

This is a power conversion element that interfaces a nonlinear time domain model, in the Hammerstein-Wiener (HW) framework, to the OpenDSS dynamics mode. The model senses terminal voltage and updates the injected current at each OpenDSS time step. Figure 1 shows the relationship between HW and OpenDSS domains, and it defines the key signal locations to reference when reading the Delphi code. In a snapshot mode, the model injected current will be constant, as determined by its ratings and initial power output level. The initial application is for photovoltaic (PV) inverter modeling, and the parameters are defined in those terms. The PV inverter models began with a project sponsored by EPRI at the University of Pittsburgh [1, 2], and they are intended to fill a gap between very detailed [3] and very simple [4] models. The models have since been updated with a phase-locked loop (PLL) implementation for use in protection studies [5]¹.

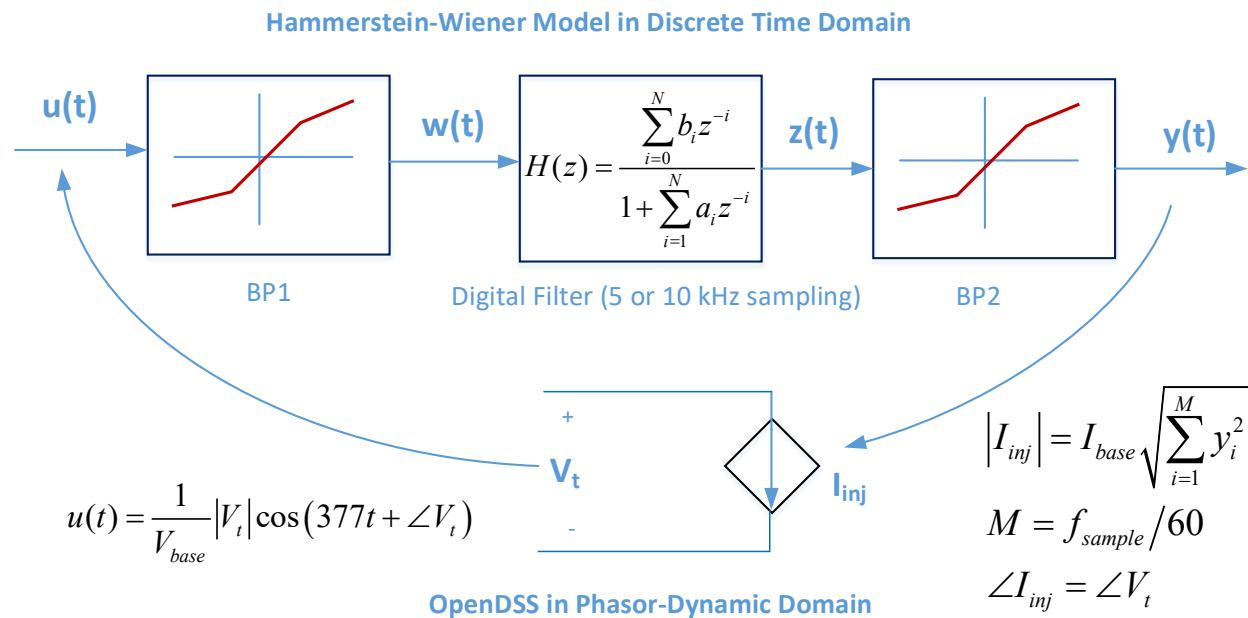


Figure 1: Interface between HW and OpenDSS solution variables

VCCS Input Parameters

Input parameters are listed below. The HW components in Figure 1 work on per-unit variables, so the user may only need to adjust **Ppct**, **Prated** and **Vrated** for specific applications. There are now two available VCCS operating modes, flagged by the value of **RMSmode**.

- Basefreq: as other PC elements (assumed 60 in Figure 1)
- BP1: XYCurve defining the input piecewise linear block in Figure 1; not used in RMS mode.
- BP2: XYCurve defining the output piecewise linear block in Figure 1; not used in RMS mode.
- Bus1: as other PC elements
- Enabled: as other PC elements
- Filter: XYCurve defining the infinite impulse response (IIR) digital filter coefficients in Figure 1. X values are the numerator coefficients and Y values are the denominator coefficients, and note

¹ This material is based upon work supported by the U.S. Department of Energy's Office of Energy Efficiency and Renewable Energy (EERE) under Solar Energy Technologies Office (SETO) Agreement Number 34233.

that $a_0=1$ must be input explicitly. This also enforces equal order in numerator and denominator. In RMSmode, this is typically a second-order digital filter implementation of the phase-locked loop, but other control dynamics in a fast-phasor model could be implemented in this $H(z)$.

- Fsample: sampling rate for $H(z)$, either 5 kHz or 10 kHz in this project. The time step should be an integer multiple of the sample step.
- Imaxpu: for RMSmode only, the nominal maximum current injection in per-unit of rated current.
- Irmstau: for RMSmode only, the time constant of a low-pass filter injecting RMS current from the controller.
- Like: as other PC elements
- Phases: as other PC elements, but only 1-phase implemented now. 3-phase under development.
- Ppct: real power output in snapshot mode, based on Prated. Unity power factor assumed.
- Prated: inverter's rated power in Watts
- Spectrum: as other PC elements, but not implemented here.
- Vrated: rated line-to-line voltage (3-phase) or line-to-neutral voltage (1-phase) in volts
- Vrmstau: for RMSmode only, the time constant of a low-pass filter sensing RMS voltage.

