

ABSTRACT

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CONTENTS

1	INTRODUCTION	1
2	THEORY	3
2.1	Point spread function	3
2.1.1	Atmosphere	5
2.1.2	Adaptive Optics	5
2.2	Vector Apodizing Phase Plate	6
2.3	Disks	7
2.3.1	Categorization and features	7
2.3.2	Expected Contrast	8
2.4	Angular differential Imaging	8
3	DATA GENERATION	11
3.1	Disk model	11
3.2	Atmospheric Distortions	12
3.2.1	Fourier method	12
3.2.2	Using HCIPy	13
3.3	Generating observations	14
4	DATA REDUCTION	17
4.1	Pre-Processing	17
4.2	Angular differential imaging	17
4.2.1	Algorithme	17
4.2.2	Control	18
4.3	Paremater Study	18
5	RESULTS	21
6	DISCUSSION	25
	BIBLIOGRAPHY	27

LIST OF FIGURES

Figure 1	Optical layout of a Lyot coronagraph, by Matthew Kenworthy, from https://home.strw.leidenuniv.nl/~kenworthy/app	1
Figure 2	The point spread function (PSF) is the image an instrument produces when looking at a point source such as a star. Here we see the PSF of an instrument without a coronagraph, with the classical Lyot coronagraph and a one using the vector Apodizing Phase Plate (vAPP)	2
Figure 3	Fraunhofer diffraction from an arbitrary aperture, r and R large compared to the size of the hole. Extracted from Optics 5th edition, by [4].	4
Figure 4	Sketch showing the basic principle of an Adaptive Optics (AO) system, adapted from UC Berkeley science review: Into focus, Credit: Keith Cheveralls.	6
Figure 5	Sketch summarizing the different classifications of protoplanetary disks proposed in [2].	8
Figure 7	Two disks created by the model with different size and inclination both with a position angle of 45 degrees.	12
Figure 8	The Pattern used and the differences between PSFs distorted with it using the method described above.	13
Figure 9	Differences between the first psf of an observation and later psfs. Compared between simulated observations on the left and on sky data on the right. The psfs were aligned then normalised on the maximum of the leakage term, finally the absolute value of the difference between the first and n -th psf was taken. The second, 10th and 50th simulated psf are 0.7, 7 and 14 seconds apart in the simulation.	16
Figure 10	A generated exposure through the Pre-processing process, first it is aligned and then its right and left **psf kernel** are extracted.	18

Figure 11	The right and left end result of Angular Differential Imaging (ADI) applied to a generated exposure stack of a star. The stack contains 20 exposures, the field rotation over the entire stack is 60° . Note how derotating the fields leads to a circular result as we lose the angles.	19
Figure 12	Results of appying ADI to disk model A	22
Figure 13	Results of appying ADI to disk model B	23

ACRONYMS

PSF	point spread function.....	3
vAPP	vector Apodizing Phase Plate	7
APP	Apodizing Phase Plate.....	6
AO	Adaptive Optics	5
HCIPy	high-contrast imaging python.....	13
ADI	Angular Differential Imaging.....	8
FWHM	full width half maximum.....	25

INTRODUCTION

A major and successful topic in astronomy has been the discovery and characterization of exoplanets. This interest has sparked great progress in the field of high contrast imaging resulting in new imaging techniques and instruments. At the time of writing 3,949 planets have been confirmed though little is known about their formation. Certain is that a so called protoplanetary disk is an important stage in the formation of a planetary system. The disks can be observed within the visible spectrum, near infrared and radio. Each wavelength probes different molecules materials and processes. ALMA has been succesfull in mapping emissins from molecules while optial and near infrared map the scattert light from the disk.

It is however a great challenge to observe a disk in the optical and infrared due to the high contrast between the disk and its star at the required angular resolution. For ground-based observations adaptive optics are used. This negates most of the atmospheric seeing.

Reducing contrast is done with coronagraph, an instrument that blocks the light from a star. The classic Lyot coronagraph blocks the star light in the focal-plane (see: [Figure 1](#)). In the focus an opaque mask is placed, it scatters the stars light. Then in the pupil-plane a ring shaped mask blocks most of the now scatterd star light. Then at the second focus the image is made as usual.

A Lyot coronagraph it not able to observe disks close to stars. The vAPP [12] is a type of coronagraph placed at the pupil of a telescope. The vAPP blocks starlight by modifying the phase of incoming light. This phase change flips the light in a D-shaped region around the star to the other side. Any faint object next to the star in the now dark region becomes detectable. Compared to the classic Lyot coronagraph the vAPP reduces can allow starlight to a greater degree, see [Figure 2](#).

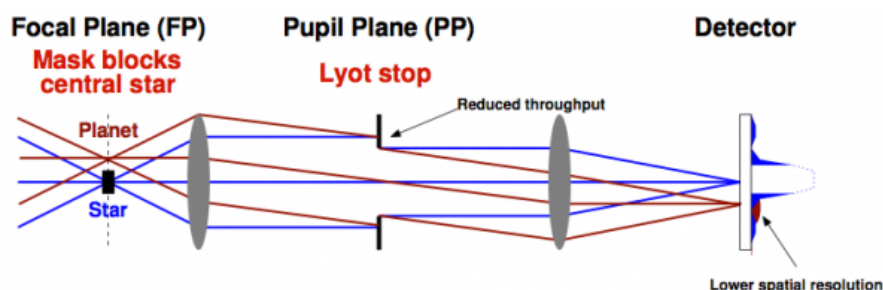
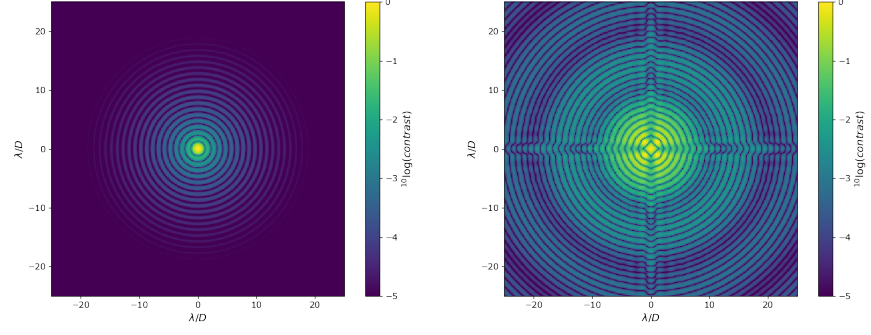
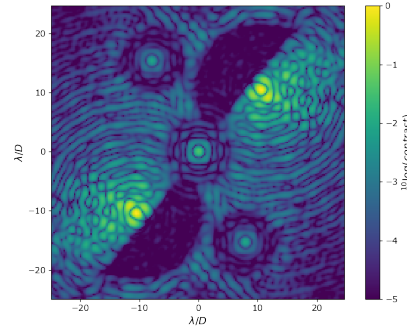


Figure 1: Optical layout of a Lyot coronagraph, by Matthew Kenworthy, from <https://home.strw.leidenuniv.nl/~kenworthy/app>



(a) PSF of a telescope without coronagraph.

