with an assumption that there's a linear relationship between X and Y .
- They are SAME!

Machine Learning

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graph TD; ML[Machine Learning] --> S[Supervised]; ML --> U[Unsupervised]; ML --> R[Reinforcement]
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Supervised

Unsupervised

Reinforcement

LINEAR REGRESSION COMES UNDER SUPERVISED LEARNING

why?

Because the training data are labelled.

OVERVIEW

What is Linear Regression?

- A supervised algorithm that learns from a set of training samples

What is the objective?

- Find the best fitted LINE based on training data

As a data scientist what is your outcome of interest?

- Estimation, Prediction and validation of your model

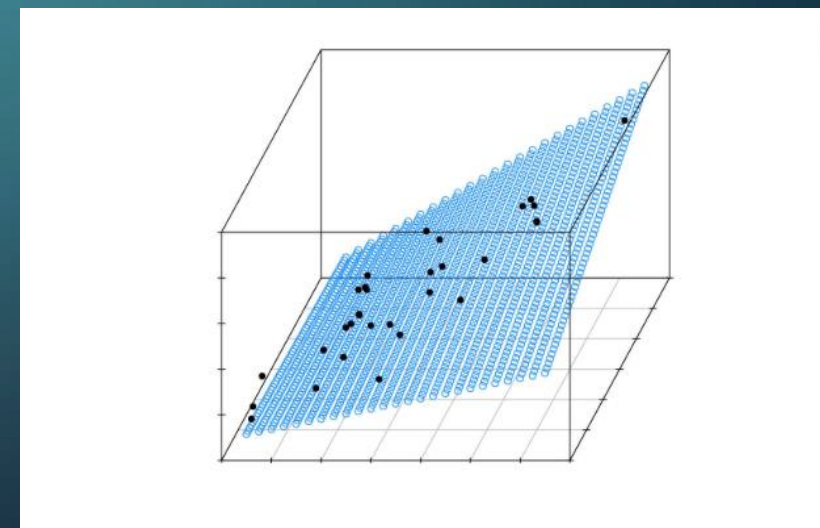
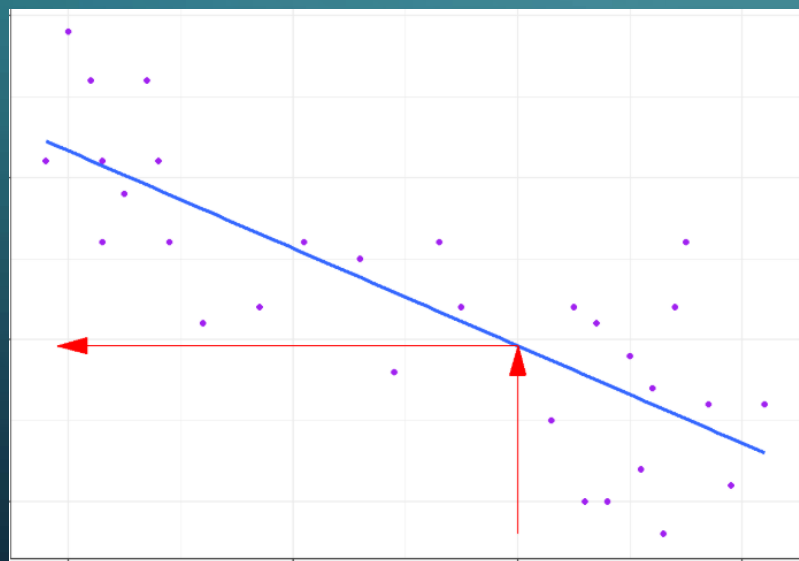
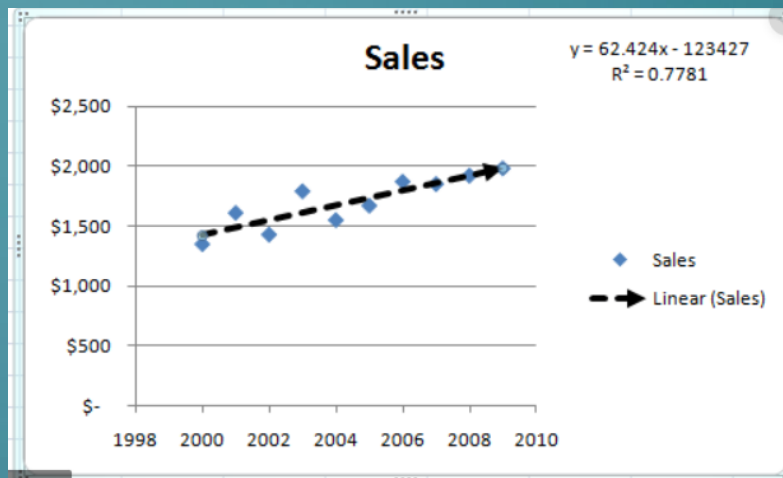
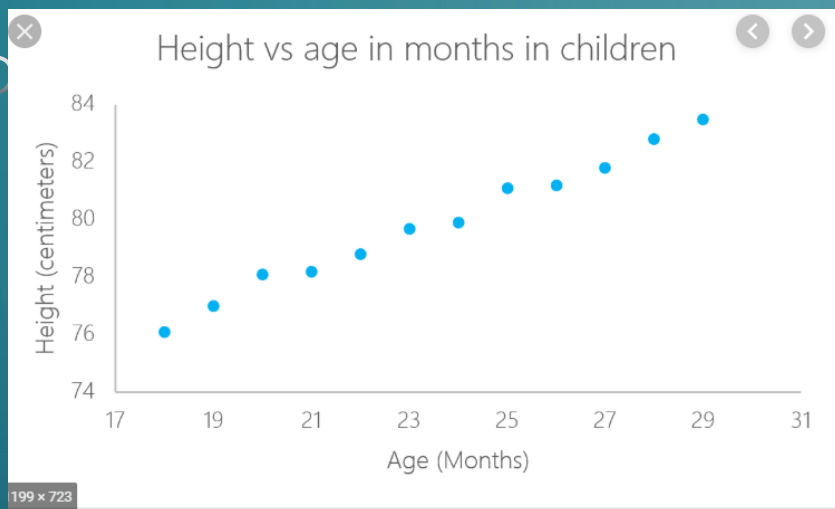
How can I solve it?