HWPLL.DSS and HWPLL3.DSS

This file illustrates a second-order phase-locked-loop (PLL) controller in phasor domain [2]. The $H(z)$ defined in lines 5-7 implements a second-order PLL with some overshoot, seen in the **blue** trace of Figure 2 (left). This overshoot is not actually injected into the circuit because of the 50 ms irmstau time constant specified in line 10, with effect seen in the **magenta** trace. Based on the sensed rms voltage, i.e., the **black** trace, the VCCS calculates **lpwr** (**red** trace) to maintain the pre-event real power output. However, lpwr is affected by $H(z)$ and then Irmstau. Figure 2 (right) shows the per-unit voltage and current at the VCCS terminals. In this example, $H(z)$ and the time constants have been chosen to provide clear illustration of their impacts; these are not necessarily typical values for a real inverter.

```

1 Clear
2 new circuit.HWPLL
3 ~ basekv=4.16 pu=1.0 angle=0 phases=3 bus1=SourceBus
4 ~ r1=0.029 x1=0.058 r0=0.014 x0=0.029
5 New XYcurve.z_pll npts=3
6 ~ xarray=[ 1.0000 -1.9852 0.9853] // denominator
7 ~ yarray=[ 0.0000 0.0148 -0.0147] // numerator
8 New vccs.pv Phases=1 Bus1=SourceBus.1 Prated=125e3 Vrated=2400 Ppct=100
9 ~ filter='z_pll' fsample=10000 rmsmode=true imaxpu=1.15
10 ~ vrmstau=0.01 irmstau=0.05
11 new fault.flt bus1=Sourcebus.1 phases=1 r=0.001 temporary=yes ontime=0.1
12 new monitor.invvi element=vccs.pv terminal=1 mode=0
13 new monitor.invst element=vccs.pv terminal=1 mode=3
14 Set Voltagebases=[4.16]
15 set maxiterations=100
16 calcv
17 set mode=snap
18 solve
19 set mode=dynamic
20 set stepsize=0.0001 // 0.0001 matches fsample
21 set number=2500 // 2500 matches fsample
22 Solve
23 plot type=monitor obj=invvi channels=[1 3] bases=[2400 52.083]
24 plot type=monitor obj=invst channels=[1 2 3 4]
```

Figure 3 shows the voltage, current, and power injection from a 3-phase version of this inverter, rated 375 kW at 4160 V line-to-line. The input file is distributed as **HWPLL3.dss**. The state variable outputs are very similar to Figure 2 (left) for the single-phase inverter. The three-phase inverter continues to produce current and power on the unfaulted phases during the single line to ground fault.

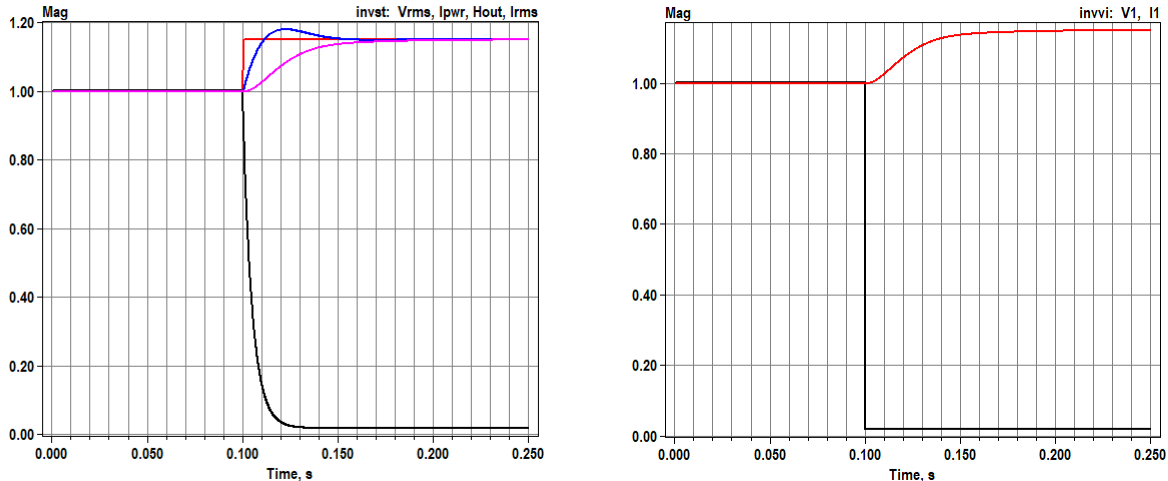


Figure 2: Phasor-mode 1-phase VCCS results for controller state variables (left) and the terminal voltage and current (right).

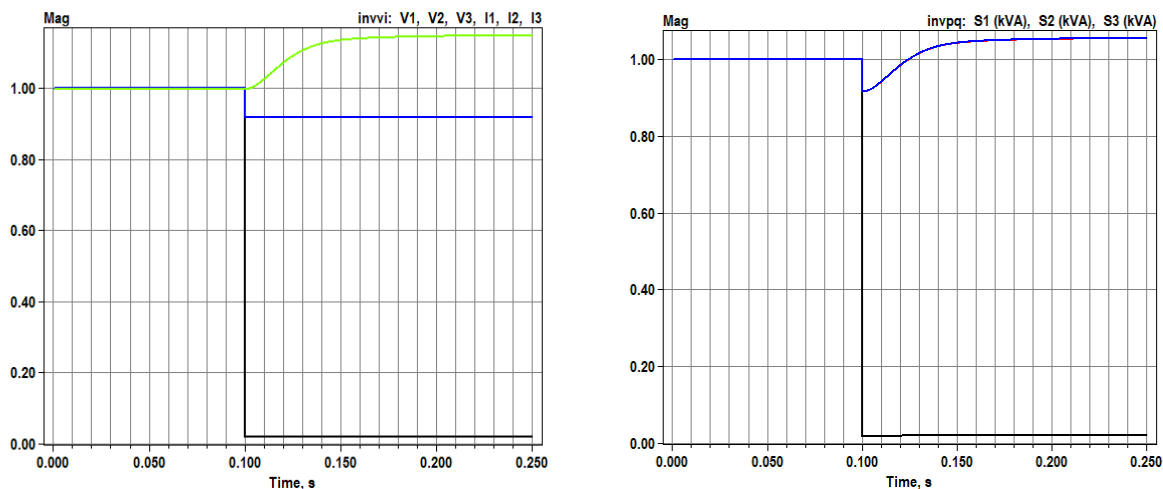


Figure 3: Phase-mode 3-phase VCCS voltages and currents (left) and apparent powers (right).