(b) PSF of a classical Lyot coronagraph.



(c) PSF of the vAPP.

Figure 2: The PSF is the image an instrument produces when looking at a point source such as a star. Here we see the PSF of an instrument without a coronagraph, with the classical Lyot coronagraph and one using the vAPP.

The vAPP has mainly been developed to detect exoplanets. However it could also allow us to resolve disk features and study disks in greater detail directly. However as the vAPP has a peculiar PSF and the entire disk will never lie within one of the dark zones it might prove challenging to differentiate disk features from the PSF's features.

ADI is a technique to remove stationary and slowly changing PSF structures from an exposure. It does so by rotating the field of view while keeping the PSF still. It has been well proven for the detection of stellar companions such as exoplanets however it has not been applied to disks. ADI removes rotational symmetry, therefore it might create large scale distortions in the result.

Here we study what the effect is of both the vAPP and ADI on the apparent morphology of disks.

overview thesis

THEORY

Here we discuss what an point spread function (PSF) is, how it helps us describe an optical system and how they naturally appear from basic optics. Then we look at the different types of disks that have been observed and what contrasts we expect.

2.1 POINT SPREAD FUNCTION

We can describe what happens to light going through an optical system with its PSF. It describes the light intensity on the focal-plane (where the science detector is) as a function of x and y when a single point source is imaged on the center of the focal-plane.

Light is an propagating electromagnetic wave. We derive how to find the PSF from the Huygens-Fresnel Principle. It states any part of a wave can be described as a front of infinitely many point sources interfering with one another. An optical element can change these arrangement of theses sources, for example an aperture allows only a small area to be filled with these point sources as illustrated in [Figure 3](#).

We find the electric field at a point P at distance R by summing up the fields of these infinite point sources taking into account the different distances to R . Writing the infinite sum as an integral we get ?? for the electric field at a point P some distance R from an aperture.

$$E = \frac{\epsilon_A e^{i(\omega t - kR)}}{R} \iint_{\text{Aperture}} e^{ik(Yy + Zz)/R} dy dz \quad (1a)$$

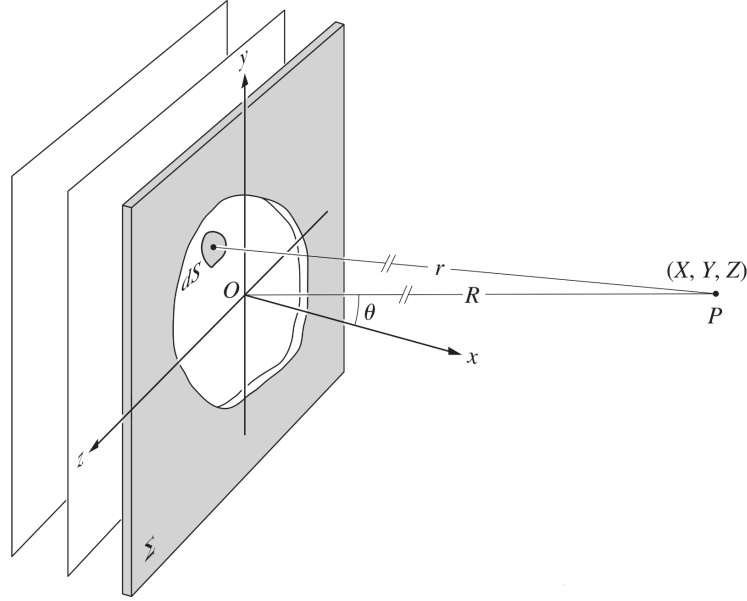
Here Y, Z describe the position in the imaging plane in which P lies as seen in [Figure 3](#). Small letters y and z are the position in the aperture plane. The integral is over the aperture, only integrating over the transparent parts.

Here we integrate only over the apperture and assume all light is transmitted within and no light outside of it. To allow for changes in phase and magnitude caused by for example dirty glass, or a complicated Optical instrument we including an aperture function and integrate over all space.

$$\mathcal{A}(y, z) = \mathcal{A}_0(y, z) e^{i\phi(y, z)} \quad (2)$$

Here the time changing electromagnetic wave ϵ is averaged into a constant field of magnitude one. Then the transmission through the aperture changes the magnitude (\mathcal{A}_0) and the phase ($\phi(y, z)$).

Figure 3: Fraunhofer diffraction from an arbitrary aperture, r and R large compared to the size of the hole. Extracted from Optics 5th edition, by [4].



$$E(Y, Z) = \iint_{-\infty}^{\infty} \mathcal{A}(y, z) e^{ik(Yy + Zz)/R} dy dz \quad (1b)$$

The expression for the E field at the point P (??) rewritten to make use of the aperture function.

We can rewrite this to get rid of the dependence on the distance by substituting $K_y = kY/R$ and $K_z = kZ/R$ for Y and Z . This gives the final form:

$$E(K_Y, K_Z) = \iint_{-\infty}^{\infty} \mathcal{A}(y, z) e^{ik(K_Y y + K_Z z)/R} dy dz \quad (1c)$$

This is the 2 dimensional Fourier transformation of the aperture function. Thus “the field distribution in the Fraunhofer diffraction pattern is the Fourier transform of the field distribution across the aperture (e.i., the aperture function)” [4]. Here the fraunhofer diffraction pattern is the instruments focal-plane.

For the PSF we are interested in the intensity which is not the electric field E but $|E|^2$. This means we can calculate the PSF of an instrument by Fourier transforming its (complex) aperture function and squaring the result. Note that the amplitude in the aperture function

does not only have to depend on the shape of the aperture as there might be partially transparent material. We can use it to simulate any optical instrument such as the vector Apodizing Phase Plate (vAPP).

