```
% This script estimates the optimal influences
% T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt for a set of given ranges for
% optimal influence model parameters defined for the worst case
within a
% 14 dimmensional grid space.
% IMPORTANT NOTE!!!
% This script file provides a slight modification of the original
script
% file "OliqopolisticOptimalInfluencesGridSearcher.m" which lies upon
the
% computation of the optimal prices (pA_opt, pB_opt), the optimal
% quantities (Q_A_opt, Q_B_opt) and the optimal profits (F_A_opt,
 F B opt)
% and their constituent quantities associated with the corresponding
% and cost (F_A_Rev_opt, F_A_Cost_opt, F_B_Rev_opt, F_B_Cost_opt).
This script
% computes the aforementioned quantities at a later stage outside the
% multiple nested loop.
% For some reason, conducting the computation of the aforementioned
% quantities within the multiple nested loop affects the validity of
the
% obtained results. This is an issue that demands for further
% investigation.
clc
clear all
% Define external optimization parameters that will remain constant
% throughout the whole experimentation within the context of the
% oligopolistic competition environment. That is, each firm holds the
% maximum possible initial belief for its own product and the minimum
% possible initial belief for the other firm's product.
P_A_A = 1;
P_A_B = 0;
P_B_A = 0;
P B B = 1;
% Define ranges and corresponding increment step for each parameter of
the
% optimal influence model.
% Parameter #1
Lambda A 1 MIN = 0.25;
Lambda_A_1_MAX = 0.25;
Lambda_A_1_STEP = 0.01;
% Parameter #2
Lambda A 2 MIN = 0.25;
Lambda_A_2_MAX = 0.25;
Lambda_A_2_STEP = 0.01;
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```
% Parameter #3
Lambda B 1 MIN = 0.25;
Lambda_B_1_MAX = 0.25;
Lambda B 1 STEP = 0.01;
% Parameter #4
Lambda_B_2_MIN = 0.25;
Lambda_B_2_MAX = 0.25;
Lambda B 2 STEP = 0.01;
% Parameter #5
Theta1 MIN = 0.2;
Theta1_{MAX} = 0.2;
Theta1_STEP = 0.05;
% Parameter #6
Theta2_MIN = 0.2;
Theta2 MAX = 0.2;
Theta2_STEP = 0.01;
% Parameter #7
P_A_1_{MIN} = 0.0;
P A 1 MAX = 1.0;
P_A_1_STEP = 0.05;
% Parameter #8
P_A_2MIN = 0.7;
P_A_2_{MAX} = 0.7;
P A 2 STEP = 0.01;
% Parameter #9
P B 1 MIN = 0.7;
P_B_1_MAX = 0.7;
P_B_1_STEP = 0.01;
% Parameter #10
P B 2 MIN = 0.7;
P_B_2_MAX = 0.7;
P_B_2_{STEP} = 0.01;
% Parameter #11
M_MIN = 0.3;
M MAX = 0.3;
M\_STEP = 0.05;
% Parameter #12
K_MIN = 0.3;
K_MAX = 0.3;
K\_STEP = 0.05;
% Parameter #13
C_MIN = 0.0001;
C MAX = 0.0001;
C_{STEP} = 0.000001;
% Parameter #14
Gamma MIN = 0.5;
Gamma MAX = 0.5;
Gamma STEP = 0.01;
% Set the corresponding ranges for each one of the model parameters.
Lambda_A_1_RANGE = [Lambda_A_1_MIN:Lambda_A_1_STEP:Lambda_A_1_MAX];
Lambda A 2 RANGE = [Lambda A 2 MIN:Lambda A 2 STEP:Lambda A 2 MAX];
Lambda_B_1_RANGE = [Lambda_B_1_MIN:Lambda_B_1_STEP:Lambda_B_1_MAX];
Lambda_B_2_RANGE = [Lambda_B_2_MIN:Lambda_B_2_STEP:Lambda_B_2_MAX];
```

```
Thetal_RANGE = [Thetal_MIN:Thetal_STEP:Thetal_MAX];
Theta2 RANGE = [Theta2 MIN:Theta2 STEP:Theta2 MAX];
P_A_1_RANGE = [P_A_1_MIN:P_A_1_STEP:P_A_1_MAX];
P A 2 RANGE = [P A 2 MIN:P A 2 STEP:P A 2 MAX];
P_B_1_RANGE = [P_B_1_MIN:P_B_1_STEP:P_B_1_MAX];
P_B_2_RANGE = [P_B_2_MIN:P_B_2_STEP:P_B_2_MAX];
M_RANGE = [M_MIN:M_STEP:M_MAX];
K RANGE = [K MIN:K STEP:K MAX];
C_RANGE = [C_MIN:C_STEP:C_MAX];
Gamma RANGE = [Gamma MIN:Gamma STEP:Gamma MAX];
% Initialize matrices that store fundamental intermediate quantities
 of the
% underlying optimization problem within the oligopolistic enviroment
% well as the values of the external optimization parameters for each
% of the multi-dimensional grid searching process.