HWTest.DSS

This file illustrates two inverter models in a snapshot solution. The inverters are connected to a 360-volt source, which matches the lab tests done at 208 volts. The short circuit current supplied by the source is 7354 amps. When **phases=3**, the VCCS component works in snapshot mode, but not yet in dynamics mode. **BP1**, **BP2**, **Filter** and **Fsample** have no effect in snapshot mode. The initial currents will be

$$I_{SM41} = \frac{3000}{208} \frac{100}{100} = 14.42 \text{ and } I_{SM43} = \frac{3000}{360\sqrt{3}} \frac{50}{100} = 2.41$$

```
Clear
new circuit.HWTest
~ basekv=0.360 pu=1.0 angle=0 phases=3 bus1=SourceBus r1=0.02 r0=0.02 x1=0.02 x0=0.02
```

```

redirect HW_Inverters.txt

New VCCS.PV1 Phases=1 Bus1=SourceBus.1 Prated=3000 Vrated=208
~ Ppct=100 bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000

New VCCS.PV3 Phases=3 Bus1=SourceBus Prated=3000 Vrated=360
~ Ppct= 50 bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000

Set Voltagebases=[0.360]
set maxiterations=100
calcv
Solve

```

HWDyn.dss

The file that runs a dynamics test has been set up to run either the single-phase inverter or the microinverter, feeding a bolted fault with source impedance adjusted to match that of Pitt's electric power lab. The fault's **ontime** value will determine when the HW model departs from its initial condition. In this case, **Fsample** is 10 kHz, so the OpenDSS time step must be at least 0.1 ms, but it can be longer. The HW model can run at a faster time step within each OpenDSS time step.

```

Clear
// EPSL impedance is 10% on 75 kVA positive sequence, 5% zero sequence,
assume X/R = 2
new circuit.HWDynamic
~ basekv=0.360 pu=1.0 angle=0 phases=3 bus1=SourceBus r1=0.029 x1=0.058
r0=0.014 x0=0.029

redirect HW_Inverters.txt
New vccs.pv Phases=1 Bus1=SourceBus.1 Prated=3000 Vrated=208 Ppct=100
~ bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000
//New vccs.pv Phases=1 Bus1=SourceBus.1 Prated=190 Vrated=208 Ppct=89.5
//~ bp1='bp1_micro' bp2='bp2_micro' filter='z_micro' fsample=10000

new fault.flt bus1=Sourcebus.1 phases=1 r=0.001 temporary=yes ontime=0.1

new monitor.invvi element=vccs.pv terminal=1 mode=0
new monitor.invpq element=vccs.pv terminal=1 mode=1
new monitor.invst element=vccs.pv terminal=1 mode=3
new monitor.fltvi element=fault.flt terminal=1 mode=0

Set Voltagebases=[0.360]
set maxiterations=100
calcv

set mode=snap
solve

set mode=dynamic
set stepsize=0.01 // 0.0001 matches fsample
set number=25 // 2500 matches fsample
Solve

```

HW_Inverters.txt

This included file defines **BP1**, **BP2**, and a 14th-order filter for the microinverter, listed below. The single-phase inverter data is formatted the same way, but it has a 51-order filter, which means its transient response will last longer.

```
// library model for microinverter

New XYcurve.bp1_micro npts=3
~ xarray=[-0.882023 0.0 0.882023]
~ yarray=[-0.19      0.0 0.19]

New XYcurve.bp2_micro npts=5
~ xarray=[-0.085467 -0.0202 0.0 0.0202 0.085467]
~ yarray=[ 4.59572  1.0    0.0 -1.0   -4.59572]

New XYcurve.z_micro npts=14
~ xarray=[ 1.00000000000000 -1.3802100241988 -0.9341004900495 1.1196620891546
0.1499829369937 1.2123723040884 -0.7654392492287 -0.9113338678997
0.3694835076144 0.1034830928158 0.1549604084080 -0.2209879303901
0.1373924816843 -0.0352249177928 ] // denominator
~ yarray=[ 0.00000000000000 -0.2328126380366 0.9436331671129 -0.5290906112039
-1.2586072419992 0.6136072759695 0.5705618604200 1.00000000000000 -
0.5053547399078 -1.1387058093285 -0.0677012182563 0.5067831545610
0.4003099336092 -0.3026288423351 ] // numerator
```

Example BP1 and BP2

Sample non-linear blocks for the single-phase inverter are shown in Figure 4. They do not necessarily display appropriate symmetry and offset characteristics. Work is ongoing to improve the stability of the fitted model, some of which has been reflected in the non-linear blocks defined in HW_Inverters.txt listed previously. Note that **BP2** decreases with X, which required a bug fix to the XYCurve object in OpenDSS for reverse lookup. It's possible that InvControl is also affected by this fix.

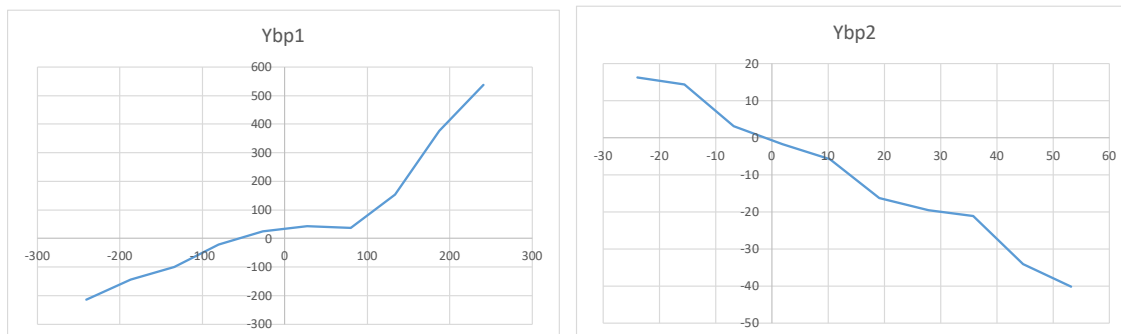


Figure 4: Sample 10-point nonlinear blocks BP1 and BP2

Single-phase Inverter Sample Outputs

Figure 5 shows the single-phase inverter model running at OpenDSS time steps of 0.1 ms. On the left, internal HW model current waveform is in black, RMS in red and peak in blue. The model initialization is smooth, but steady state is not well established until about 0.1 seconds elapse. The red trace on the left is the per-unit RMS current injected into the feeder network. On the right, this is plotted in Amps.

