

4. Survey Data, Scale Reliability & Common Method Bias

- In surveys, we can ask people how they feel, or about their own perceptions about behavior
- This is mostly done through *survey items* that the respondent is asked to evaluate, such as “I am very satisfied with my job”
- In commonly used *Likert-scales*, respondents are asked for their level of agreement on a number of given statements on a scale such as
 1. Strongly disagree
 2. Disagree
 3. Neither agree nor disagree
 4. Agree
 5. Strongly agree
- While practitioners are often tempted to use single items for a certain attitude or behavior, researchers stress the importance to use *multiple items* to assess a phenomenon

4.1 Psychological Constructs and Reliability

- Researchers typically use scales with *multiple items* that are supposed to measure certain psychological constructs
- A *psychological construct* is a label for a cluster of covarying behaviors or attitudes (such as job satisfaction, job engagement, but also of personality traits such as conscientiousness, extraversion, etc.)
- Typically
 - item responses are averaged to compute a score
 - the score then represents a person's position on the construct
- Important question: How *reliable* is a scale?
- That is, how consistently does a scale measure the same underlying construct?

- A first step is often to assess the correlation between variables
- We can obtain a correlation matrix with `df.corr()`
 - Note: this can be a huge matrix as it shows the correlation coefficients between all variables in the DataFrame
 - Typically, it makes sense to only show it for a subset of the data
- To do so, we can filter the data frame (which gives us a smaller data frame selected by the filtering criteria)
 - Show correlation between two variables age and tenure:
`df.filter(items=['age', 'tenure']).corr()`
 - Show correlation matrix for all variables starting with “Satis”:
`df.filter(regex='Satis*').corr()`

- The LPP includes a scale to measure employee engagement, a short version of the Utrecht Work Engagement Scale (Schaufeli et al. (2006)):
 - *At my work, I feel bursting with energy*
 - *At my job, I feel strong and vigorous*
 - *I am enthusiastic about my job*
 - *My job inspires me*
 - *When I get up in the morning, I feel like going to work*
 - *I feel happy when I am working intensely*
 - *I am proud of the work that I do*
 - *I am immersed in my work*
 - *I get carried away when I'm working*
- The response scale ranges from 1 “every day” to 5 “never”
- The respective 9 item variables in the data set start with menga
- Print the correlation matrix for these variables
- Save the notebook

Assessing Reliability: Classical Test Theory in Psychology

- Suppose now we have $i = 1, \dots, k$ items X_i that measure a construct
- The observed score is $\bar{X} = \frac{1}{k} \sum_{i=1}^k X_i$
- Basic assumptions:
 - Response to a survey item = sum of “true score” T and some noise
$$X_i = T + \varepsilon_i$$
 - The noise terms ε_i are independent and identically distributed

- The so-called reliability of the scale is often defined as

$$\frac{V[T]}{V[\bar{X}]}$$

- That is: A scale is reliable when much of the variance in the observed score \bar{X} is due to variance in the true scores T
- When a scale is more reliable we have a smaller *measurement error* and a weaker *attenuation bias* when using the construct's score in a regression

The Length of a Scale

Note that we can write

$$\begin{aligned}\frac{V[T]}{V[\bar{X}]} &= \frac{V[T]}{V[\frac{1}{k} \sum_{i=1}^k (T + \varepsilon_i)]} \\ &= \frac{\sigma_T^2}{V[T + \frac{1}{k} \sum_{i=1}^k \varepsilon_i]} = \frac{\sigma_T^2}{V[T] + V[\frac{1}{k} \sum_{i=1}^k \varepsilon_i]} \\ &= \frac{\sigma_T^2}{\sigma_T^2 + \frac{1}{k^2} k \sigma_\varepsilon^2} = \frac{\sigma_T^2}{\sigma_T^2 + \frac{1}{k} \sigma_\varepsilon^2}\end{aligned}$$

Therefore:

- The reliability thus increases in the length of the scale k !
- Intuition: When responses to single items are noisy and this noise is independent, then the noise terms tend to “cancel each other out”
- The measurement error should be reduced when scales are longer

But how do we assess the reliability when we do not know T ?