Topts = []; % Optimal investment levels.
Sopts = []; % Optimal limiting influences.
Xopts = []; % Optimal limiting beliefs.
Popts = []; % Optimal prices.
Qopts = []; % Optimal quantities.
Fopts = []; % Optimal profits.
Fvals = []; % Optimal values for the combined optimization objective.
OptFlags = []; % Optimization flags (i.e. number of different valid
 solutions).
DigitFlags = []; % Length of maximal sequence of identical digits
 within the obtained optimal solutions.
Params = []; % 14-plet of the varying optimization parameters.
% Perform the actual grid searching.
for Lambda_A_1 = Lambda_A_1_RANGE
    for Lambda_A_2 = Lambda_A_2_RANGE
        for Lambda B 1 = Lambda B 1 RANGE
            for Lambda_B_2 = Lambda_B_2_RANGE
                for Theta1 = Theta1 RANGE
                    %Theta1
                    for Theta2 = Theta2 RANGE
                        for P_A_1 = P_A_1_RANGE
                            P_A_2 = P_A_1;
                            for P_A_2 = P_A_2_RANGE
                                P_B_1 = P_A_1;
                                for P_B_1 = P_B_1_RANGE
                                    P_B_2 = P_A_1;
                                    for P B 2 = P B 2 RANGE
                                        for M = M_RANGE
                                            for K = K RANGE
                                                 for C = C_RANGE
                                                     for Gamma =
 Gamma_RANGE
                                                         P A 1
                                                         params =
 [P_A_1,P_A_2,P_B_1,P_B_2,Lambda_A_1,Lambda_A_2,Lambda_B_1,Lambda_B_2,Theta1,Theta
```

```
Params =
[Params; params];
[T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt,Fval,OptFlag,DigitFlag] =
OligopolisticOptimalInfluences(Lambda_A_1,Lambda_A_2,Lambda_B_1,Lambda_B_2,Theta1
           [SA_opt,S1_opt,S2_opt,SB_opt] =
OligopolisticSOptimal(T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt,Lambda_A_1,Lambda_A_2,L
[XA_opt,XB_opt] =
[pA_opt,pB_opt] = OligopolisticPOptimal(XA_opt,XB_opt,C,K,M);
[Q_A_opt,Q_B_opt] = OligopolisticQOptimal(XA_opt,XB_opt,C,K,M);
[F_A_opt,F_B_opt,F_A_Rev_opt,F_A_Cost_opt,F_B_Rev_opt,F_B_Cost_opt]
OligopolisticFOptimal(T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt,pA_opt,pB_opt,Q_A_opt,Q
[T1_A_opt,T2_A_opt,T1_B_opt,T2_B_opt];
                                                    S =
[SA_opt,S1_opt,S2_opt,SB_opt];
                                                    X =
[XA_opt,XB_opt];
                                                    P =
[pA_opt,pB_opt];
                                                    O =
[Q_A_opt,Q_B_opt];
[F_A_opt,F_B_opt,F_A_Rev_opt,F_A_Cost_opt,F_B_Rev_opt,F_B_Cost_opt];
                                                    Fvals =
[Fvals; Fval];
                                                    OptFlags =
[OptFlags;OptFlag];
                                                    DigitFlags =
[DigitFlags;DigitFlag];
                                                    Topts =
[Topts;T];
                                                    Sopts =
[Sopts;S];
                                                    Xopts =
[Xopts;X];
                                                    Popts =
[Popts;P];
                                                    Qopts =
[Qopts;Q];
                                                    Fopts =
[Fopts;F];
                                                end;
                                            end;
                                         end;
                                     end;
```