In Figure 5, the OpenDSS time step matches the HW model time step. When OpenDSS runs at a slower time step, the HW model still runs internally at **Fsample**=10 kHz. However, the output is only sampled at the slower time step, and the current injections are only updated at the slower time step. Figure 6 shows this effect. Especially at 10 ms time step, the waveform is “choppy” but the RMS vs. time is not affected very much.

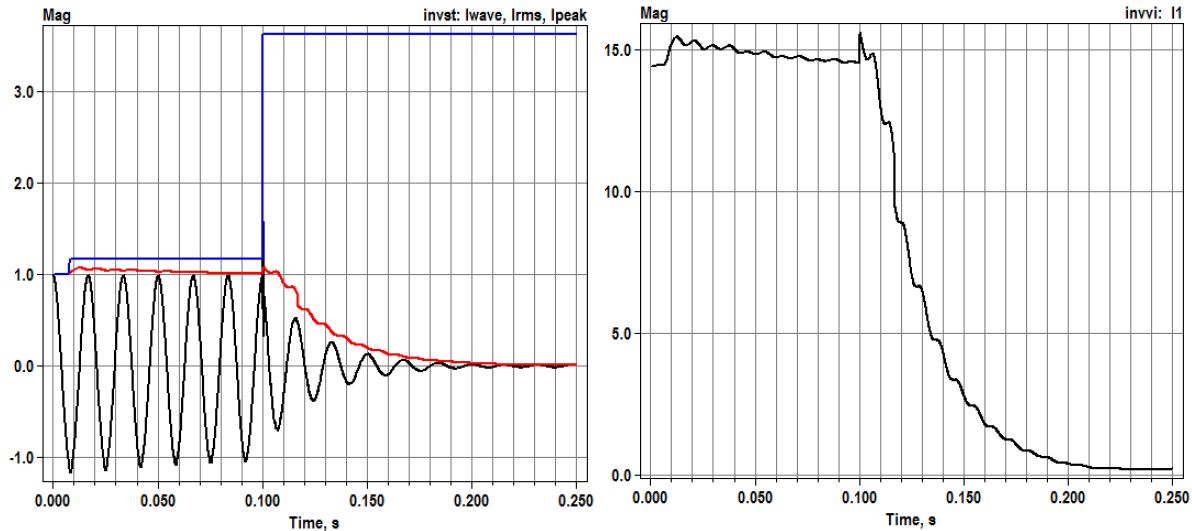


Figure 5: Current waveform, RMS and peak state variables [per-unit] for single-phase inverter. $h=0.1$ ms (left) and injected current into the feeder [Amps] (right)

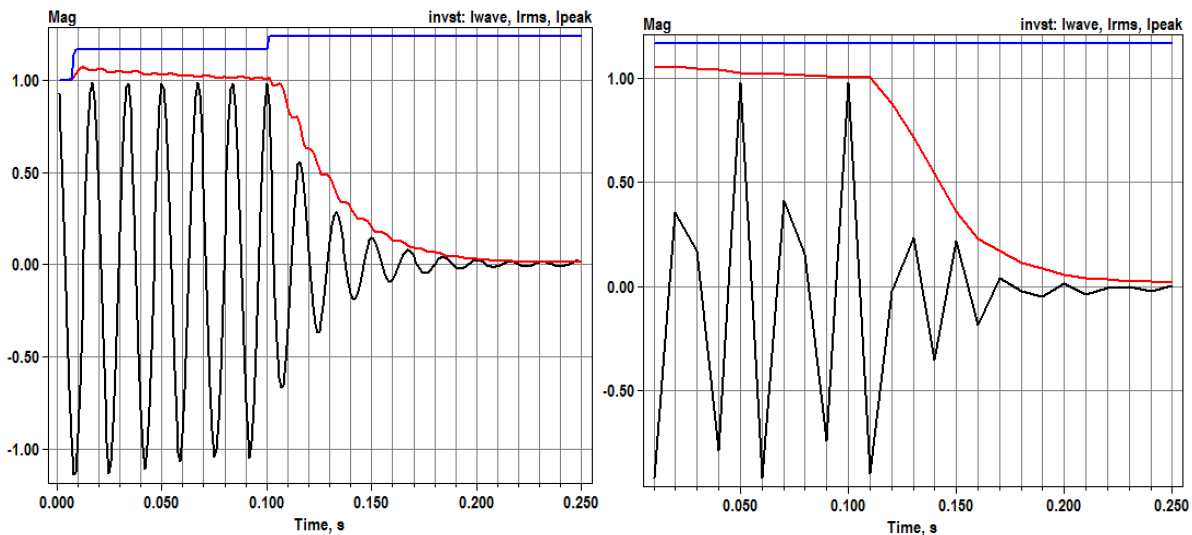


Figure 6: Current waveform, RMS and peak state variables [pu] for single-phase inverter. $h=1$ ms (left) and 10 ms (right)

Microinverter Sample Outputs

Figure 7 shows a microinverter response to the same fault. With a 14th-order filter at 10 kHz sampling rate, the transient response is shorter in duration. Initialization is smooth, but the accuracy could be improved. The model captures a transient current peak that loads the inverter terminal voltage. When OpenDSS runs at a step longer than 0.1 ms, this loading effect is not captured because the RMS function

smooths the current peak. Therefore, the peak current is reduced when the OpenDSS time step increases, shown in Figure 6 compared to Figure 5, or Figure 8 compared to Figure 7.