With the PSF we know how a single point source would look when imaged by an optical system. If we assume the system is linear system we can use the superposition principle to image extended sources by convolving the PSF with the extended source.

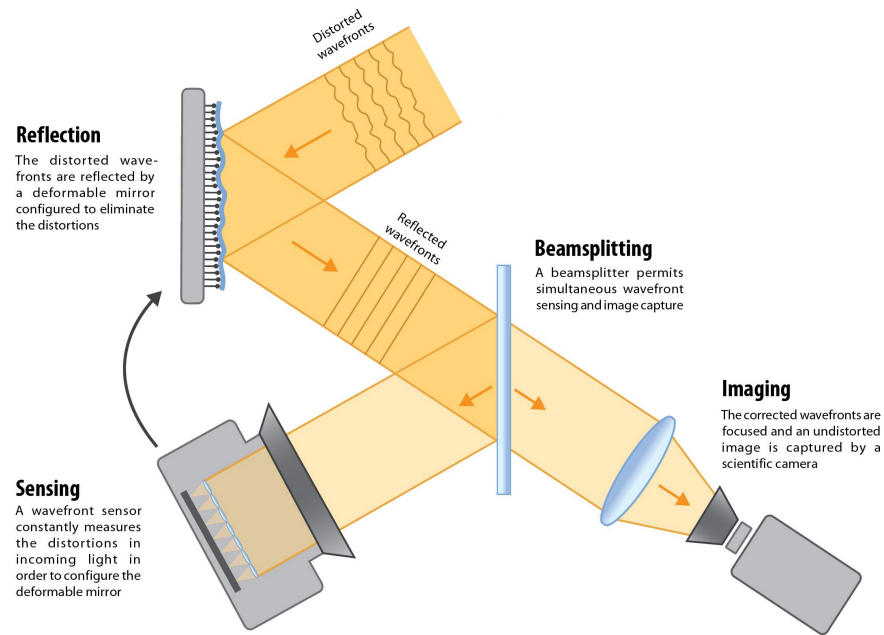
2.1.1 *Atmosphere*

The telescope or coronagraph are the only optical system at play. There are many differently moving layers of air between the telescope and space. These work as independent optical systems that change in time. The varying temperature and humidity between and within layers changes the air's refractive index resulting in phase changes. Each layer moves in a different direction at a different speed as winds differ between altitudes. Combined this causes the complete PSF to change continuously. The changes are smaller at smaller timescales as the layers move less far and temperature and humidity change less.

2.1.2 *Adaptive Optics*

Since the 1990's Adaptive Optics (AO) are used. They change utilise an adaptive mirror that can change its shape to undo the phase change of the atmosphere, see [Figure 4](#). To do this they first need to measure the errors in the wavefront. However as a measurement costs some limited time the lag behind the actual shape of the wavefront. Furthermore they have errors themselves, the phase is never completely corrected. Both these effects cause small distortions in the final image. Thus even with AO the total PSF for the atmosphere, the AO and the instrument will keep changing in time, however the magnitude of the change is severely reduced. Adaptive optics do not correct the entire field, generally each system has a control radius around the star in which the AO can reduce the seeing.

Figure 4: Sketch showing the basic principle of an AO system, adapted from UC Berkeley science review: Into focus, Credit: Keith Cheveralls.



2.2 VECTOR APODIZING PHASE PLATE

As mentioned in the introduction, the vector apodizing phase plate is not a normal coronagraph. The Apodizing Phase Plate (APP) is a coronagraph that changes the phase in the pupil-plane to create destructive interference in an area of the PSF. Imaged this creates a dark zone in the PSF. Dim objects can be imaged if the contrast between them and the star is smaller than the contrast between center peak of the PSF and the dark zone. The contrast can be higher if post processing techniques such as Angular Differential Imaging (ADI) are used (see [Section 2.4](#)).

As the coronagraph works in the pupil-plane it is insensitive to the effects of tip tilt errors, these are caused by vibrations in the telescope. Furthermore unresolved stars do not limit how close to a star the coronagraph can function.

The APP does this by introduces differences in the optical path length thereby changing the phase. These changes are designed to create the mentioned dark zone in the shape of a 180° half circle with a radius of 2 to $9 \lambda/D$ [1]. To do so optical the path length differences need to be different throughout the pupil, the design can be seen as a heightmap of path differences. The APP is manufactured by diamond turning glass.

The vector Apodizing Phase Plate (vAPP) iterates on the the idea of the APP. Instead of modifying the optical path length, it introduces the phase using the geometrical properties of a liquid crystal plate. The two circular polarisations receive opposite phase and create dark holes at opposite sides of the PSF [12] [10] [1]. By then splitting the right and left handed light and imaging both seperated we get not 180° of dark zone but 360° solving one of the major problems of the APP at a cost of brightness. The vAPP is manufactured with liquid crystals..

2.3 DISKS

With the formation of a star it is inevitable a disk will form due to to the conservation of angular momentum. While initially material will orbit in various directions and planes these will slowly cancel out due to collisions and attraction leaving the average plane and direction as the final orientation of a disk around the star. It seems likely these disk will allow the formation of planets due to the high detection rate of exoplanets [13].

The formation of discs goes through 3 main stages[13]. Only the last stage allows direct imaging in the near-IR and optical bands though all are observable in Radio:

1. Right after the molecular core collapses, most mass is still in a cloud surrounding the disk and the star. Due to that it is not possible to see the disk in the near-IR or optical regime.
2. Most mass moves into the star, the disk is obstructed by outflow of mass. The enveloping mass is about the same as the disks.
3. Central star becomes visible, the enveloping dust has cleared and the disk only contains a few percent of the total mass. It now is a protoplanetary disk.