end;

```
%end;
                           end;
                       end;
                   end;
               end;
           end;
        end;
    end;
end;
% Get the previously computed optimal influence levels for the two
firms
% for each consumer.
% % T1_A = Topts(:,1);
% % T2 A = Topts(:,2);
% % T1_B = Topts(:,1);
% % T2_B = Topts(:,2);
% Get the previously computed optimal beliefs (XA and XB) for the two
firms
% A and B.
% % XA = Xopts(:,1);
% % XB = Xopts(:,2);
% Get the optimal price levels (pA and pB) for the two firms A and B.
% % [pA,pB] = OligopolisticPOptimal(XA,XB,C,K,M);
% Get the optimal quantity levels (Q_A and Q_B) for the two firms A
and B.
% % [Q_A,Q_B] = OligopolisticQOptimal(XA,XB,C,K,M);
% Get the optimal profit levels (F_A and F_B) for the two firms A and
B as
% well as their associated costituent quantities
 (F_A_Rev_opt,F_A_Cost_opt,
% F_B_Rev_opt,F_B_Cost_opt).
% % [F_A,F_B,F_A_Rev,F_A_Cost,F_B_Rev,F_B_Cost] =
OligopolisticFOptimal(T1 A,T2 A,T1 B,T2 B,pA,pB,Q A,Q B,C,Gamma);
% Form matrices Popts, Qopts and Fopts.
% % Popts = [pA,pB];
% % Qopts = [Q_A,Q_B];
% Set the varying parameter index.
ParamIndex = 1;
% Set parameters' indices and corresponding values for the parameters
that
% remain constant.
ConstIndices = setdiff(1:length(params),ParamIndex);
ConstValues = params(ConstIndices);
% Perform plotting operations.
plot_parameters_tuples(Topts,Sopts,Xopts,Popts,Qopts,Fopts,Params,ParamIndex,Const
```

