```
% This script estimates the optimal influences
% T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt for a set of given ranges for
% optimal influence model parameters defined for the worst case
within a
% 14 dimmensional grid space.
% IMPORTANT NOTE!!!
% This script file provides a slight modification of the original
script
% file "OliqopolisticOptimalInfluencesGridSearcher.m" which lies upon
the
% computation of the optimal prices (pA_opt, pB_opt), the optimal
% quantities (Q_A_opt, Q_B_opt) and the optimal profits (F_A_opt,
 F B opt)
% and their constituent quantities associated with the corresponding
% and cost (F_A_Rev_opt, F_A_Cost_opt, F_B_Rev_opt, F_B_Cost_opt).
This script
% computes the aforementioned quantities at a later stage outside the
% multiple nested loop.
% For some reason, conducting the computation of the aforementioned
% quantities within the multiple nested loop affects the validity of
the
% obtained results. This is an issue that demands for further
% investigation.
clc
clear all
% Define external optimization parameters that will remain constant
% throughout the whole experimentation within the context of the
% oligopolistic competition environment. That is, each firm holds the
% maximum possible initial belief for its own product and the minimum
% possible initial belief for the other firm's product.
P_A_A = 1;
P_A_B = 0;
P_B_A = 0;
P B B = 1;
% Define ranges and corresponding increment step for each parameter of
the
% optimal influence model.
% Parameter #1
Lambda A 1 MIN = 0.25;
Lambda_A_1_MAX = 0.25;
Lambda_A_1_STEP = 0.01;
% Parameter #2
Lambda A 2 MIN = 0.25;
Lambda_A_2_MAX = 0.25;
Lambda_A_2_STEP = 0.01;
```

```
% Parameter #3
Lambda B 1 MIN = 0.25;
Lambda_B_1_MAX = 0.25;
Lambda B 1 STEP = 0.01;
% Parameter #4
Lambda_B_2_MIN = 0.25;
Lambda_B_2_MAX = 0.25;
Lambda B 2 STEP = 0.01;
% Parameter #5
Theta1 MIN = 0.2;
Theta1_{MAX} = 0.2;
Theta1_STEP = 0.05;
% Parameter #6
Theta2_MIN = 0.2;
Theta2 MAX = 0.2;
Theta2_STEP = 0.01;
% Parameter #7
P_A_1_{MIN} = 0.2;
P A 1 MAX = 0.2;
P_A_1_STEP = 0.01;
% Parameter #8
P_A_2MIN = 0.2;
P_A_2_{MAX} = 0.2;
P A 2 STEP = 0.01;
% Parameter #9
P B 1 MIN = 0.2;
P_B_1_MAX = 0.2;
P_B_1_STEP = 0.01;
% Parameter #10
P B 2 MIN = 0.2;
P_B_2_MAX = 0.2;
P_B_2_{STEP} = 0.01;
% Parameter #11
M_MIN = 0.0;
M MAX = 1.0;
M\_STEP = 0.05;
% Parameter #12
K_MIN = 0.3;
K_MAX = 0.3;
K\_STEP = 0.06;
% Parameter #13
C_MIN = 0.0001;
C MAX = 0.0001;
C_{STEP} = 0.000001;
% Parameter #14
Gamma MIN = 0.5;
Gamma MAX = 0.5;
Gamma STEP = 0.01;
% Set the corresponding ranges for each one of the model parameters.
Lambda_A_1_RANGE = [Lambda_A_1_MIN:Lambda_A_1_STEP:Lambda_A_1_MAX];
Lambda A 2 RANGE = [Lambda A 2 MIN:Lambda A 2 STEP:Lambda A 2 MAX];
Lambda_B_1_RANGE = [Lambda_B_1_MIN:Lambda_B_1_STEP:Lambda_B_1_MAX];
Lambda_B_2_RANGE = [Lambda_B_2_MIN:Lambda_B_2_STEP:Lambda_B_2_MAX];
```

```
Theta1_RANGE = [Theta1_MIN:Theta1_STEP:Theta1_MAX];
Theta2 RANGE = [Theta2 MIN:Theta2 STEP:Theta2 MAX];
P_A_1_RANGE = [P_A_1_MIN:P_A_1_STEP:P_A_1_MAX];
P A 2 RANGE = [P A 2 MIN:P A 2 STEP:P A 2 MAX];
P_B_1_RANGE = [P_B_1_MIN:P_B_1_STEP:P_B_1_MAX];
P_B_2_RANGE = [P_B_2_MIN:P_B_2_STEP:P_B_2_MAX];
M_RANGE = [M_MIN:M_STEP:M_MAX];
K RANGE = [K MIN:K STEP:K MAX];
C_RANGE = [C_MIN:C_STEP:C_MAX];
Gamma_RANGE = [Gamma_MIN:Gamma_STEP:Gamma_MAX];
% Initialize matrices that store fundamental intermediate quantities
 of the
% underlying optimization problem within the oligopolistic enviroment
% well as the values of the external optimization parameters for each
% of the multi-dimensional grid searching process.
Topts = []; % Optimal investment levels.
Sopts = []; % Optimal limiting influences.
Xopts = []; % Optimal limiting beliefs.
Popts = []; % Optimal prices.
Qopts = []; % Optimal quantities.
Fopts = []; % Optimal profits.
Fvals = []; % Optimal values for the combined optimization objective.
OptFlags = []; % Optimization flags (i.e. number of different valid
 solutions).
DigitFlags = []; % Length of maximal sequence of identical digits
 within the obtained optimal solutions.
Params = []; % 14-plet of the varying optimization parameters.
% Perform the actual grid searching.
for Lambda_A_1 = Lambda_A_1_RANGE
    for Lambda_A_2 = Lambda_A_2_RANGE
        for Lambda B 1 = Lambda B 1 RANGE
            for Lambda_B_2 = Lambda_B_2_RANGE
                for Theta1 = Theta1 RANGE
                    %Theta1
                    for Theta2 = Theta2 RANGE
                        for P_A_1 = P_A_1_RANGE
                            for P A 2 = P A 2 RANGE
                                for P_B_1 = P_B_1_RANGE
                                    for P_B_2 = P_B_2_RANGE
                                         for M = M_RANGE
                                             for K = K_RANGE
                                                 for C = C RANGE
                                                     for Gamma =
 Gamma RANGE
                                                         K
                                                         params =
 [P_A_1,P_A_2,P_B_1,P_B_2,Lambda_A_1,Lambda_A_2,Lambda_B_1,Lambda_B_2,Theta1,Theta
                                                         Params =
 [Params; params];
```