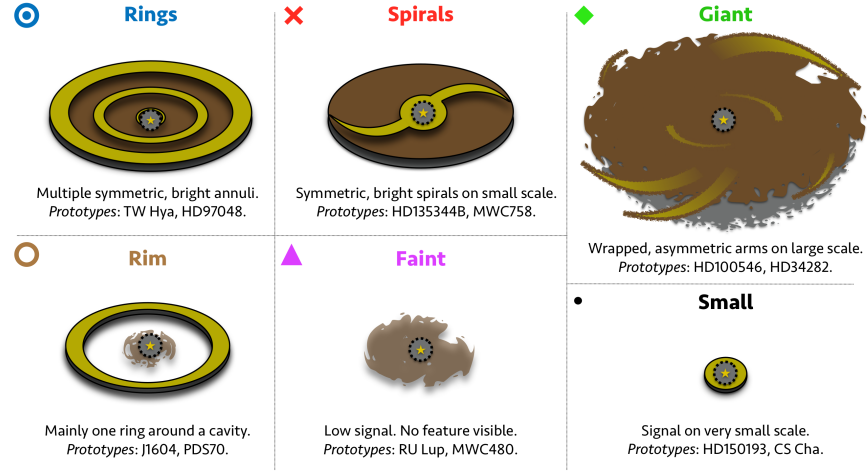
During the first two stages the star is still forming, the disk is obstructed by dust and they take a relatively short time. However at the third stage we should be able to study the disk. After this stage planets can form, their formation process is uncertain.

2.3.1 Categorization and features

It is suspected the disks features are linked to the formation of planets. Rings in a disk could indicate a planet embedded in the disk [6] however those planets can currently not be detected. There is also evidence that spirals in disks can be caused by planets in the disk [2]. This means the morphology of disks can provide valuable insight in how planets form.

Disks seem to be ring or spiral shaped with some forms in between. They can be classified into 6 categories [2] see Figure 5.

Figure 5: Sketch summarizing the different classifications of protoplanetary disks proposed in [2].



With this categorization they [2] further conclude:

- faint disks are young
- spiral disks are around stars that almost start their main sequence
- ring disk have no outer stellar companion

Furthermore they [2] conclude that in small disks of 10 to 20 Au in size and young faint disks structures remain undetected.

2.3.2 Expected Contrast

To get an upper limit on the brightness of a disk we assume all star light that hits the disk is scattered towards us. The light from a star drops quadratically as it gets farther away. Thus we will never have a disk brightness exceeding $1/R^2$. A disk at 1 AU from an sun like star will have a brightness 2.1×10^{-5} of the star. At 5 AU this drops to 8.6×10^{-7} . This is the minimal contrast we can expect, as the density of the disk might make it less the optically thick.

2.4 ANGULAR DIFFERENTIAL IMAGING

Angular Differential Imaging (ADI) is a technique to remove stationary and slowly changing PSF structures from an exposure. It is a proven method for the detection of companions with classic PSFs such as the one in Figure 2a.

The basis of ADI is to let the field of view rotate with respect to the coronagraph and sensor during an observation. By then taking multiple short exposures anything off center will be rotated a bit in each exposure. If the mean of all other exposures is subtracted from an exposure we lose most of the stars PSF. Once done for every exposure, rotating all the results so the field of view is aligned the median can be taken which gives the final image.

To use ADI with the vAPP we need to make sure the entire sequence fits in the dark hole.

DATA GENERATION

There are no observations of disks with the vAPP here we describe how we generate observations using a disk model and PSFs. This presents a number of advantages though the main reason is the lack of disk observations using the vAPP. Generating the data from a model allows us to vary parameters as we wish. We can try a reduction method on a simple slightly inclined disk or a near face on disk with many rings. By reducing images with varying disk morphology we can map how a reduction method performs for each disk morphology. Most importantly we can clearly separate artifacts created during data reduction from disk features when we know what the disk looks like.

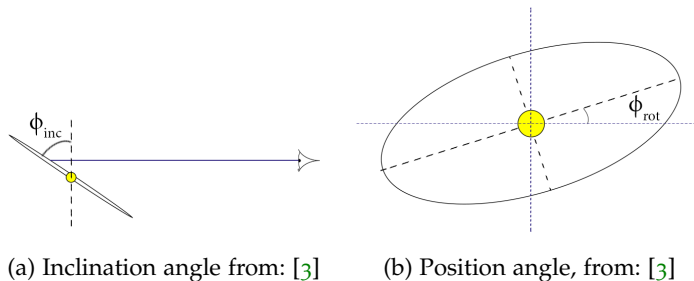
3.1 DISK MODEL

We use a 2-dimensional disk model based on the work by [3]. The model has 4 basic parameters:

INCLINATION The angle the disk is tilted towards the observer. A 0 degrees inclination gives a face on disk and 90 degrees a horizontal line being an edge on disk. As illustrated in Figure 6b

POSITION ANGLE After inclination the disk can be rotated around the line of sight from the observer, rotation to the left is positive. See Figure 6a

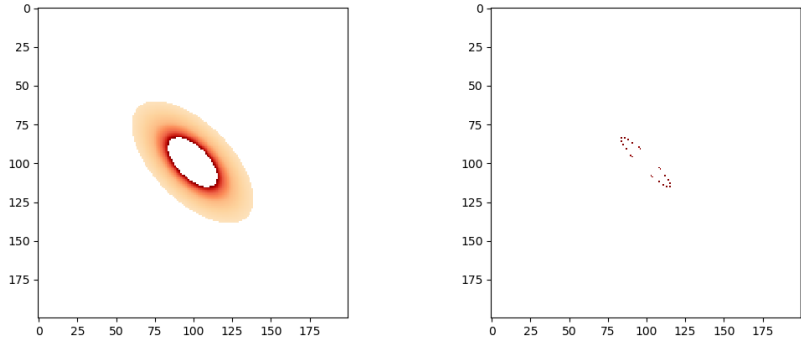
INNER AND OUTER RADIUS Many disks start and stop at some radius from star. The inner and outer radius are relative to the field size that defaults to 10. An Inner radius of 2 gives a hole in the disk with a diameter 20% of the image width.



The disk is modeled as optically thick and does not emit light on its own. At a certain radii between the inner and outer radii the disks brightness is given by:

$$B(r) = B_{\text{star}} \cdot \left(\frac{r}{R_{\text{star}}} \right)^2 \quad (3)$$

We evaluate the model onto an image of 200 by 200 pixels. This speeds up calculations and is similar to the resolution of observed vAPP datasets. The model behaves well for most disks however on this resolution features that are small in the observers plane are pixilated as we see in [Figure 7](#) below. This poses no problem as we do not expect to resolve such features.



(a) Model output for an inclination of 60 deg, an inner radius of 2 and an outer radius of 5. (b) Model output for an inclination of 80 deg, an inner radius of 2.2 and an outer radius of 2.3.