 $P_A_1 =$

0

 $P_A_1 =$

0.0500000000000000

P_A_1 =

0.1000000000000000

P_A_1 =

0.1500000000000000

P_A_1 =

0.2000000000000000

P_A_1 =

0.2500000000000000

P_A_1 =

0.3000000000000000

P_A_1 =

0.3500000000000000

P_A_1 =

0.4000000000000000

P_A_1 =

0.450000000000000

P_A_1 =

0.5000000000000000

P_A_1 =

0.5500000000000000

P_A_1 =

0.6000000000000000

P_A_1 =

0.6500000000000000

 $P_A_1 =$

0.7000000000000000

P_A_1 =

0.7500000000000000

P_A_1 =

0.8000000000000000

P_A_1 =

0.8500000000000000

P_A_1 =

0.9000000000000000

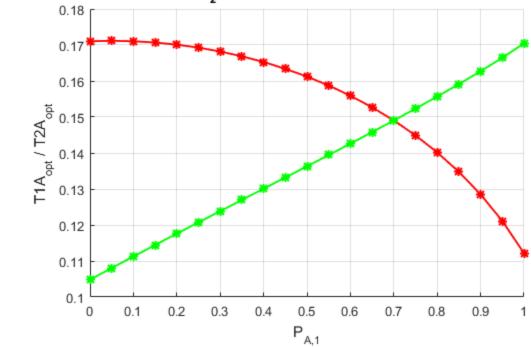
P_A_1 =

0.9500000000000000

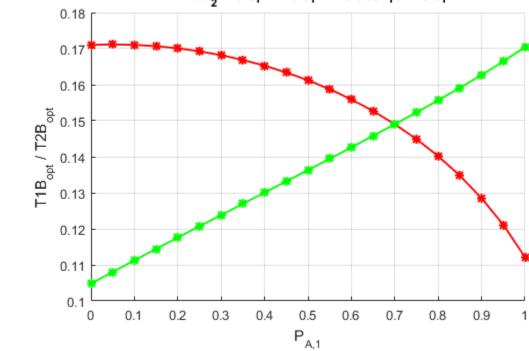
P_A_1 =

1

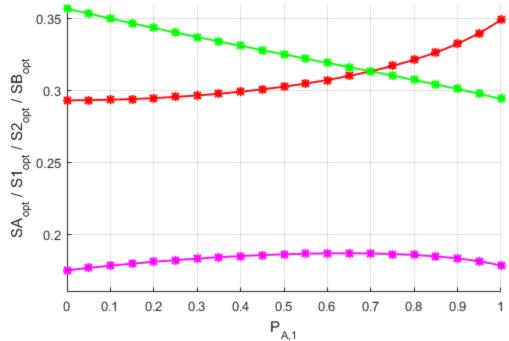
 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ \text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.25 | \text{Lambda}_{3} &= 0.25 |$



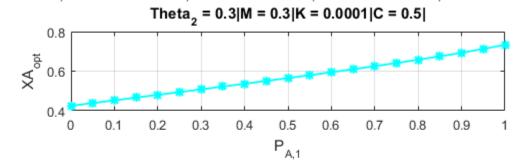
 $\begin{aligned} \mathbf{P_{A,1}} &= 0.7|\mathbf{P_{A,2}} = 1|\mathbf{P_{B,1}} = 0.7|\mathbf{P_{B,2}} = 0.25|\\ &-\text{ambda}_{A,1} = 0.25|\text{Lambda}_{A,2} = 0.25|\text{Lambda}_{B,1} = 0.25|\text{Lambda}_{B,2} = 0.2|\text{Theta}_{1} = 0.25|\\ &-\text{Theta}_{2} = 0.3|\mathbf{M} = 0.3|\mathbf{K} = 0.0001|\mathbf{C} = 0.5| \end{aligned}$

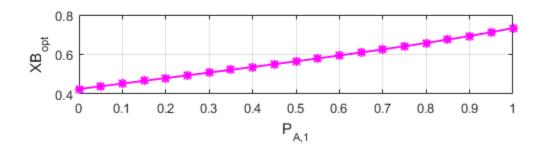


 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ \text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.2 | \text{Theta}_{2} &= 0.2 | \text{Theta}_{3} &= 0.25 | \text{Lambda}_{3} &= 0.25 | \text{Lambda}_{4} &= 0.25 | \text{Lambda}_{3} &= 0.25 | \text{Lambda}_{4} &= 0.25 | \text{L$

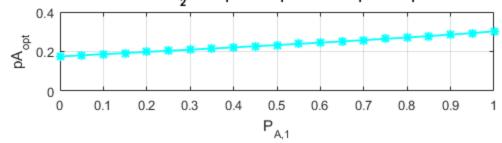


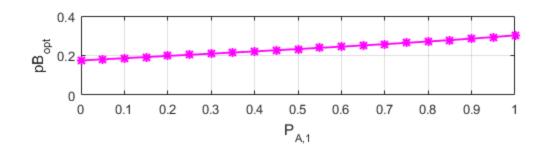
 $P_{A,1} = 0.7|P_{A,2} = 1|P_{B,1} = 0.7|P_{B,2} = 0.25|$ $-ambda_{A,1} = 0.25|Lambda_{A,2} = 0.25|Lambda_{B,1} = 0.25|Lambda_{B,2} = 0.2|Theta_1 = 0.25|Lambda_{B,2} = 0.25|Lambda_{B,2} = 0.2|Theta_1 = 0.25|Lambda_{B,2} = 0.2$