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```
[T1 A opt,T2 A opt,T1 B opt,T2 B opt,Fval,OptFlag,DigitFlag] =
OligopolisticOptimalInfluences(Lambda_A_1,Lambda_A_2,Lambda_B_1,Lambda_B_2,Theta1
            [SA_opt,S1_opt,S2_opt,SB_opt] =
OligopolisticSOptimal(T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt,Lambda_A_1,Lambda_A_2,L
[XA opt, XB opt] =
OligopolisticXOptimal(P_A_A,P_A_1,P_A_2,P_A_B,P_B_A,P_B_1,P_B_2,P_B_B,SA_opt,S1_o
[pA_opt,pB_opt] = OligopolisticPOptimal(XA_opt,XB_opt,C,K,M);
[Q_A_opt,Q_B_opt] = OligopolisticQOptimal(XA_opt,XB_opt,C,K,M);
[F_A_opt,F_B_opt,F_A_Rev_opt,F_A_Cost_opt,F_B_Rev_opt,F_B_Cost_opt]
OligopolisticFOptimal(T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt,pA_opt,pB_opt,Q_A_opt,Q
[T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt];
                                                         S =
[SA_opt,S1_opt,S2_opt,SB_opt];
                                                        X =
[XA_opt,XB_opt];
                                                         P =
[pA_opt,pB_opt];
                                                        O =
[Q_A_opt,Q_B_opt];
[F_A_opt,F_B_opt,F_A_Rev_opt,F_A_Cost_opt,F_B_Rev_opt,F_B_Cost_opt];
                                                        Fvals =
[Fvals; Fval];
                                                        OptFlags =
[OptFlags;OptFlag];
                                                        DigitFlags =
[DigitFlags; DigitFlag];
                                                        Topts =
[Topts;T];
                                                        Sopts =
[Sopts;S];
                                                        Xopts =
[Xopts;X];
                                                        Popts =
[Popts;P];
                                                        Qopts =
[Qopts;Q];
                                                        Fopts =
[Fopts;F];
                                                    end;
                                                end;
                                            end;
                                        end;
                                    end;
                                end;
                            end;
```

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```
end;
                    end;
                end;
            end;
        end;
    end;
end;
% Get the previously computed optimal influence levels for the two
 firms
% for each consumer.
% % T1_A = Topts(:,1);
% % T2 A = Topts(:,2);
% % T1_B = Topts(:,1);
% % T2 B = Topts(:,2);
% Get the previously computed optimal beliefs (XA and XB) for the two
firms
% A and B.
% % XA = Xopts(:,1);
% % XB = Xopts(:,2);
% Get the optimal price levels (pA and pB) for the two firms A and B.
% % [pA,pB] = OligopolisticPOptimal(XA,XB,C,K,M);
% Get the optimal quantity levels (Q A and Q B) for the two firms A
and B.
% % [Q A,Q B] = OligopolisticQOptimal(XA,XB,C,K,M);
% Get the optimal profit levels (F_A and F_B) for the two firms A and
B as
% well as their associated costituent quantities
 (F A Rev opt, F A Cost opt,
% F_B_Rev_opt,F_B_Cost_opt).
% % [F_A,F_B,F_A_Rev,F_A_Cost,F_B_Rev,F_B_Cost] =
OligopolisticFOptimal(T1_A,T2_A,T1_B,T2_B,pA,pB,Q_A,Q_B,C,Gamma);
% Form matrices Popts, Qopts and Fopts.
% % Popts = [pA,pB];
% % Qopts = [Q A,Q B];
% % Fopts = [F_A,F_B,F_A_Rev,F_A_Cost,F_B_Rev,F_B_Cost];
% Set the varying parameter index.
ParamIndex = 11;
% Set parameters' indices and corresponding values for the parameters
that
% remain constant.
ConstIndices = setdiff(1:length(params),ParamIndex);
ConstValues = params(ConstIndices);
% Perform plotting operations.
plot_parameters_tuples(Topts,Sopts,Xopts,Popts,Qopts,Fopts,Params,ParamIndex,Const
K =
```