Figure 7: Two disks created by the model with different size and inclination both with a position angle of 45 degrees.

3.2 ATMOSPHERIC DISTORTIONS

To simulate an observation we do not use a single given psf. Since during an observation the combined psf of the atmosphere and instrument changes. However a complete simulation of these effects is outside the scope of the thesis. Instead try and approach a similar morphology to a on sky psf, with similar changes in time. We try two different methods, adding distortions on top of an existing vAPP PSF and adding an atmosphere simulation to the PSF generation. Finally we compare the result of each method to on sky observations.

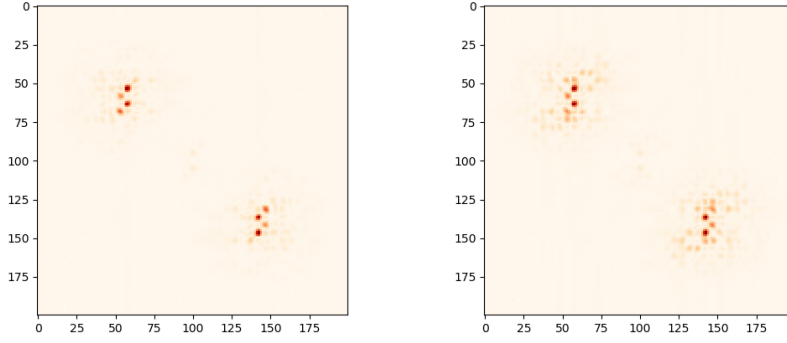
3.2.1 Fourier method

First we tried modifying a give single vAPP psf to get a set of disturbed psfs. To achieve this a pattern is added to the foerier transform of the

psf before transforming it back from foerier space, see the equation below. The pattern is then shifted for every timestep.

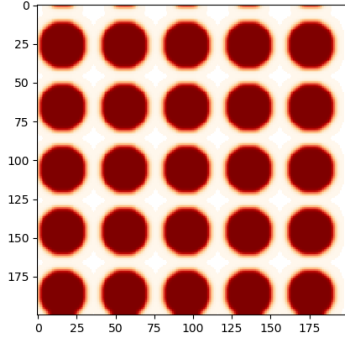
$$I_{\text{final}} = \mathcal{F}_{2d}^{-1} \left(\text{intensity} \cdot \mathcal{F}_{2d}(\text{PSF}) \cdot \text{pattern} + (1 - \text{intensity}) \cdot \mathcal{F}_{2d}(\text{PSF}) \right) \quad (4)$$

The best results where achieved using a grid of blurred circles as pattern, see [Figure 8](#). Note the distortions to the PSF are around the center of its peaks but not randomly spread. As Clearly this will not do.



(a) Difference between two PSFs created using this method, between PSFs the pattern has shifted 10 pixels.

(b) Difference between two PSFs created using this method, between PSFs the pattern has shifted 5 pixels.



(c) Pattern that is shifted and applied to the foerier space of a PSF.

Figure 8: The Pattern used and the differences between PSFs distorted with it using the method described above.

3.2.2 Using HCIPy

Then we tried a simulation of the psfs using high-contrast imaging python (HCIPy), an open-source object-oriented framework written in

Python for performing end-to-end simulations of high-contrast imaging instruments [11]. The framework is used to generate PSFs with a very rough simulation. We use the provided methods in HCIPy to create a multi-layer atmospheric model that changes in time. Then we use that model, the v APP amplitude and v APP phase screen to generate a series of PSFs using:

$$I_{vAPP} = \mathcal{F}_{2d}(Ae^{i\theta}) + \mathcal{F}_{2d}(Ae^{i\theta}) + \mathcal{F}_{2d}(Ae) \cdot C \quad (5)$$

Here we use not one apperture function ($Ae^{i\theta}$) as in Section 2.1 but combine three. The first two simulate the opposite phase the two circular polarisations receive from the v APP (see Section 2.2). The third factor, called the leakage term *****

Instead of modelling an active optics system we modified the fried parameter for the atmosphere to get similar morphological changes in time to the available on sky images. This is sufficient as the dark hole, where the we will observe the disk, will lie in the control radius of the AO which means the effect of an AO system on the disk will mostly be a increase in resolution by reducing the seeing effect.

We use a telescope diameter of 8.2m and a wavelength, of $1 \cdot 10^{-6}$ m for the generation. For a fried parameter of 4m we find quantitatively similar psf morphologies to the on sky data. To put this into perspective: to simulate excellent seeing conditions we would use 20cm. With these setting we use HCIPy to create an ordered set of PSFs changing through time as the simulated atmosphere evolves. See Figure 10 for the difference between the first PSF in a set and later PSFs in the same set, compared between on sky and generated PSFs. Note that as time evolves the differences between first and later PSFs grow. Qualitatively on sky and generated PSFs evolve similar in time. We decide to use this method to generate all PSFs.

3.3 GENERATING OBSERVATIONS

To get a dataset that simulates an observation we create an ordered set of disk images each one rotated a bit to eachother. This accounts for the field rotation between exposures caused by observing with an alt azimuth telescope. The angle depends on the time between exposures and the field rotation rate.

$$\psi = 0.2506 \cdot \frac{\cos(A) \cos \phi}{\sin(z)} \quad (6)$$

The field rotation ψ in degrees per minute for a given target azimuth A , zenith distance z and telescope latitude ϕ [8, page 95]. If we would be observing from mauna kea (latitude 19.8) at a resonable 30

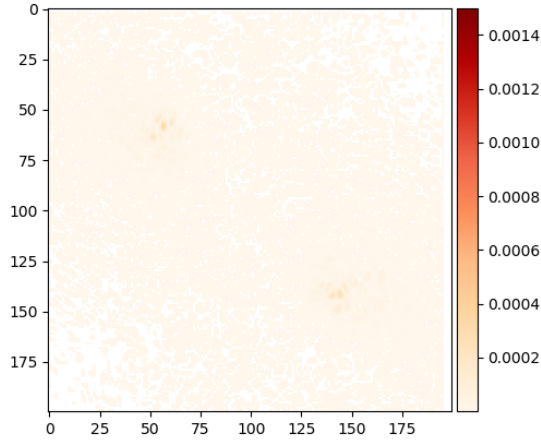
degrees from the zenith this gives a rotation rate between 0 and 14.74 degrees per minute.