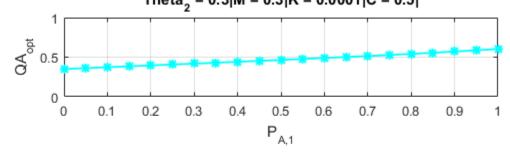


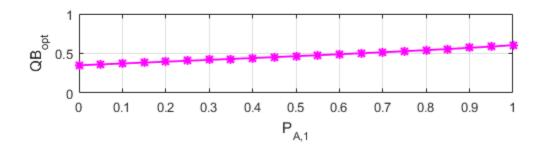
 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ &\text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.2 | \text{Theta}_{2} &= 0.2 | \text{Theta}_{3} &= 0.2 | \text{Theta}_{4} &= 0.2 | \text{Theta}_{3} &= 0.2 | \text{Theta}_{4} &= 0$



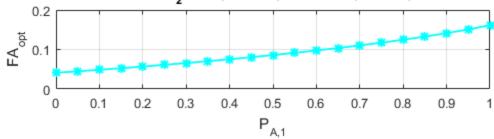


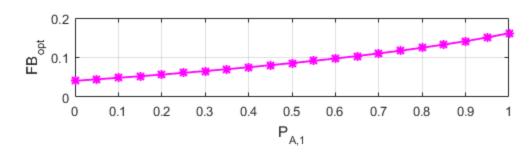
 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ \text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.2 | \text{Theta}_{2} &= 0.2 | \text{Theta}_{3} &= 0.2 | \text{Theta}_{4} &= 0.2 | \text{Theta}_{3} &= 0.2 | \text{Theta}_{4} &= 0.2 | \text{Thea}_{4} &= 0.2 | \text{Theta}_{4} &= 0.2 | \text{Theta}_{4} &= 0.2 | \text{Thea}_{4} &= 0.2 | \text{Thea}_{$



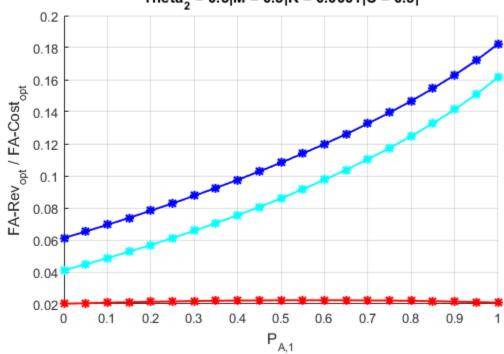


 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ \text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.25 | \text{Lambda}_{3} &= 0.25 |$

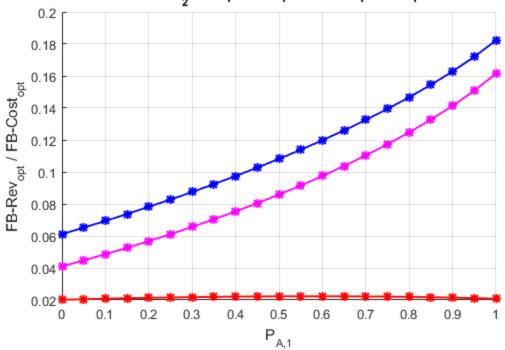




 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ &\text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.2 | \text{Theta}_{2} &= 0.2 | \text{Theta}_{3} &= 0.2 | \text{Theta}_{4} &= 0.2 | \text{Theta}_{3} &= 0.2 | \text{Theta}_{4} &= 0$



 $\begin{aligned} P_{A,1} &= 0.7 | P_{A,2} &= 1 | P_{B,1} &= 0.7 | P_{B,2} &= 0.25 | \\ \text{-ambda}_{A,1} &= 0.25 | \text{Lambda}_{A,2} &= 0.25 | \text{Lambda}_{B,1} &= 0.25 | \text{Lambda}_{B,2} &= 0.2 | \text{Theta}_{1} &= 0.25 | \text{Lambda}_{1} &= 0.25 | \text{Lambda}_{2} &= 0.2 | \text{Theta}_{2} &= 0.2 | \text{Theta}_{3} &= 0.25 | \text{Lambda}_{4} &= 0.25 | \text{L$



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