- By fitting the "BEST" line between the output variable (response) input variable (explanatory).

How do I know my answer is good?

- We need to test for proximity of training data and fitted data.

Few Examples of linear regression:



IMPORTANT ASPECTS OF REGRESSION

Assumption

- What assumptions we need to make?

Fixed part Random

2. $\epsilon \sim \text{iid } N(0, \sigma^2)_{\text{part}}$
3. a and b are fixed and unknown
4. Other assumptions are beyond our scope

Estimation

- We need to find a and b based on some criteria
- What criteria?
- The estimated value should be very close to the predicted value
based on training data

Validation

- How do I know my model is good?
- -- check how close the predicted values (**that you modelled**) to the actual value(**obtained from training data**). (Closer they are, the better your model is)
- (Measurement tool:
- p value, t statistic etc..)

CASE STUDY ON AGE AND SALARY

PROBLEM

Consider predicting the salary of an employee based on his/her age. We can easily identify that there seems to be a correlation between employee's age and salary (more the age more is the salary).

SOLUTION



$$\text{Salary} = \text{age} * 3000 + 500$$

P value= .005

IMPORTANT ASPECTS OF REGRESSION

Assumption

- What assumptions we need to make?

1. $y = ax + b + \epsilon$

$\underbrace{ax + b}_{\text{Fixed part}} \quad \downarrow \epsilon_{\text{Random part}}$

- $\epsilon \sim \text{iid } N(0, \sigma^2)$
- a and b are fixed and unknown
- Other assumptions are beyond our scope

Estimation




- $a = 3000$
- $b = 500$


Validation

- $p \text{ value} = .005$ is smaller than a predefined threshold (.05).
- So the model seems to be good, based on the training data set and our initial assumptions; age seems to explain a significant amount of variation in salary



FOOD FOR THOUGHT

- If we keep increasing the age, will salary keep increasing?
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BLAKE HAMMENT AND KEMIL HERATH
WILL ELABORATE THE CONCEPTS
WITH A PRACTICAL EXAMPLE IN THE
NEXT SESSION.

TO DO ITEMS FOR MEMBERS:

1. PLEASE INSTALL PYTHON AND R IN YOUR LAPTOP
2. BRING YOUR LAPTOP IN THE NEXT SESSION
3. FAMILIAR YOURSELF WITH DIFFERENT TERMS OF MACHINE LEARNING:
 - a) Data sets (Training data, Validation data, Test data)
 - b) Supervised learning, Unsupervised learning
 - c) Overfitting, Underfitting