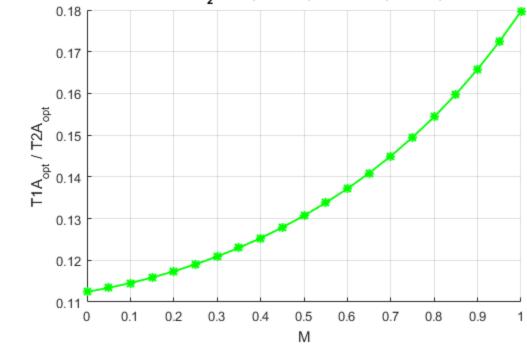
0.300000000000000

| K | =   |
|---|---|
| K | 0.300000000000000                           |
|   | 0.300000000000000                           |
| K | <pre>- 0.3000000000000000</pre>             |
| K |   |
|   | 0.300000000000000                           |
| K | <pre>- 0.3000000000000000</pre>             |
| K | =   |
|   | 0.300000000000000                           |
| K | - 0.300000000000000000000000000000000000    |
| K | =<br>0.300000000000000000000000000000000000 |
| K |   |
|   | 0.300000000000000                           |
| K | <pre>- 0.30000000000000000</pre>            |
| K | =   |
|   | 0.3000000000000000                          |

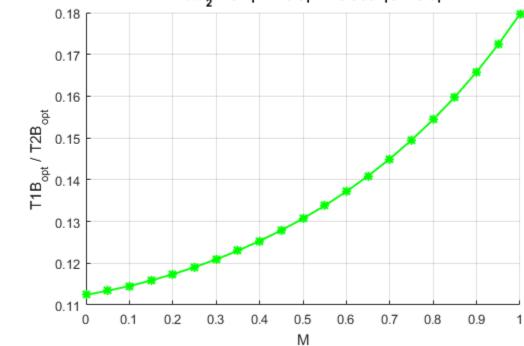
| K   | =   |
|-----|---|
|     | 0.3000000000000000                                  |
| K   | =<br>0.300000000000000000000000000000000000         |
| K   | =   |
|     | 0.3000000000000000                                  |
| K   | <pre>- 0.300000000000000000000000000000000000</pre> |
| K   | =<br>0.300000000000000000000000000000000000         |
| K   | =<br>0.300000000000000000000000000000000000         |
| K   |   |
| K   | 0.300000000000000                                   |
| IV. | 0.300000000000000                                   |
| K   | =   |