The Reliability of Scales: Cronbach's Alpha

- Consider again the reliability coefficient $\frac{V[T]}{V[\bar{X}]}$
- For any two items, we have that

$$\text{Cov}[X_1, X_2] = \text{Cov}[T + \varepsilon_1, T + \varepsilon_2] = V[T]$$

- Now estimate $V[T]$ by the mean of all covariances between any two items:

$$\overline{\sigma_{ij}} = \frac{1}{k(k-1)} \sum_{i=1}^k \sum_{j \neq i}^k \text{Cov}[X_i, X_j]$$

- The ratio $\alpha = \frac{\overline{\sigma_{ij}}}{V[\bar{X}]}$ is called **Cronbach's alpha**

Note:

- α is a very frequently applied measure for the *internal consistency* of a scale
- Scale is considered to have a good internal consistency if $\alpha > 0.8$

- To obtain the score for the scale we typically compute the average across all items of the scale
- In Python we can do that for instance (say we have four items measuring satisfaction called `satis1`, ..., `satis4`)
 - by “manually” summing up the items and averaging:
`df['satis'] = (df.satis1+df.satis2+...) / 4`
 - or averaging across all columns of a filtered DataFrame:
`df['satis'] = df.filter(regex='satis*').mean(axis=1)`
 - **Note:** the method `mean` returns the mean of the values either over rows/observations (`axis=0`) or columns/variables (`axis=1`)
- Frequently, scores are *standardized* $X_{STD} = \frac{X - m_X}{\sigma_X}$ where m_X is the mean and σ_X the standard deviation of X
- We can do that for instance by
`df['sat_std'] = (df.satis-df.satis.mean())/df.satis.std()`

- We can use method `cronbach_alpha` from package `pingouin`
 - To so we must first install `pingouin` with `!pip install pingouin -q`
 - Then we can import `pingouin` as `pg`
 - You call the function with `pg.cronbach_alpha(data=df)`

- Or we can define our own function:

```
def cronbach(data):  
    k = data.shape[1]  
    varX = data.sum(axis=1).var()  
    sumVar = data.var(axis=0).sum()  
    return k / (k-1) * (1 - sumVar/varX)
```

- Note: the DataFrame you pass to either function must only consist of the variables of the specific scale, you can generate such a DataFrame with `df.filter(regex='menga*')`

Estimate the Reliability of a Scale

- Please open again the notebook `LPPanalysis.ipynb` used to look at the engagement data
- Generate a new variable `enga` for the mean engagement score
- Note: As the variable is coded, low values indicate high engagement. To avoid later confusion, it makes sense to reverse the scale (you can do that by simply stating `df['enga'] = 6 - df['enga']`)
- Also generate a standardized version of the variable (call it `enga_std`)
- What is the value of Cronbach's alpha? To what extent is the engagement scale internally consistent?

4.2 Common Method Bias

- The noise terms of different items in a survey will often likely be correlated due to factors beyond a common true score of a construct
- This can for instance be due to: respondents' different ...
 - ... tendencies to reply in a socially acceptable manner (social desirability)
 - ... tendencies or more or less consistently (consistency motif)
 - ... personality traits or cognitive abilities
 - ... levels of fatigue or mood when filling out the survey...
- We must thus be aware that the ε_i will be correlated beyond their connection through some underlying “true score” T

- Importantly:
This will also affect *separate* constructs elicited in the same survey
- Particularly problematic *when dependent and independent variable of a regression are collected in same survey*
 - Then you tend to overestimate the association between the constructs
 - This phenomenon is often called [common method bias](#)
- Hence: Be careful when you use different constructs from the same survey in a regression!
 - When regressing one psychological construct on another one measured in the same survey (for instance regress job satisfaction on engagement) you likely overestimate their true association
 - Less problematic for factual survey items where respondents' assessments are less subjective