

## Performance measurement of Models

- 1) **Accuracy Score:** It's a measure or a matrix to check the accuracy of the classification model

$$\text{Accuracy Score} = \frac{\text{Total no of correctly classified points}}{\text{Total number of points}}$$

### Problem with Accuracy Score

- i) Imbalance Dataset
  - a. Where we have one class in majority (If the transaction is fraudulent or not, there will be roughly 5-10% transactions as fraudulent but rest will be non-fraudulent)
  - b. We are giving more non-fraudulent transactions to machine for learning, the chances will be high your machine will predict a fraudulent transaction as a non-fraudulent.
  - c. 90% - non-Fraudulent / 10% - Fraudulent – 100% Non-Fraudulent
  - d. There will be a high chance that the model will be a dumb model and the accuracy will come as 90% which is wrong.
- ii) Model Comparison: In the model comparison accuracy score will not help us to understand which model is the best as it does not consider probability.

X	Y	M1	M2	$\hat{Y}_1$	$\hat{Y}_2$
1	1	0.9	0.6	1	1
2	1	0.8	0.55	1	1
3	0	0.1	0.45	0	0
4	0	0.15	0.48	0	0

### 2) Confusion Matrix

	0 (Prediction)	1 (Prediction)	
0 (Actual)	A (TN)	B (FP)	TN+FP = N
1 (Actual)	C (FN)	D (TP)	FN+TP = P

A+B+C+D = Total number of records

A+B = Total no of negative records in the actual data

C+D = Total no of positive records in the actual data

A+C = Total no of negative records in the prediction

B+D = Total no of positive records in the prediction

$A+D/A+B+C+D$  = Accuracy score

A = TN = True Negatives

D = TP = True Positives

C = FN = False Negatives

B = FP = False Positives

TN + TP = Total number of correct classification

FN + FP = Total number of wrong classification

FN + TP = Total number of Positives in the dataset

FP + TN = Total number of negatives in the dataset

- **TPR (True positive rate) =  $TP/P$  ( $TP/TP+FN$ )**  
Total number of correctly classified Positive points upon total number of positive points in the dataset
- **TNR (True negative rate) =  $TN/N$  ( $TN/TN+FP$ )**  
Total number of correctly classified negative points upon total number of negative points in the dataset
- **FPR (False positive rate) =  $FP/N$  ( $FP/TN+FP$ )**  
Total number of incorrectly classified as Positive points upon total number of negative points in the dataset
- **FNR (False negative rate) =  $FN/P$  ( $FN/TP+FN$ )**  
Total number of incorrectly classified as negative points upon total number of positive points in the dataset

When TPR and TNR is high my model is good it's a sensible model

When FNR and FPR is high my model is not good

Problem with these 4 ratios

	(NF) 0 (Prediction)	(F) 1 (Prediction)
(NF) 0 (Actual)	900	0
(F) 1 (Actual)	100	0

TPR = 0

TNR = 1

FPR = 0

FNR = 1

## Dumb model

Cancer patients:

Patient is having a cancer as per the model but actually he is not having the cancer – Better

The further tests will happen

Patient is not having the cancer as per the model but actually he is having the cancer – Not good

	(NC) 0 (Prediction)	(C) 1 (Prediction)
(NC) 0 (Actual)	A	B (High – OK)
(C) 1 (Actual)	C (Low - Good)	D (High – Good)

B = Patient is having a cancer as per the model but actually he is not having the cancer – Better

C = Patient is not having the cancer as per the model but actually he is having the cancer – Problem

We are looking for High TPR and very low FNR

If FPR is high its ok as we can go with more powerful tests

### 3) Precision and Recall

	0 (Prediction)	1 (Prediction)	
0 (Actual)	A (TN)	B (FP)	TN+FP = N
1 (Actual)	C (FN)	D (TP)	FN+TP = P

Precision:  $TP/TP+FP$

Out of total number of points predicted as positive what %age of points is actually positive