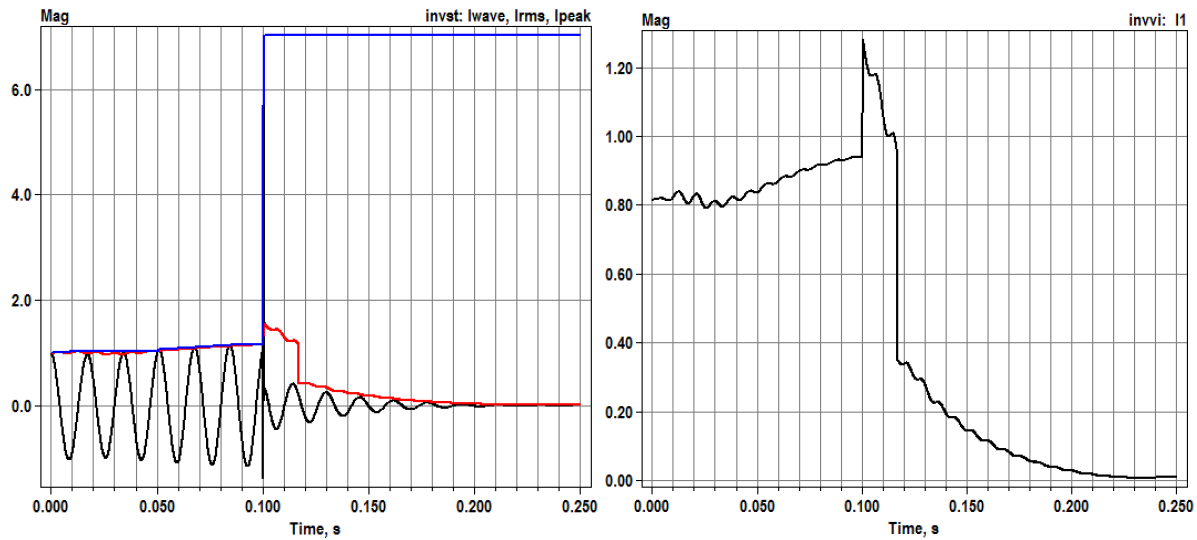


Figure 7: Microinverter current state variables [per-unit] (left) and injected current into the feeder [Amps] (right) at $h=0.1$ ms.

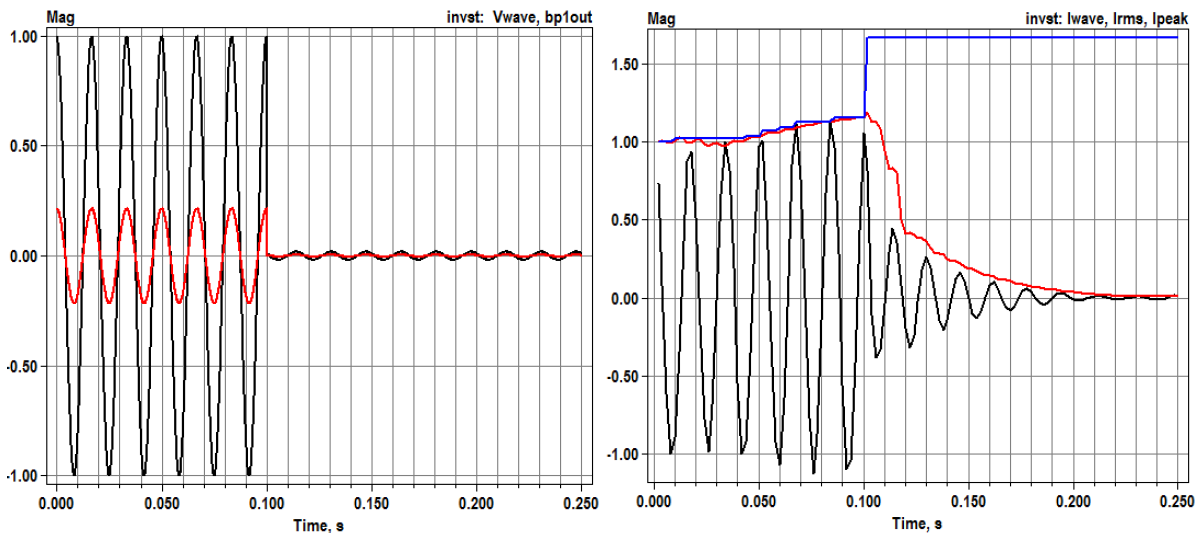


Figure 8: Microinverter voltage state variables (left) and current state variables (right) at $h=2$ ms.

Code Listings

The most significant parts of the VCCS code define, initialize, and integrate the state variables. Listings follow.

Evaluating $H(z)$ in Figure 1 requires history storage for both input and output. A second copy of both history terms is required for the predictor and corrector steps. Otherwise, when the OpenDSS and HW steps are unequal, the last step's history could be corrupted by a partial update before the corrector step initiates. The history terms are **z**, **whist**, **zlast** and **wlast**, allocated to a size determined from the base and sampling frequencies. A ring buffer indexing scheme is used to manage this storage, with helper functions MapIdx and OffsetIdx.

The overloaded InitStateVars procedure extracts terminal voltage and current from the most recent snapshot solution. Then it steps back in time at the sampling frequency to initialize the history terms. The history of **z** is determined from the history of current, **i**, passed in reverse through **BP2**. The HW model current uses generator convention while the OpenDSS current uses passive convention, leading to a negative sign on the initial values of **z**.