Now to get the simulated observation an ordered set is created by convolving each n -th image from the disk set with the n -th image of the psf set. These are the simulated observations through time.

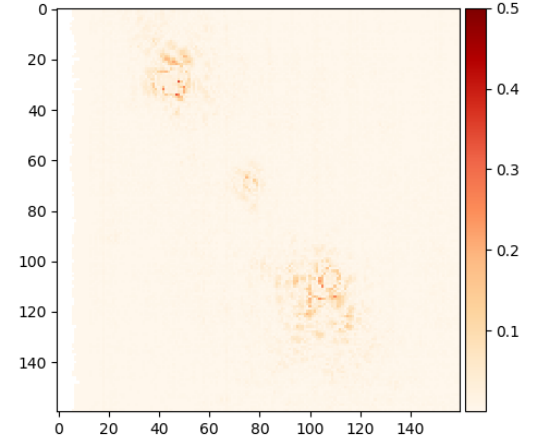
Using variations on this method we create 3 different sets.

1. Place the star as a single pixel with value one in the center of the disk before going through the above procedure. This is our observation set.
2. Leave out the disk, place only the single pixel in the center representing the star. This can be useful for checking if data reduction algorithms work properly.
3. Leave out the star, this way we see what the $vAPP$ does to the extended disk.

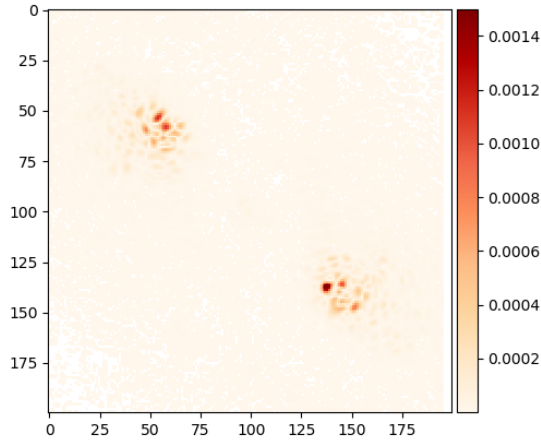
For each of the sets we can generate an additional variant to look at what the best result attainable is by leaving out the psf distortions. We do this by taking the convolution of the n -th disk image with the first PSF of the PSF set instead of the n -th.



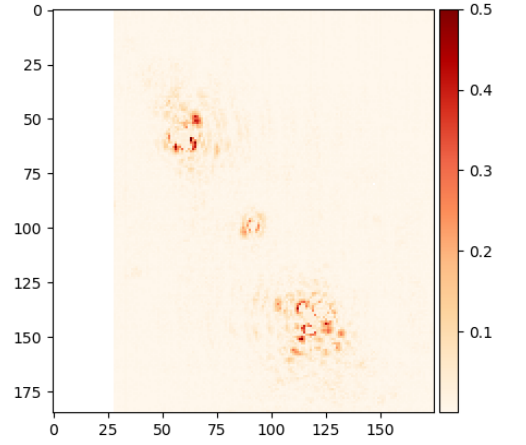
(a) Simulated psf: 1e - 2e, 0.7 seconds difference.



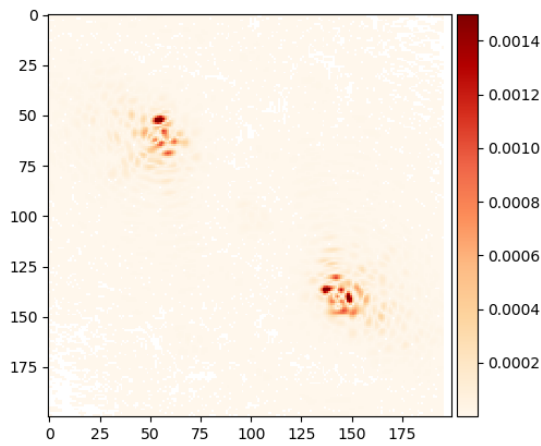
(b) On sky psf: 1th - 2th, *** seconds difference.



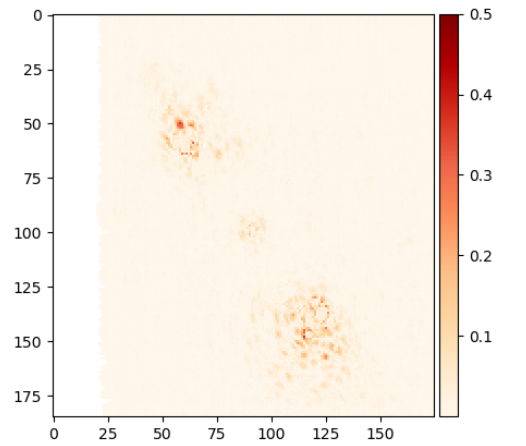
(c) Simulated psf: 1th - 10th, 7 seconds difference.



(d) On sky psf: 1th - 10th, *** seconds difference.



(e) Simulated psf: 1th - 50th, 14 seconds difference.



(f) On sky psf: 1th - 50th, *** seconds difference.

Figure 9: Differences between the first psf of an observation and later psfs. Compared between simulated observations on the left and on sky data on the right. The psfs were aligned then normalised on the maximum of the leakage term, finally the absolute value of the difference between the first and n-th psf was taken. The second, 10th and 50th simulated psf are 0.7, 7 and 14 seconds apart in the simulation.

DATA REDUCTION

The generated exposures contain 2 mirrored dark zones and are shifted relative to each other by the changing PSFs, see ???. Before applying any post processing technique we create 2 aligned stacks of processed exposures. Then we apply the ADI algorithm to remove most of the star light.

4.1 PRE-PROCESSING

Before we extract the `**psf kernels**` we align the exposures. We find the shift relative to the vAPP instrument PSF for every exposure in the set by cross correlating the upsampled image. Then the images are shifted using spline interpolation¹. For the implementation of both algorithms we use the SciPy library[5].

To find the center of the `**psf kernels**` an exposure is divided left right. Now for each half the brightest pixel gives the center, around it we copy out a square with sides of 30% of the image width. Done for all exposures this gives the 2 aligned stacks, a slice of which we see in [Figure 10b](#) and [Figure 10c](#).