Recall: True positive rate (TPR) =  $TP/TP+FN$

Total number of correctly classified Positive points upon total number of positive points in the dataset

$$\text{F1-Score} = \left( 2 * \frac{\text{PRECISION} * \text{RECALL}}{\text{PRECISION} + \text{RECALL}} \right)$$

The value of F1 score – 0 to 1 (More towards 1 better the model is , more towards 0 worst the model is)

Cancer patients:

We want high recall if we are looking for the cancerous patients prediction

We are allowed to have a low precision as we can go with further tests

	(NC) 0 (Prediction)	(C) 1 (Prediction)
(NC) 0 (Actual)	A	B (High – OK)
(C) 1 (Actual)	C (Low - Good)	D (High – Good)

#### 4) ROC (Receiver operating characteristics curve) / AUC (Area under the curve)

Electronics and Radio engineers – 2<sup>nd</sup> world war – They wanted to predict how well your missile working

X	Y	$\hat{Y}_p$
1	1	0.95
2	1	0.92
3	0	0.80
4	1	0.76
5	1	0.71

Step1: Take the data and sort  $\hat{Y}_p$  Predicted in descending order

Step2: Take the first predicted value as a threshold = 0.95

X	Y	$\hat{Y}_p$	$\hat{Y}_{T1}$	TPR @ T1	FPR @ T1
1	1	0.95	1		
2	1	0.92	0		
3	0	0.80	0		
4	1	0.76	0		
5	1	0.71	0		

X	Y	$\hat{Y}_p$	$\hat{Y}_{T2}$	TPR @ T2	FPR @ T2
1	1	0.95	1		
2	1	0.92	1		

3	0	0.80	0		
4	1	0.76	0		
5	1	0.71	0		

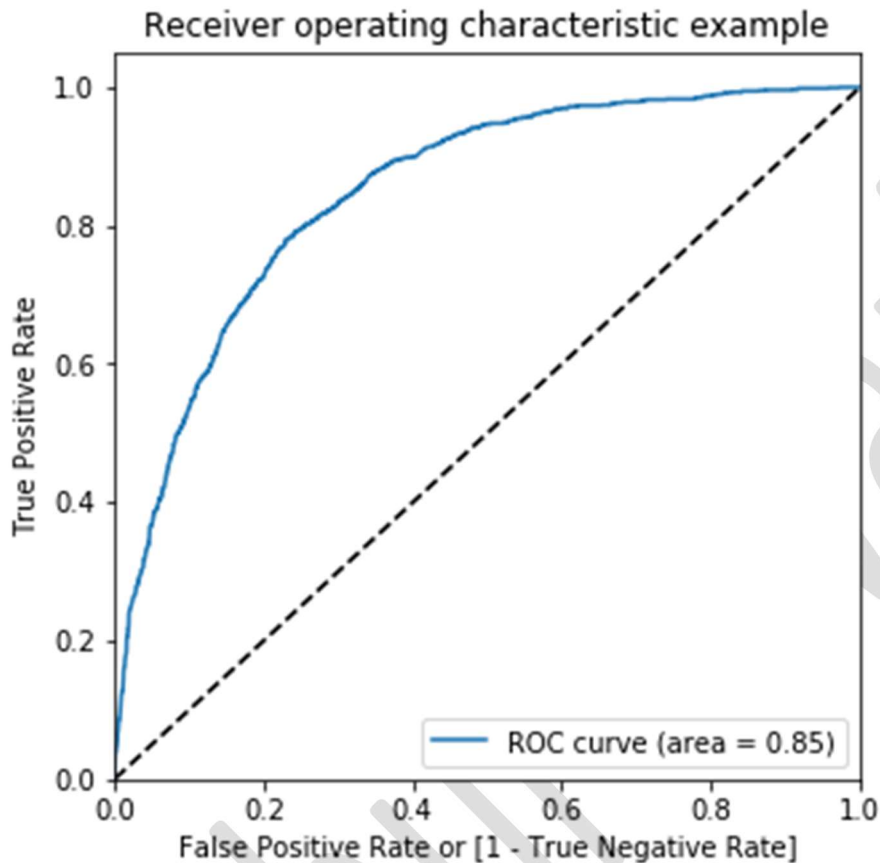
X	Y	$\hat{Y}_p$	$\hat{Y}_{T3}$	TPR @ T3	FPR @ T3
1	1	0.95	1		
2	1	0.92	1		
3	0	0.80	1		
4	1	0.76	0		
5	1	0.71	0		