The overloaded IntegrateStates procedure is called twice in each OpenDSS time step, first as predictor (Forward Euler) and then as corrector (Backward Trapezoidal). Each time, it extracts terminal voltage and ensures that **whist** and **z** begin afresh from the previous OpenDSS time step. Then, it runs through the **BP1**, **z**, and **BP2** evaluations defined in Figure 1 for the number of sampling steps contained in an OpenDSS time step. RMS current is calculated “brute force” at the end of the OpenDSS time step, for both predictor and corrector. This value, **slrms**, is later injected into the grid via the overloaded procedure GetInjCurrent (not listed below). Note that the current angle updates are not yet implemented. The peak current state variable is checked every HW step to catch “fast” peaks that might not appear in monitor output. The other state variables, and the **wlast** / **zlast** history terms, are only updated at each OpenDSS corrector time step.

```
private
  Fbp1: TXYcurveObj;
  Fbp1_name: String;
  Fbp2: TXYcurveObj;
  Fbp2_name: String;
  Ffilter: TXYcurveObj;
  Ffilter_name: String;
  BaseCurr: double; // line current at Ppct
  BaseVolt: double; // line-to-neutral voltage at Vrated
  FsampleFreq: double; // discretization frequency for Z filter
  Fwinlen: integer;
  Ffiltlen: integer;
  Irated: double; // line current at full output
  Fkv: double; // scale voltage to HW pu input
  Fki: double; // scale HW pu output to current

  // Support for Dynamics Mode - PU of BaseVolt and BaseCurr
  sVwave: double;
  sIwave: double;
  sIrms: double;
  sIpeak: double;
  sBP1out: double;
  sFilterout: double;
  vlast: complex;
  y2: pDoubleArray;
  z: pDoubleArray; // current digital filter history terms
  whist: pDoubleArray;
  zlast: pDoubleArray; // update only after the corrector step
  wlast: pDoubleArray;
  sIdxU: integer; // ring buffer index for z and whist
  sIdxY: integer; // ring buffer index for y2 (rms current)
  y2sum: double;

  // helper functions for ring buffer indexing, 1..len
  function MapIdx(idx, len: integer):integer;
  begin
    while idx <= 0 do idx := idx + len;

```



```

    Result := idx mod (len + 1);
    if Result = 0 then Result := 1;
end;

function OffsetIdx(idx, offset, len: integer):integer;
begin
    Result := MapIdx(idx+offset, len);
end;

// support for DYNAMICMODE
// NB: The test data and HW model used source convention (I and V in phase)
//     However, OpenDSS uses the load convention
procedure TVCCSObj.InitStateVars;
var
    d, wt, wd, val, iang, vang: double;
    i, k: integer;
begin
    // initialize outputs from the terminal conditions
    ComputeITerminal;
    iang := cang(ITerminal^1);
    vang := cang(Vterminal^1);
    sVwave := cabs(Vterminal^1) / BaseVolt;
    sIrms := cabs(ITerminal^1) / BaseCurr;
    sIwave := sIrms;
    sIpeak := sIrms;
    sBPlout := 0;
    sFilterout := 0;
    vlast := cdivreal (Vterminal^1, BaseVolt);

    // initialize the history terms for HW model source convention
    d := 1 / FsampleFreq;
    wd := 2 * Pi * ActiveSolutionObj.Frequency * d;
    for i := 1 to Ffiltlen do begin
        wt := vang - wd * (Ffiltlen - i);
        whist[i] := 0;
        whist[i] := Fbp1.GetYValue(sVwave * cos(wt));
        wlast[i] := whist[i];
    end;
    for i := 1 to Fwinlen do begin
        wt := iang - wd * (Fwinlen - i);
        val := sIrms * cos(wt); // current by passive sign convention
        y2[i] := val * val;
        k := i - Fwinlen + Ffiltlen;
        if k > 0 then begin
            z[k] := -Fbp2.GetXvalue (val); // HW history with generator convention
            zlast[k] := z[k];
        end;
    end;

    // initialize the ring buffer indices; these increment by 1 before actual use
    sIdxU := 0;
    sIdxY := 0;
end;

// this is called twice per dynamic time step; predictor then corrector
procedure TVCCSObj.IntegrateStates;
var
    t, h, d, f, w, wt: double;

```

```

    vre, vim, vin, scale, y: double;
    nstep, i, k, corrector: integer;
    vnow: complex;
    iu, iy: integer; // local copies of sIdxU and sIdxY for predictor
begin
    if not Closed[1] then begin
        ShutoffInjections;
        exit;
    end;
    ComputeIterminal;

    t := ActiveSolutionObj.DynaVars.t;
    h := ActiveSolutionObj.DynaVars.h;
    f := ActiveSolutionObj.Frequency;
    corrector := ActiveSolutionObj.DynaVars.IterationFlag;
    d := 1 / FSampleFreq;
    nstep := trunc (1e-6 + h/d);
    w := 2 * Pi * f;

    vnow := cdivreal (Vterminal^[1], BaseVolt);
    vin := 0;
    y := 0;
    iu := sIdxU;
    iy := sIdxY;
    for k := 1 to Ffiltlen do begin
        z[k] := zlast[k];
        whist[k] := wlast[k];
    end;
    for i:=1 to nstep do begin
        iu := OffsetIdx (iu, 1, Ffiltlen);
        // push input voltage waveform through the first PWL block
        scale := 1.0 * i / nstep;
        vre := vlast.re + (vnow.re - vlast.re) * scale;
        vim := vlast.im + (vnow.im - vlast.im) * scale;
        wt := w * (t - h + i * d);
        vin := (vre * cos(wt) + vim * sin(wt));
        whist[iu] := Fbp1.GetYValue(vin);
        // apply the filter and second PWL block
        z[iu] := 0;
        for k := 1 to Ffiltlen do begin
            z[iu] := z[iu] + Ffilter.Yvalue_pt[k] * whist[MapIdx(iu-k+1,Ffiltlen)];
        end;
        for k := 2 to Ffiltlen do begin
            z[iu] := z[iu] - Ffilter.Xvalue_pt[k] * z[MapIdx(iu-k+1,Ffiltlen)];
        end;
        y := Fbp2.GetYValue(z[iu]);
        // updating outputs
        if (corrector = 1) and (abs(y) > sIpeak) then
            sIpeak := abs(y); // catching the fastest peaks
        // update the RMS
        iy := OffsetIdx (iy, 1, Fwinlen);
        y2[iy] := y * y; // brute-force RMS update
        if i = nstep then begin
            y2sum := 0.0;
            for k := 1 to Fwinlen do y2sum := y2sum + y2[k];
            sIrms := sqrt(2.0 * y2sum / Fwinlen); // TODO - this is the magnitude, what
            about angle?
        end;
    end;