0.300000000000000

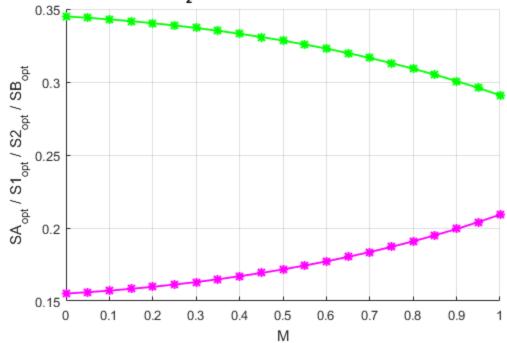
 $\begin{aligned} \mathsf{P}_{\mathsf{A},1} &= 0.2 | \mathsf{P}_{\mathsf{A},2} = 0.2 | \mathsf{P}_{\mathsf{B},1} = 0.2 | \mathsf{P}_{\mathsf{B},2} = 0.2 | \\ \mathsf{ambda}_{\mathsf{A},1} &= 0.25 | \mathsf{Lambda}_{\mathsf{A},2} = 0.25 | \mathsf{Lambda}_{\mathsf{B},1} = 0.25 | \mathsf{Lambda}_{\mathsf{B},2} = 0.25 | \mathsf{Theta}_1 = \\ \mathsf{Theta}_2 &= 0.2 | \mathsf{M} = 0.3 | \mathsf{K} = 0.0001 | \mathsf{C} = 0.5 | \end{aligned}$ 



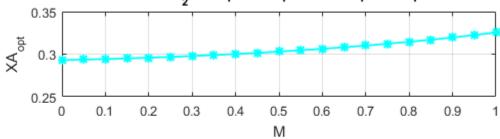
 $\begin{aligned} P_{A,1} &= 0.2 | P_{A,2} &= 0.2 | P_{B,1} &= 0.2 | P_{B,2} &= 0.2 | \\ ambda_{A,1} &= 0.25 | Lambda_{A,2} &= 0.25 | Lambda_{B,1} &= 0.25 | Lambda_{B,2} &= 0.25 | Theta_1 &= \\ &\qquad \qquad Theta_2 &= 0.2 | M &= 0.3 | K &= 0.0001 | C &= 0.5 | \end{aligned}$ 

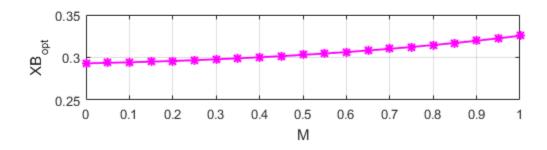


 $\begin{aligned} P_{A,1} &= 0.2 | P_{A,2} = 0.2 | P_{B,1} = 0.2 | P_{B,2} = 0.2 | \\ ambda_{A,1} &= 0.25 | Lambda_{A,2} = 0.25 | Lambda_{B,1} = 0.25 | Lambda_{B,2} = 0.25 | Theta_1 = \\ Theta_2 &= 0.2 | M = 0.3 | K = 0.0001 | C = 0.5 | \end{aligned}$ 

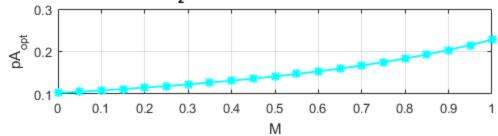


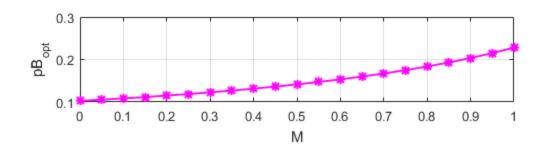
 $\begin{aligned} \mathsf{P}_{\mathsf{A},1} &= 0.2 | \mathsf{P}_{\mathsf{A},2} = 0.2 | \mathsf{P}_{\mathsf{B},1} = 0.2 | \mathsf{P}_{\mathsf{B},2} = 0.2 | \\ \mathsf{ambda}_{\mathsf{A},1} &= 0.25 | \mathsf{Lambda}_{\mathsf{A},2} = 0.25 | \mathsf{Lambda}_{\mathsf{B},1} = 0.25 | \mathsf{Lambda}_{\mathsf{B},2} = 0.25 | \mathsf{Theta}_1 = \\ \mathsf{Theta}_2 &= 0.2 | \mathsf{M} = 0.3 | \mathsf{K} = 0.0001 | \mathsf{C} = 0.5 | \end{aligned}$ 