X	Y	$\hat{Y}_p$	$\hat{Y}_{T4}$	TPR @ T4	FPR @ T4
1	1	0.95	1		
2	1	0.92	1		
3	0	0.80	1		
4	1	0.76	1		
5	1	0.71	0		

X	Y	$\hat{Y}_p$	$\hat{Y}_{T5}$	TPR @ T5	FPR @ T5
1	1	0.95	1		
2	1	0.92	1		
3	0	0.80	1		
4	1	0.76	1		
5	1	0.71	1		

TPR (Y)	FPR (X)
TPR@T1	FPR@T1
TPR@T2	FPR@T2
TPR@T3	FPR@T3
TPR@T4	FPR@T4
TPR@T5	FPR@T5

Plot the chart



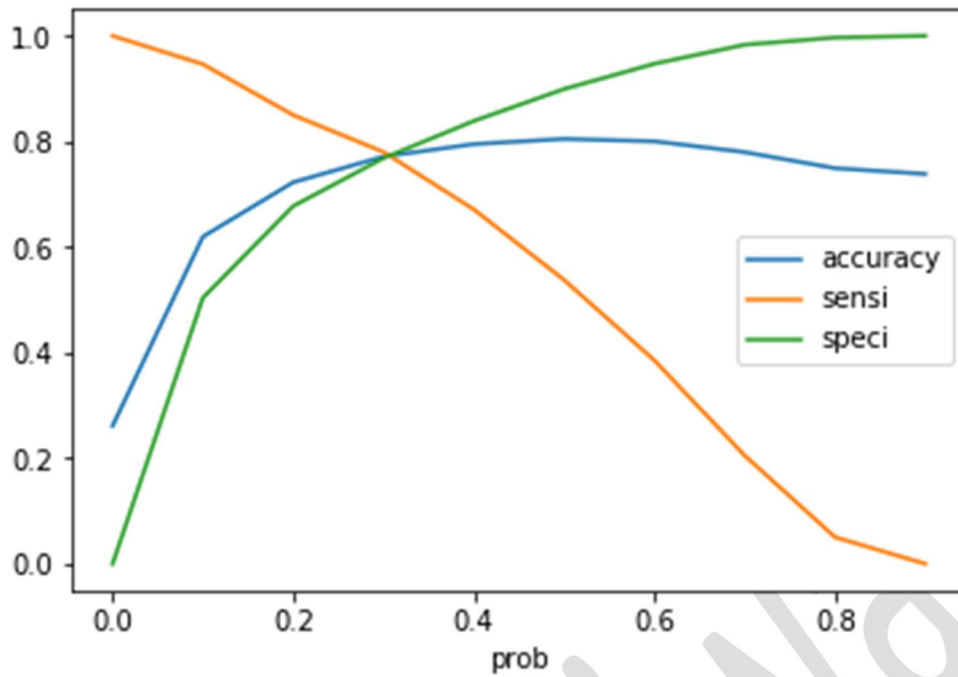
Sensitivity and Specificity

$$\text{Sensitivity} = \frac{\text{No of actual yes correctly predicted (TP)}}{\text{No of actual Yes (FN + TP)}}$$

Sensitivity is nothing but TPR

$$\text{Specificity} = \frac{\text{No of actual Nos correctly predicted (TN)}}{\text{No of actual Nos (TN + FP)}}$$

Specificity is nothing but TNR



From the above chart anything which is greater than the probability of 0.3 are positives and anything which is lesser than 0.3 are negatives