```

```

end;

if corrector = 1 then begin
  sIdxU := iu;
  sIdxY := iy;
  vlast := vnow;
  sVwave := vin;
  sBPlout := whist[sIdxU];
  sFilterout := z[sIdxU];
  sIwave := y;
  for k := 1 to FFiltlen do begin
    zlast[k] := z[k];
    wlast[k] := whist[k];
  end;
end;
end;
end;

```

DG_Prot_Fdr.dss

Our last example illustrates use of the VCCS model in an IEEE test feeder for DG protection analysis. See Figure 9, with feeder data defined in [6]. The DG was originally assumed to contribute fault current as a rotating machine, but here the source is a PV inverter, represented with a **VCCS**. Note that the VCCS does not emulate solar panel efficiency, power fluctuations, or smart inverter control; for those features, please use other components of OpenDSS (e.g. PVSystem, InvControl, ExpControl). In Figure 9, we will apply single-line-to-ground faults (SLGF) at the feeder mid-point location, bus **Bm** or fault location **3**.

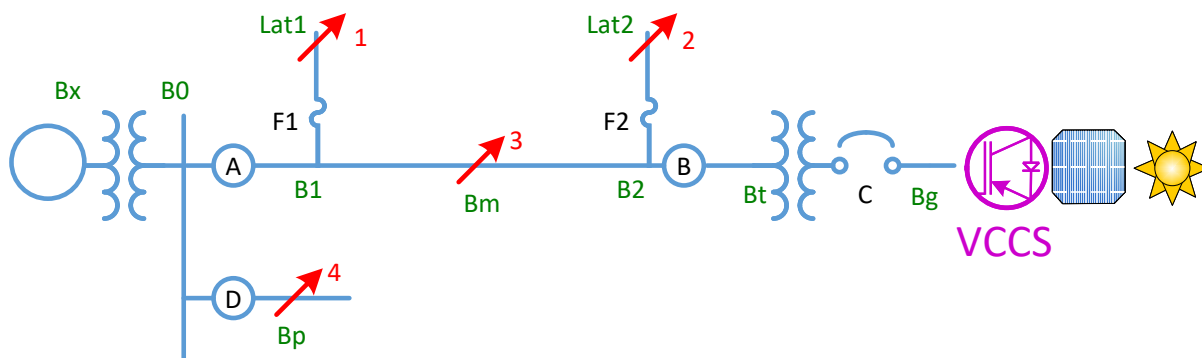


Figure 9: IEEE test feeder for DG protection analysis [6]

Here is a partial listing of the test file **DG_Prot_Fdr.dss**, showing the 1.7 MVA wind turbine generator commented out, and an equivalent 1.7 MW PV generator comprised of single-phase inverters. In either case, a 1700-kVA wye/wye interconnection transformer interfaces the DG to the primary feeder.

```

// DG interconnection transformer and a conventional machine
new Transformer.Tg phases=3 windings=2 buses=(Bt Bg) conns=(Wye Wye)
~ kvs='12.47 0.36' kvas='1700 1700' taps='1 1' XHL=5
//new Vsource.WindGen1 bus1=Bg basekv=0.36 pu=1.0 angle=-48.5
//~ X1=0.0127 R1=0.0 X0=100.0 R0=0.0

redirect HW_Inverters.dat
New vccs.pv1 Phases=1 Bus1=Bg.1 Prated=567e3 Vrated=208 Ppct=100
~ bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000
New vccs.pv2 Phases=1 Bus1=Bg.2 like=pv1
New vccs.pv3 Phases=1 Bus1=Bg.3 like=pv1

```

```
// Inverter Model Monitors
new monitor.invst1 element=vccs.pv1 terminal=1 mode=3
new monitor.invst2 element=vccs.pv2 terminal=1 mode=3
new monitor.invst3 element=vccs.pv3 terminal=1 mode=3
new monitor.invt1 element=vccs.pv1 terminal=1 mode=0
new monitor.invt2 element=vccs.pv2 terminal=1 mode=0
new monitor.invt3 element=vccs.pv3 terminal=1 mode=0
```

Figure 10 shows the current and voltage through recloser B, on the high side of the interconnection transformer, with a 1700-kW PV inverter source back-feeding the fault at Bm. The fault occurs at 0.2 seconds, just after steady-state DG output currents have stabilized. The faulted phase voltage (Figure 10 right) collapses almost immediately. Figure 11 shows the same fault response for a Thevenin equivalent source in place of the PV. The Thevenin impedance is sized to produce 6 pu short-circuit current at the source terminals based on 1700 kVA. The initial power is 1721 kW. As a result, the fault contribution is higher and the feeder primary voltage on the faulted phase, at recloser B, is maintained at a low level indefinitely.