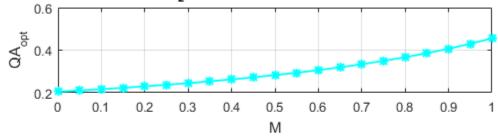


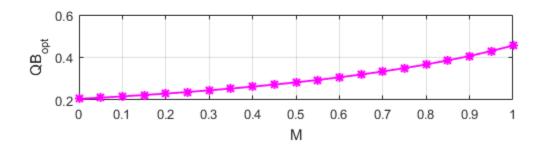
 $\begin{aligned} P_{A,1} &= 0.2 | P_{A,2} = 0.2 | P_{B,1} = 0.2 | P_{B,2} = 0.2 | \\ ambda_{A,1} &= 0.25 | Lambda_{A,2} = 0.25 | Lambda_{B,1} = 0.25 | Lambda_{B,2} = 0.25 | Theta_1 = \\ Theta_2 &= 0.2 | M = 0.3 | K = 0.0001 | C = 0.5 | \end{aligned}$ 



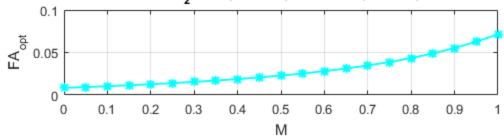


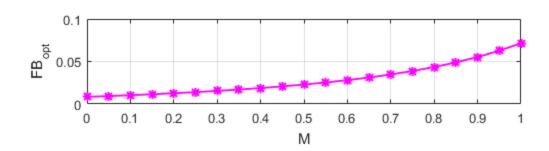
 $P_{A,1} = 0.2|P_{A,2} = 0.2|P_{B,1} = 0.2|P_{B,2} = 0.2|$   $ambda_{A,1} = 0.25|Lambda_{A,2} = 0.25|Lambda_{B,1} = 0.25|Lambda_{B,2} = 0.25|Theta_1 = Theta_2 = 0.2|M = 0.3|K = 0.0001|C = 0.5|$ 



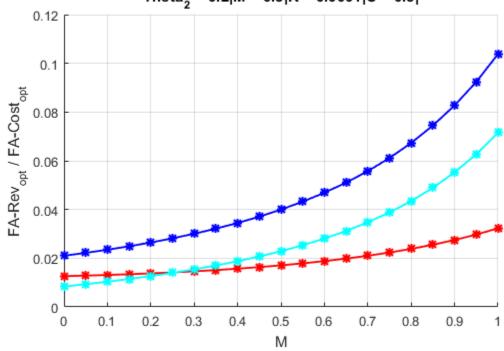


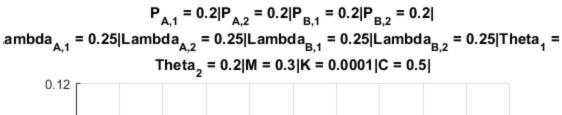
 $\begin{aligned} P_{A,1} &= 0.2 | P_{A,2} = 0.2 | P_{B,1} = 0.2 | P_{B,2} = 0.2 | \\ ambda_{A,1} &= 0.25 | Lambda_{A,2} = 0.25 | Lambda_{B,1} = 0.25 | Lambda_{B,2} = 0.25 | Theta_1 = \\ Theta_2 &= 0.2 | M = 0.3 | K = 0.0001 | C = 0.5 | \end{aligned}$ 

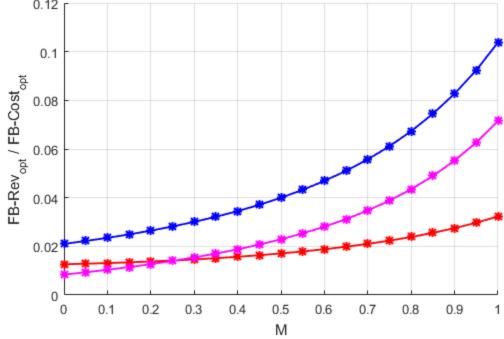




 $\begin{aligned} \mathsf{P}_{\mathsf{A},1} &= 0.2 | \mathsf{P}_{\mathsf{A},2} = 0.2 | \mathsf{P}_{\mathsf{B},1} = 0.2 | \mathsf{P}_{\mathsf{B},2} = 0.2 | \\ \mathsf{ambda}_{\mathsf{A},1} &= 0.25 | \mathsf{Lambda}_{\mathsf{A},2} = 0.25 | \mathsf{Lambda}_{\mathsf{B},1} = 0.25 | \mathsf{Lambda}_{\mathsf{B},2} = 0.25 | \mathsf{Theta}_1 = \\ \mathsf{Theta}_2 &= 0.2 | \mathsf{M} = 0.3 | \mathsf{K} = 0.0001 | \mathsf{C} = 0.5 | \end{aligned}$ 







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