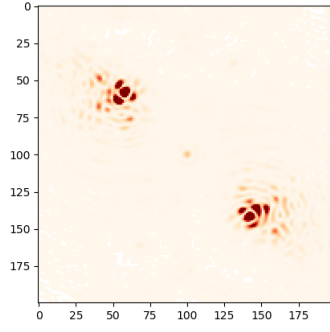
4.2 ANGULAR DIFFERENTIAL IMAGING

4.2.1 *Algorithm*

Now there are two separate stacks of exposures we apply the ADI algorithm [7] to each. First the median is taken over the stack using the implementation provided by the NumPy library [9]. This is our reference PSF. After subtracting the reference PSF from each exposure we rotated it back so the fields of all exposures are aligned again (see [Section 3.3](#)). Rotating a square inside a containing square here we lose information as the right angles rotate out of the containing square. The empty space that appears at the containing squares right angles is filled with value 0. The pixel values are determined by spline interpolating. For the rotation algorithm we use again the SciPy library [5].

Finally we take the median over the processed exposures to get a the end result.

¹ Here an image is interpolated by fitting multiple polynomials called splines



(a) Exposure after alignment.

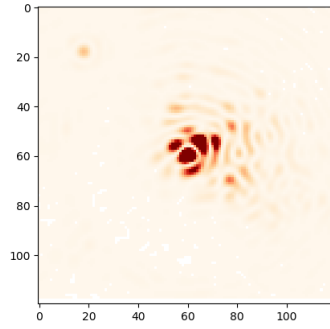
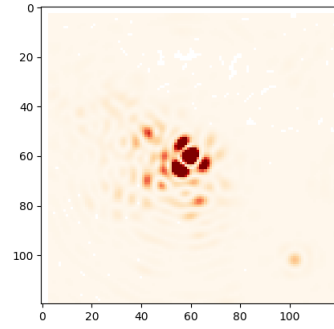
(b) Left **psf kernel**.(c) Right **psf kernel**.

Figure 10: A generated exposure through the Pre-processing process, first it is aligned and then its right and left **psf kernel** are extracted.

4.2.2 Control

Now we check if the algortime works applying it to an exposure set with only the star and no distortions applied. This results in a completely black image as expected. Next we apply ADI to an exposure set with only the star and distortions applied, this results in a circular noise pattern on the left and right as seen in [Figure 11](#)).

4.3 PAREMATER STUDY

When observing disks we are most interested in their morphology. It could however be heavily affected by the vAPP and ADI. As the vAPP by design redistributes light in an uneven way and ADI removes rotational symmetry while disks are by nature quite rotationally symmetrical. To see how the output morphology resembles the that of the input model we generate exposure stacks for a number of disks with different parameters. We vary the number of rings, the width of the rings and the inclination. We keep the contrast between the disk and star unrealistically low. For the best results of the parameter study the

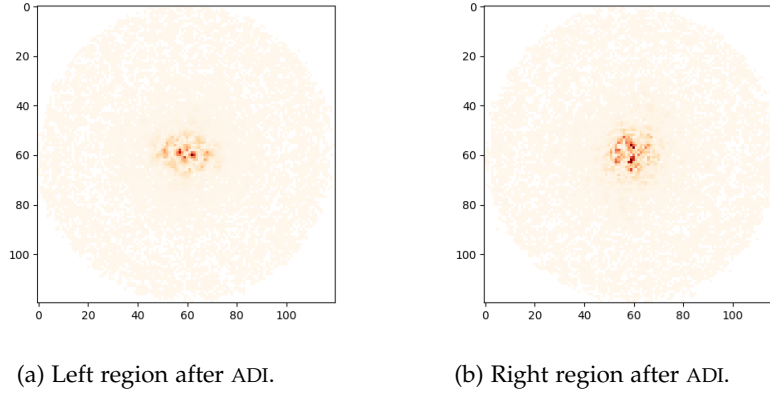


Figure 11: The right and left end result of ADI applied to a generated exposure stack of a star. The stack contains 20 exposures, the field rotation over the entire stack is 60° . Note how derotating the fields leads to a circular result as we lose the angles.

contrast is then returned to a realistic value. This allows us to easily compare results.

For each model the following images are generated:

- I An exposure of the model with a central star, using a distorted PSF.
- II The result of ADI for the model with a central star using distorted PSFs.
- III An exposure of the model without a central star, using the undistorted PSF.
- IV The result of ADI for the model without a central star using the undistorted PSF.

These images help see how the model behaves as we could observe it (I and II) and how only model is imaged when we remove anything that would distort or distract from it (III and IV). The latter is done by removing the star and using a fixed PSF. Using III and IV we can determine weather using the $vAPP$ and ADI could give usable results. We expect the morphology of the post processed disks to differ from the models input. However we expect the the new morphology to be unique for the input model or some of its paramaters.

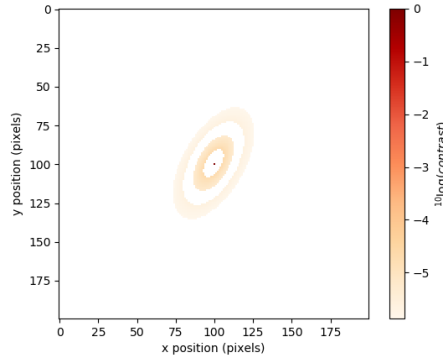
RESULTS

Here we present the results of the parameter study. We have varied the inclination, rotation and number of rings their sizes. All the combinations presented here are listed in [Table 1](#).

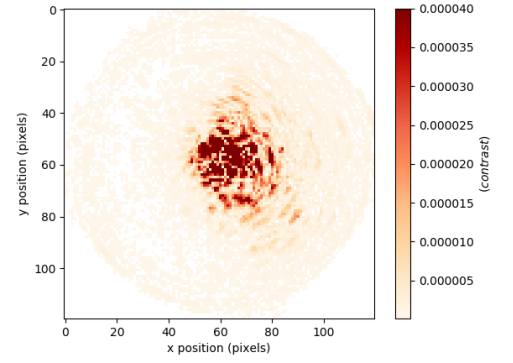
For each of these disks we show with increased disk brightness: the disk model with, the end result after ADI and three more images discussed in [Section 4.3](#). And we show the disk model at realistic brightness.