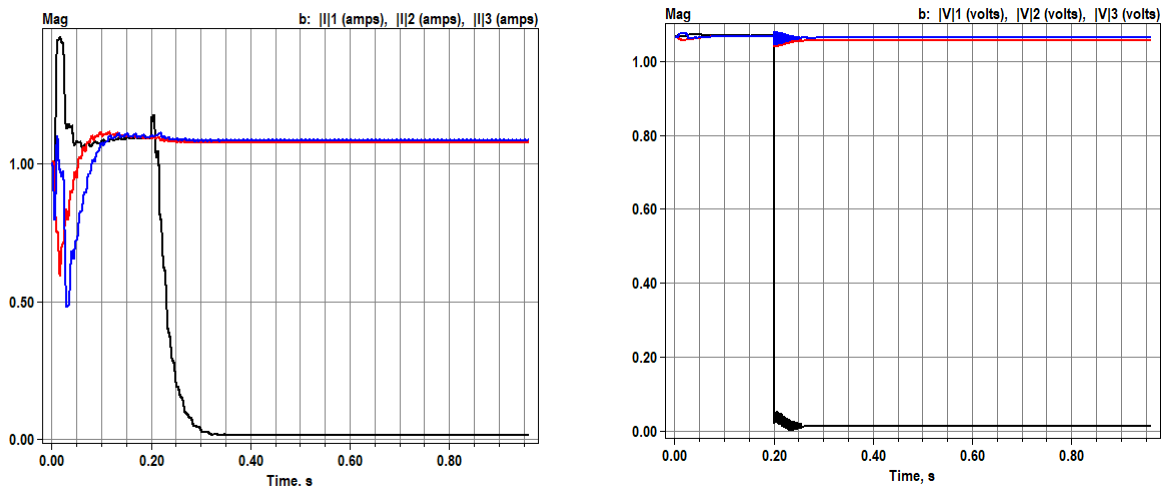


Figure 10: Per-unit currents (left) and voltages (right) at recloser B with 1.7 MW PV and single-phase inverter models

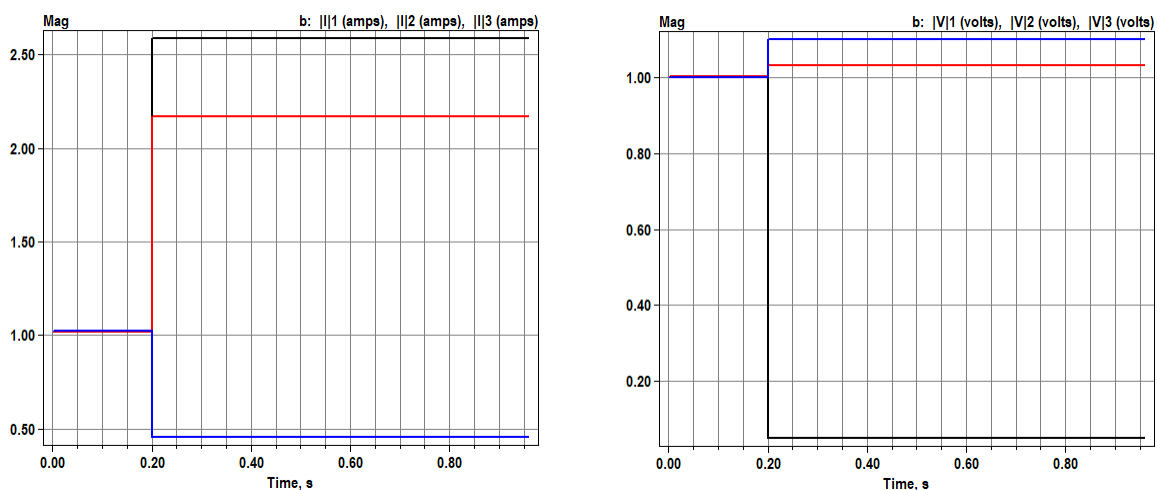


Figure 11: Per-unit currents (left) and voltages (right) at recloser B with 1.7 MW rotating machine (Thevenin equivalent)

The same case can be run with a PLL model of the inverter:

```

New XYcurve.z_pll npts=3
~ xarray=[ 1.0000 -1.9852  0.9853] // denominator
~ yarray=[ 0.0000  0.0148 -0.0147] // numerator
New vccs.pv Phases=3 Bus1=Bg Prated=1700e3 Vrated=360 Ppct=100
~ filter='z_pll' fsample=10000 rmsmode=true imaxpu=1.15
~ vrmstau=0.01 irmstau=0.05

```

Results are shown in Figure 12. During the first 0.2 seconds, the PLL reduces the current in order to produce rated power at the 1.07 per-unit pre-fault terminal voltage. After the fault, the PV inverter contributes up to 1.15 per-unit current on each phase through the interconnection transformer. Some oscillations appear on the post-fault voltages. Addition of load might dampen those oscillations. A relay can be added to `vccs.pv` that will cease-to-energize, i.e., shut off current injection, when it trips.

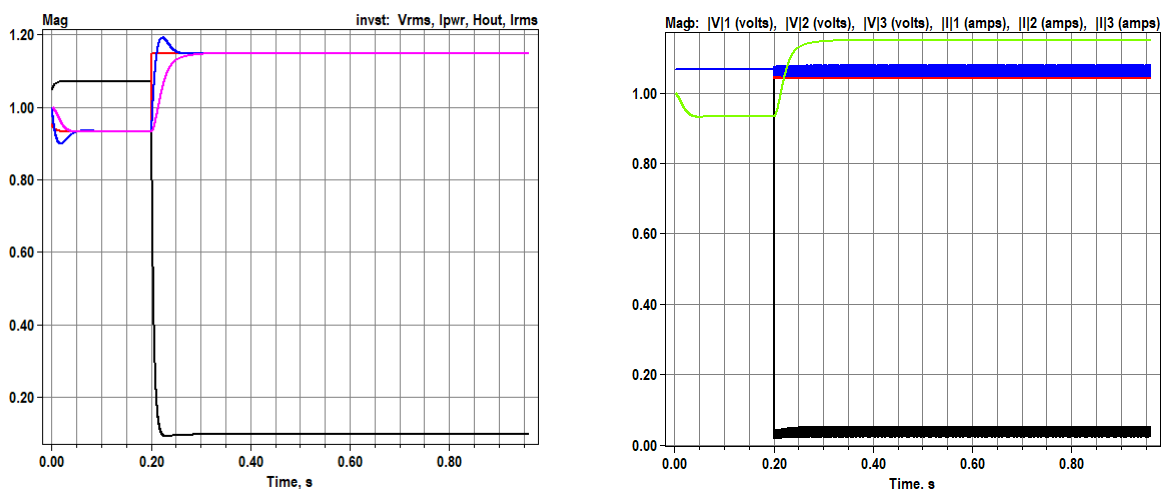


Figure 12: DG protection feeder fault with PLL model, p.u. state variables (left), recloser B p.u. voltages and currents (right).

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