

# Questions 24th March 2017

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March 24, 2017

## Elastic and Inelastic scattering

1) Show that

$$[\bar{u}(k')\gamma^\mu u(k)]^\dagger = \bar{u}(k)\gamma^\mu u(k') \quad (1)$$

3) In a fixed-targeted electron-proton elastic scattering:

$$Q^2 = 2m_p(E_1 - E_3) = 2m_p E_1 y \quad (2)$$

and

$$Q^2 = 4E_1 E_3 \sin^2\left(\frac{\theta}{2}\right) \quad (3)$$

a) Use these relations to show that

$$\sin^2\left(\frac{\theta}{2}\right) = \frac{E_1}{E_3} \frac{m_p^2}{Q^2} y^2 \quad (4)$$

and hence

$$\frac{E_3}{E_1} \cos^2\left(\frac{\theta}{2}\right) = 1 - y - \frac{m_p^2 y^2}{Q^2} \quad (5)$$

b) Assuming azimuthal symmetry and using the equations

$$E_3 = \frac{E_1 m_p}{m_p + E_1(1 - \cos\theta)} \quad (6)$$

and

$$Q^2 = \frac{2m_p E_1^2 (1 - \cos\theta)}{m_p + E_1(1 - \cos\theta)} \quad (7)$$

show that:

$$\frac{d\sigma}{dQ^2} = \left| \frac{d\Omega}{dQ^2} \right| \frac{d\sigma}{d\Omega} = \frac{\pi}{E_3^2} \frac{d\sigma}{d\Omega} \quad (8)$$

c) Using the results of a) and b), show that the Rosenbluth equation

$$\frac{d\sigma}{dQ^2} = \frac{\alpha^2}{4E_1^2 \sin^4(\frac{\theta}{2})} \frac{E_3}{E_1} \left( \frac{G_E^2 + \tau G_M^2}{(1 + \tau)} \cos^2 \frac{\theta}{2} + 2\tau G_M^2 \sin^2 \frac{\theta}{2} \right) \quad (9)$$

can be written in the Lorentz-invariant form:

$$\frac{d\sigma}{dQ^2} = \frac{4\pi\alpha^2}{Q^4} \left[ \frac{G_E^2 + \tau G_M^2}{(1 + \tau)} \left( 1 - y - \frac{m_p^2 y^2}{Q^2} \right) + \frac{1}{2} y^2 G_M^2 \right] \quad (10)$$