Disk	Figure Number	Rings		Inclination (degrees)	Initial Rotation (degrees)
		Number	Inner and Outer radius		
A	12	1	2 - 4 4 - 5	1	30
B	13	2	13.65	80	1

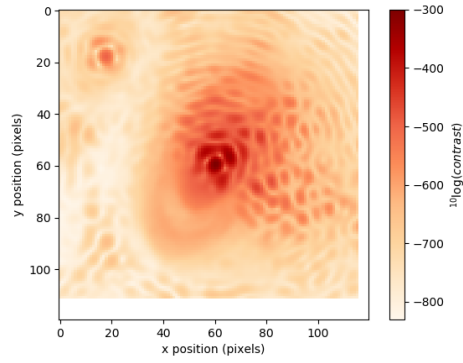
Table 1: An overview of all the disks we look at. If a disk has multiple rings their inner and outer dimensions are listed on different lines.



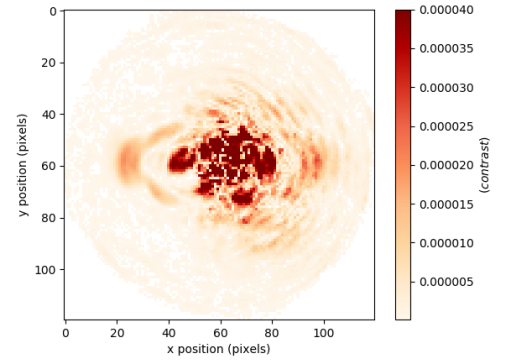
(a) The disk model used, brightness relative to the star



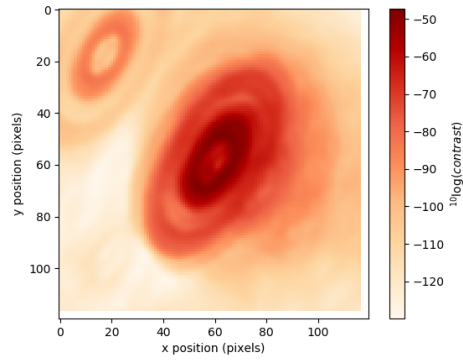
(b) ADI applied to the realistic disk model



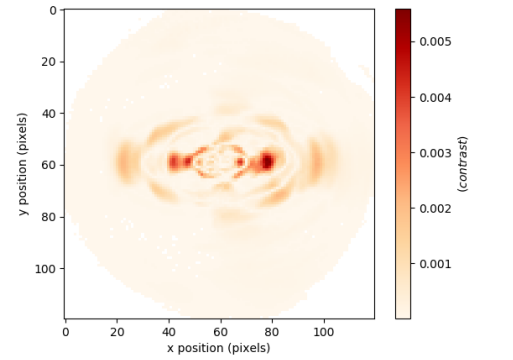
(c) As it would be observed with the vAPP



(d) ADI applied to the realistic disk model

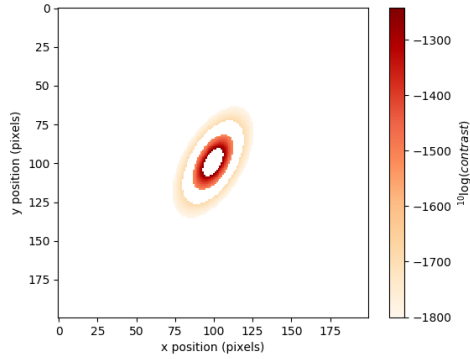


(e) Only the light of the disk

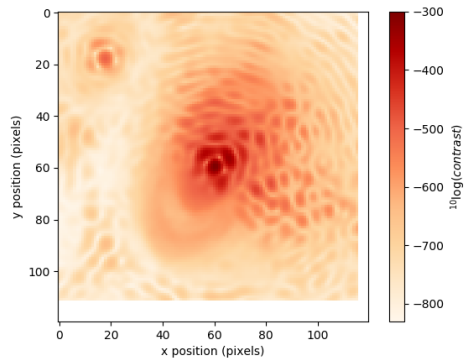


(f) ADI applied to only the light coming from the disk

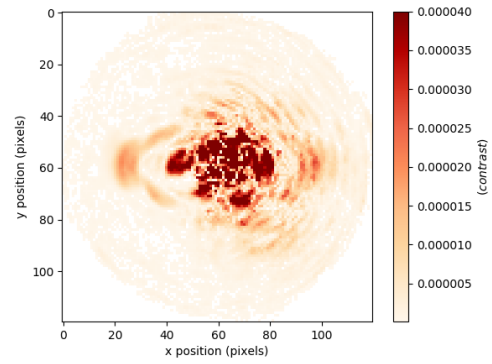
Figure 12: Results of applying ADI to disk model A



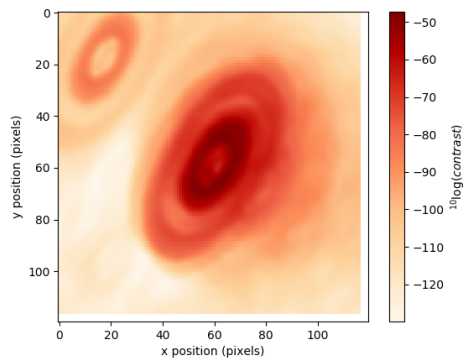
(a) the disk model used



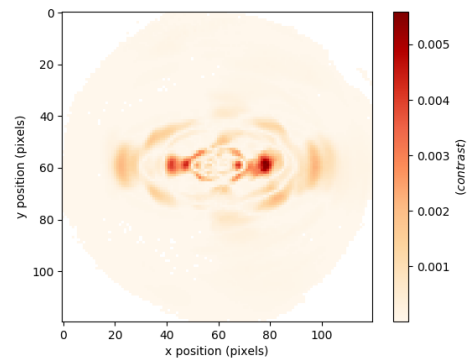
(b) As it would be observed with the vAPP



(c) ADI applied to the realistic disk model



(d) Only the light of the disk



(e) ADI applied to only the light coming from the disk

Figure 13: Results of applying ADI to disk model B

DISCUSSION

Instead of taking the mean of all other exposures as reference PSF another approach to use a few images close in time as possible as reference sequence [7]. As there is less time between the exposures the PSF has changed less due to seeing (see: [Section 2.1.2](#)) giving a greater correlation between the features on the reference image and the individual image. The disadvantage is that pixel to pixel noise is rejected less as we now only take an median over a slightly rotated sample. Care must be taken that the reference sequence has enough field rotation to displace features of interest by at least $1.5 \cdot \text{PSF full width half maximum (FWHM)}$. This ensures we don't subtract the feature from itself.

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